

Prof Douglas Paul

**Director: James Watt Nanofabrication Centre
University of Glasgow
U.K.**



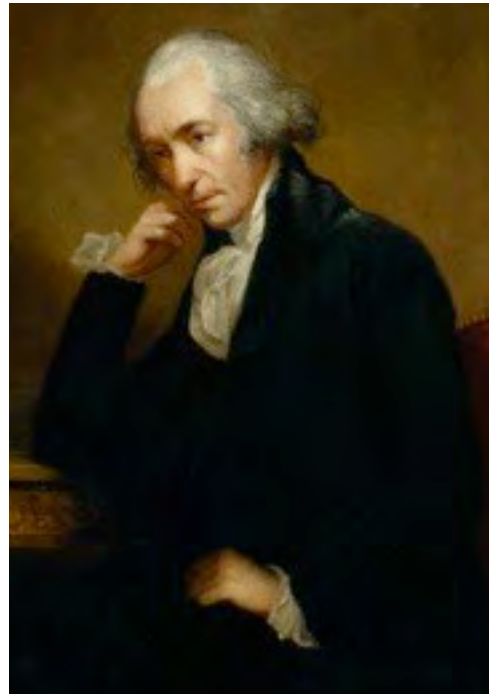
- **Established in 1451**
- **7 Nobel Laureates, 2 SI units, ultrasound, television, etc.....**
- **16,500 undergraduates, 5,000 graduates and 5,000 adult students**
- **£186M research income pa**



- **400 years in High Street**
- **Moved to Gilmorehill
in 1870**
- **Neo-gothic buildings by
Gilbert Scott**



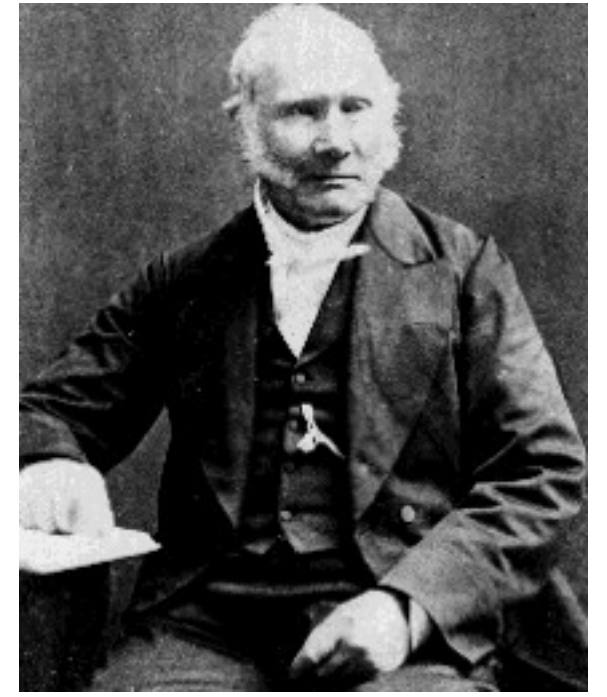
**William Thomson
(Lord Kelvin)**



James Watt



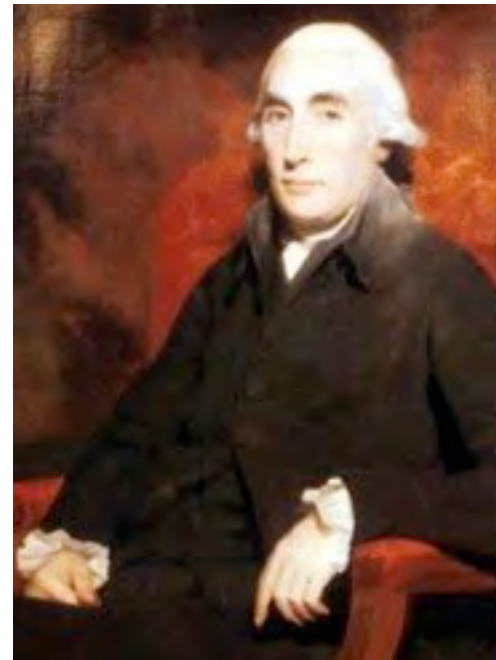
**William John
Macquorn Rankine**



Rev Robert Stirling



Rev John Kerr



Joseph Black



John Logie Baird



Adam Smith



E-beam lithography



Süss MA6 optical lith

14 RIE / PECVD / ALD



- 750m² (+150 m²) cleanroom - pseudo-industrial operation

- 15 technicians + 4 PhD research technologists

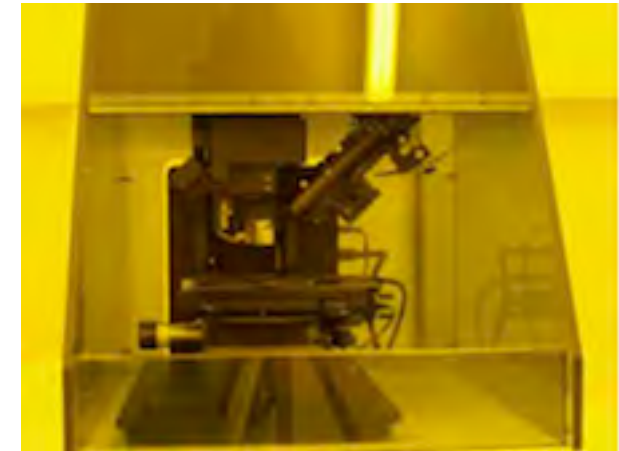
- Processes include: MMICs, III-V, Si/SiGe/Ge, integrated photonics, metamaterials, MEMS (microfluidics)

- Part of EPSRC III-V National Facility
& STFC Kelvin-Rutherford Facility

- Commercial access through Kelvin NanoTechnology

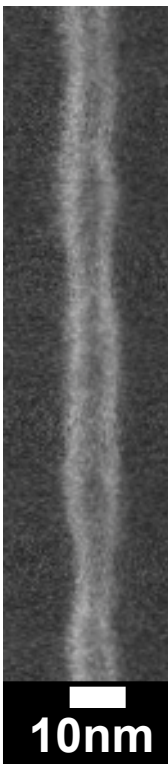
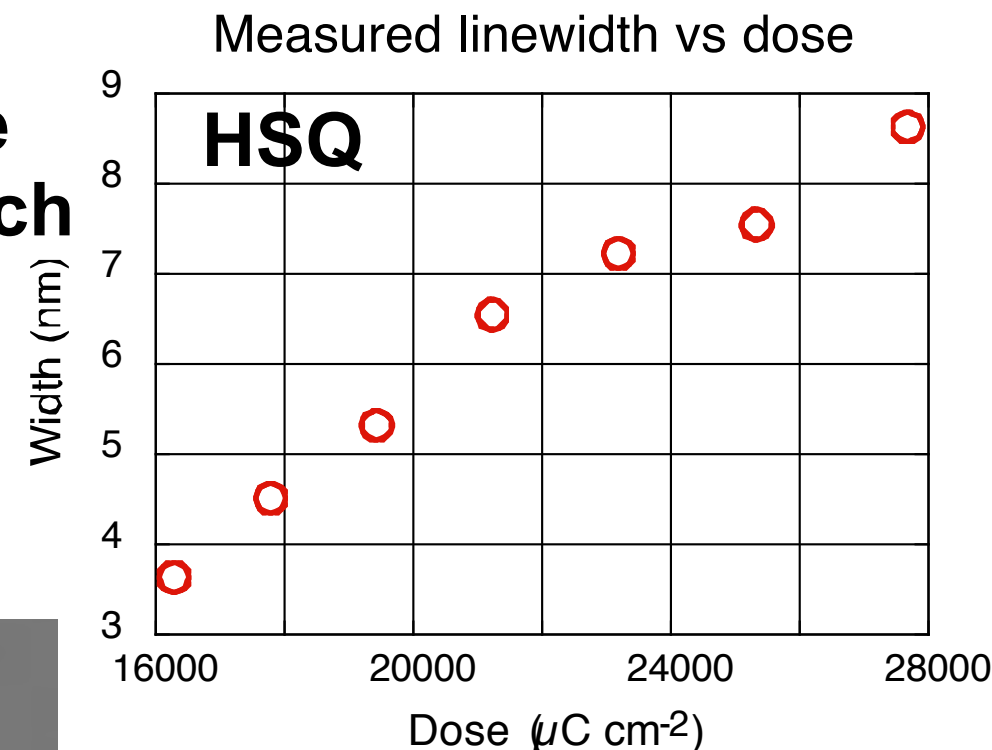
- <http://www.jwnc.gla.ac.uk/>

6 Metal dep tools 4 SEMs: Hitachi S4700 Veeco: AFMs

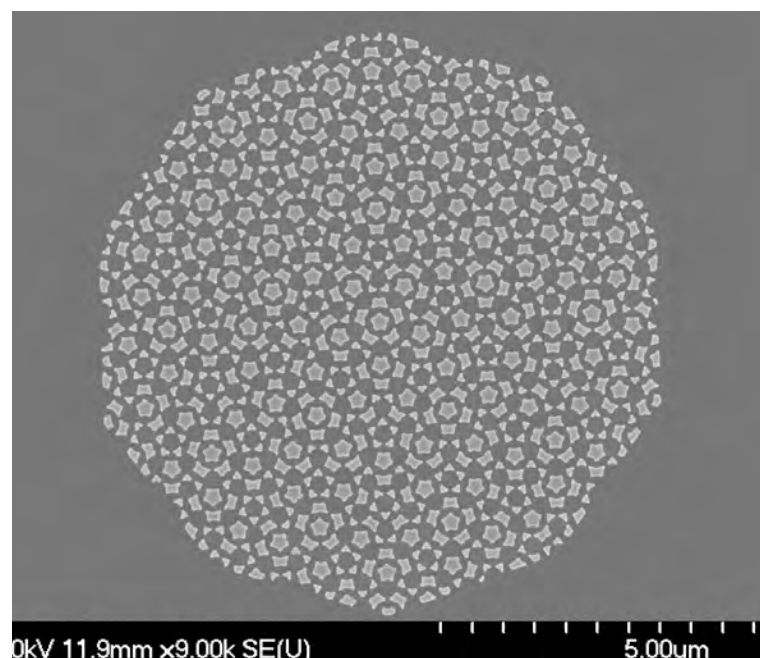


**30 years
experience
of e-beam
lithography**

**Sub-5 nm single-line
lithography for research**



Vistec VB6



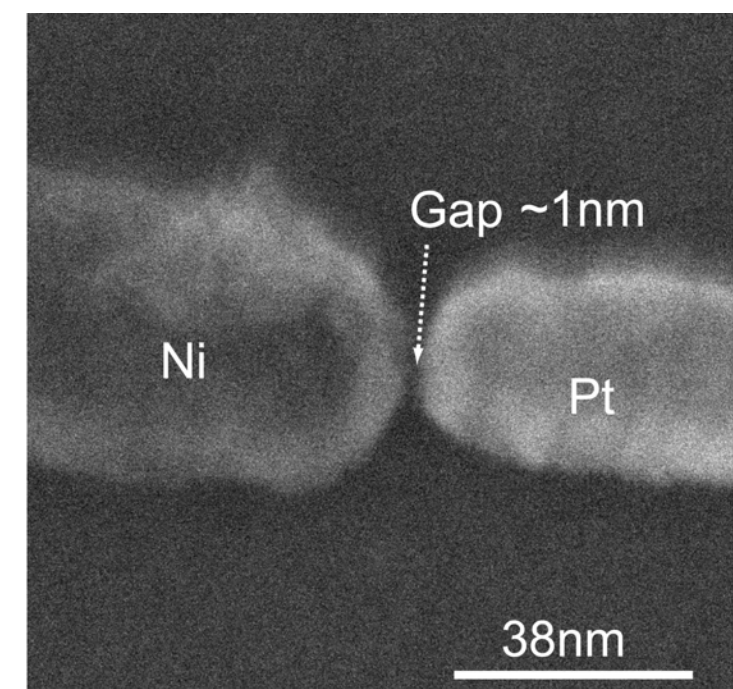
**Penrose tile: layer-to-layer
alignment 0.46 nm rms**



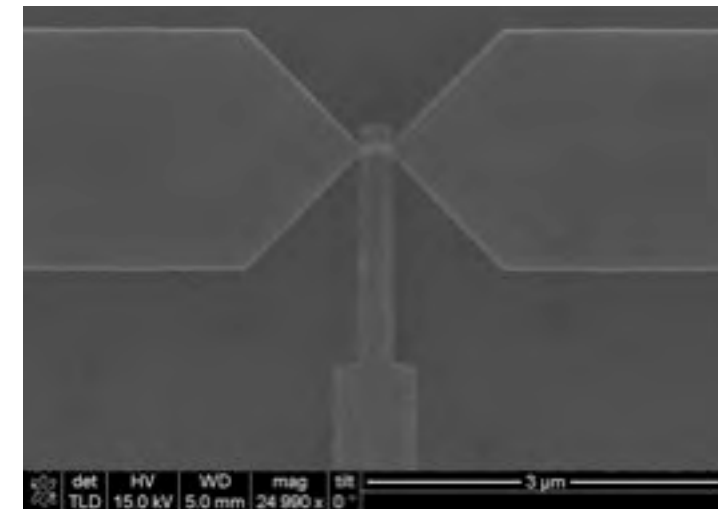
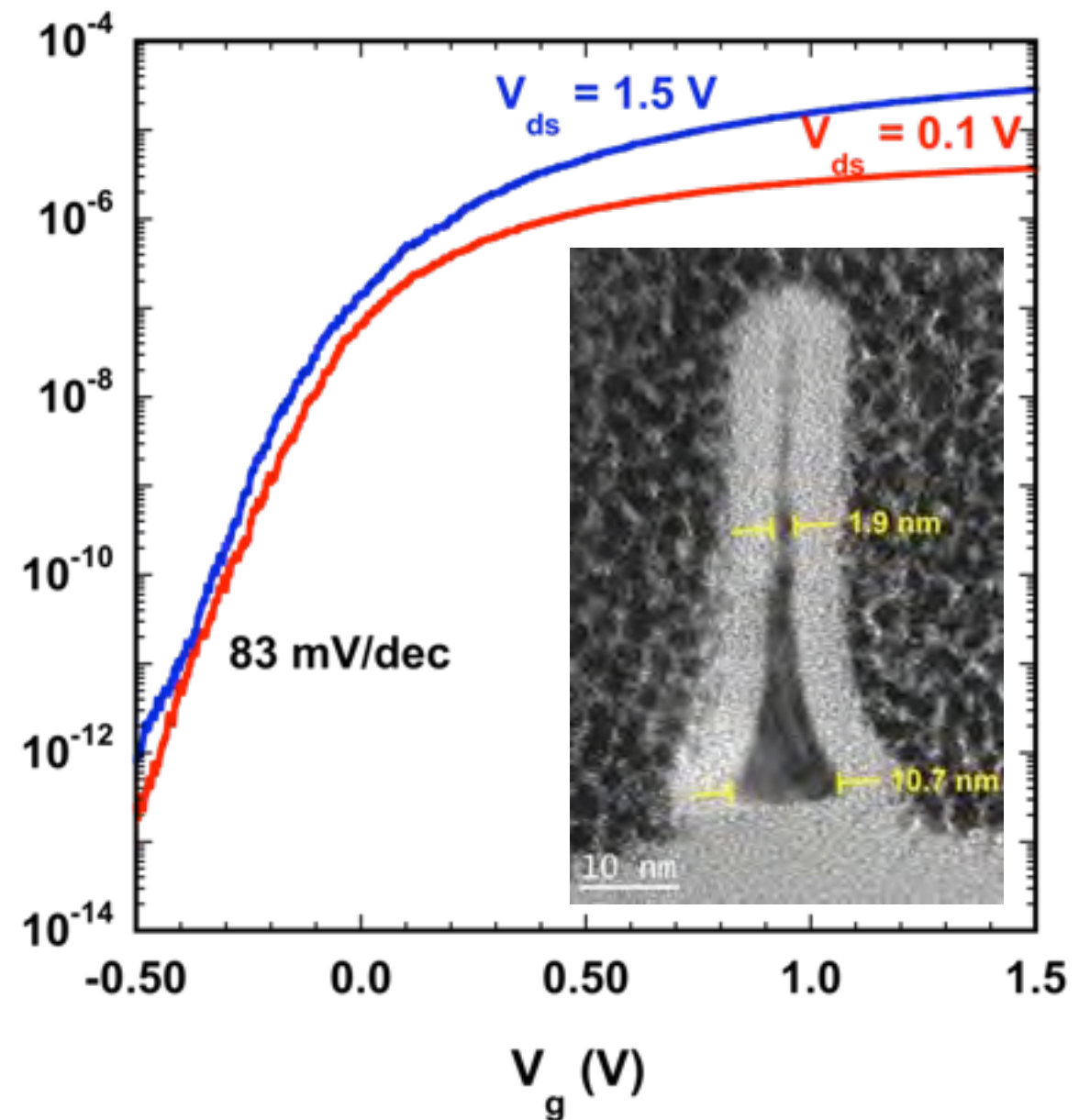
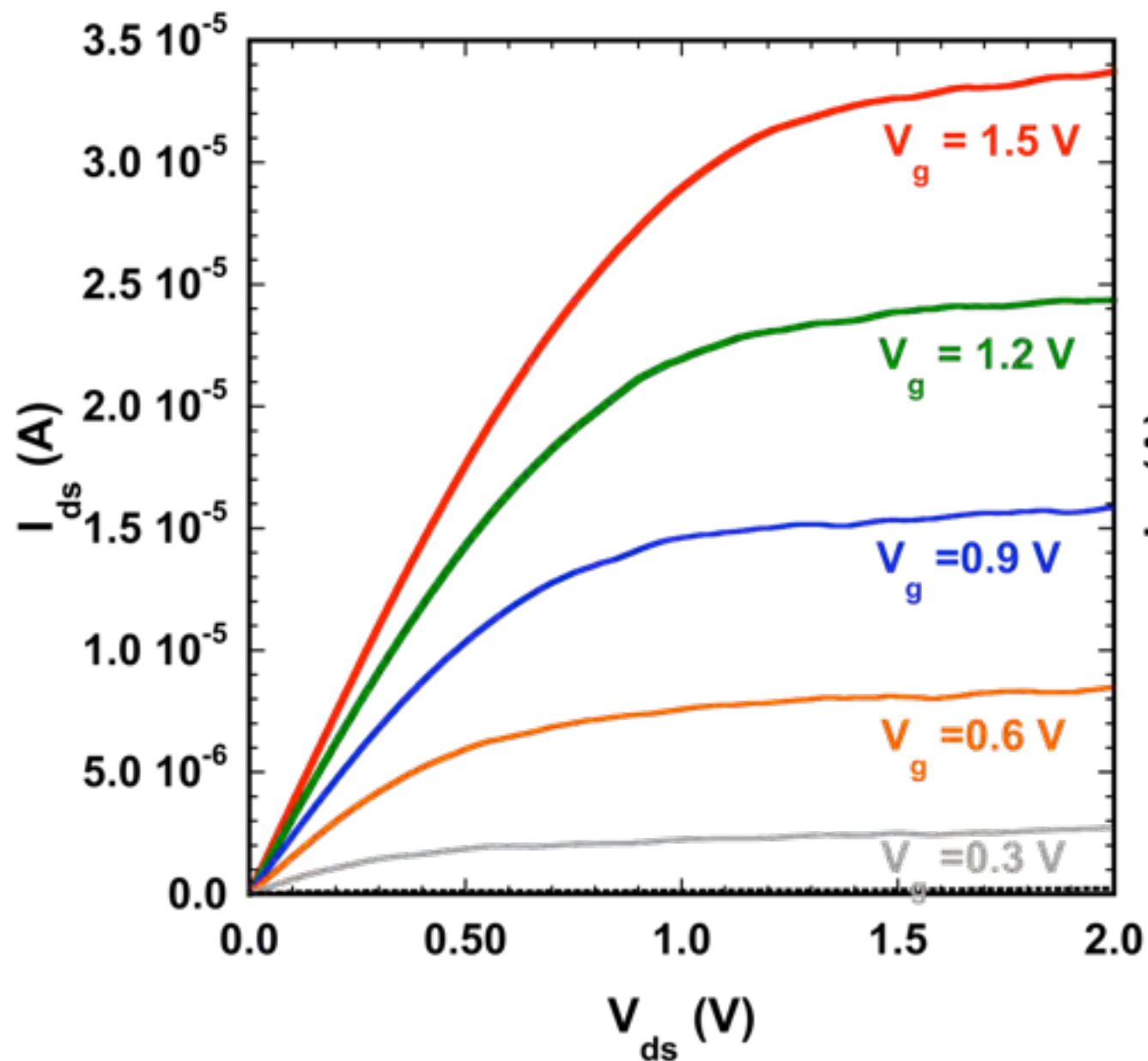
Vistec EBPG5

**Alignment allows 1 nm gaps
between different layers:**

**→ nanoscience: single
molecule metrology**

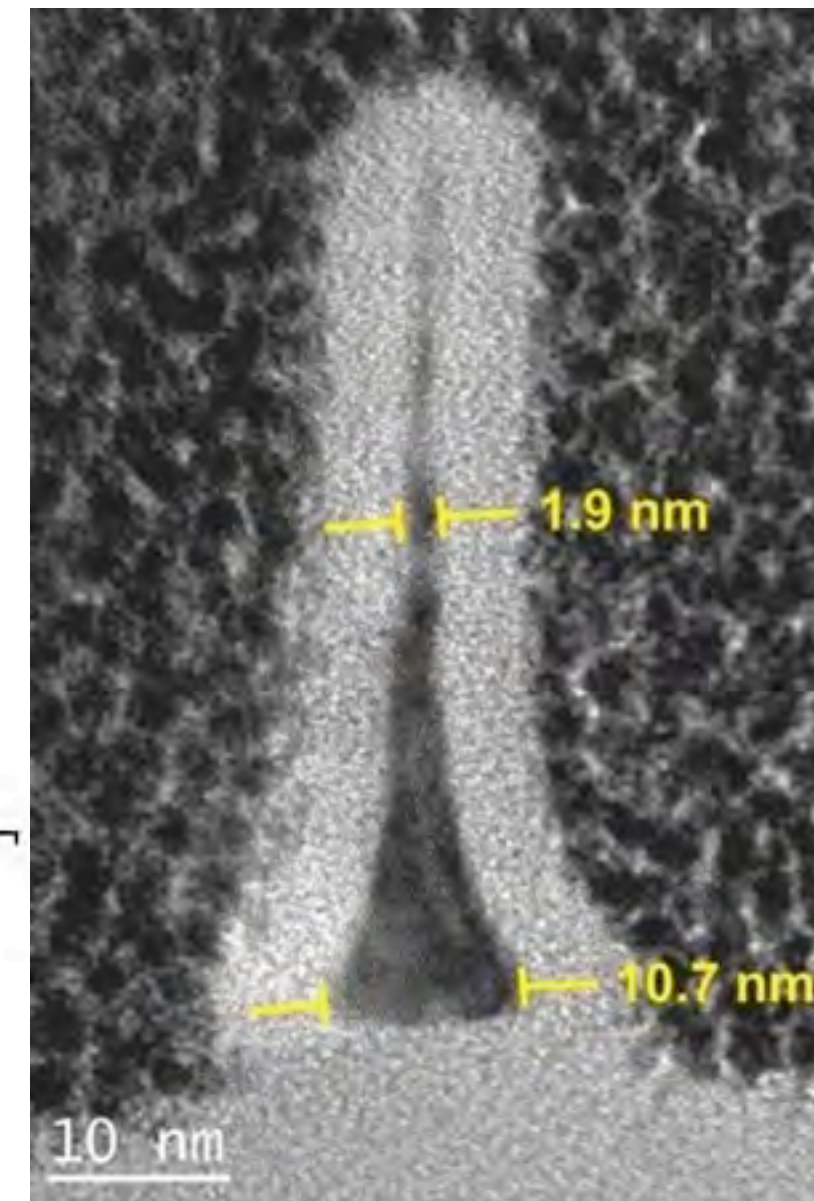
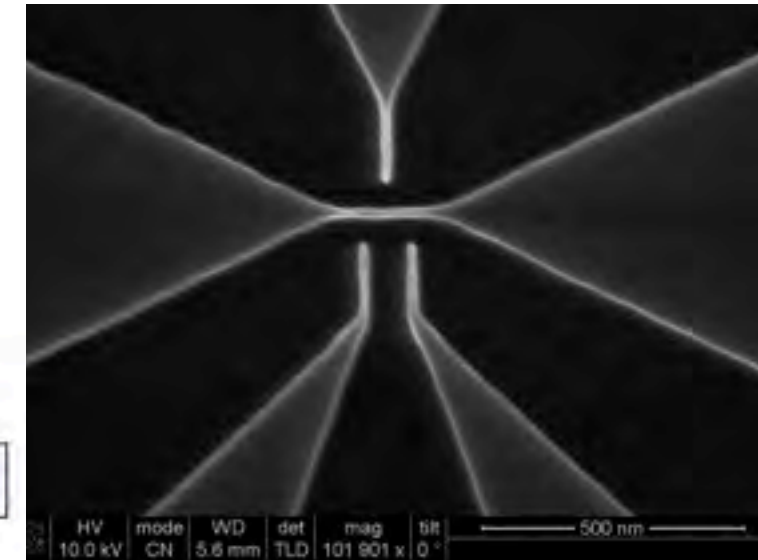
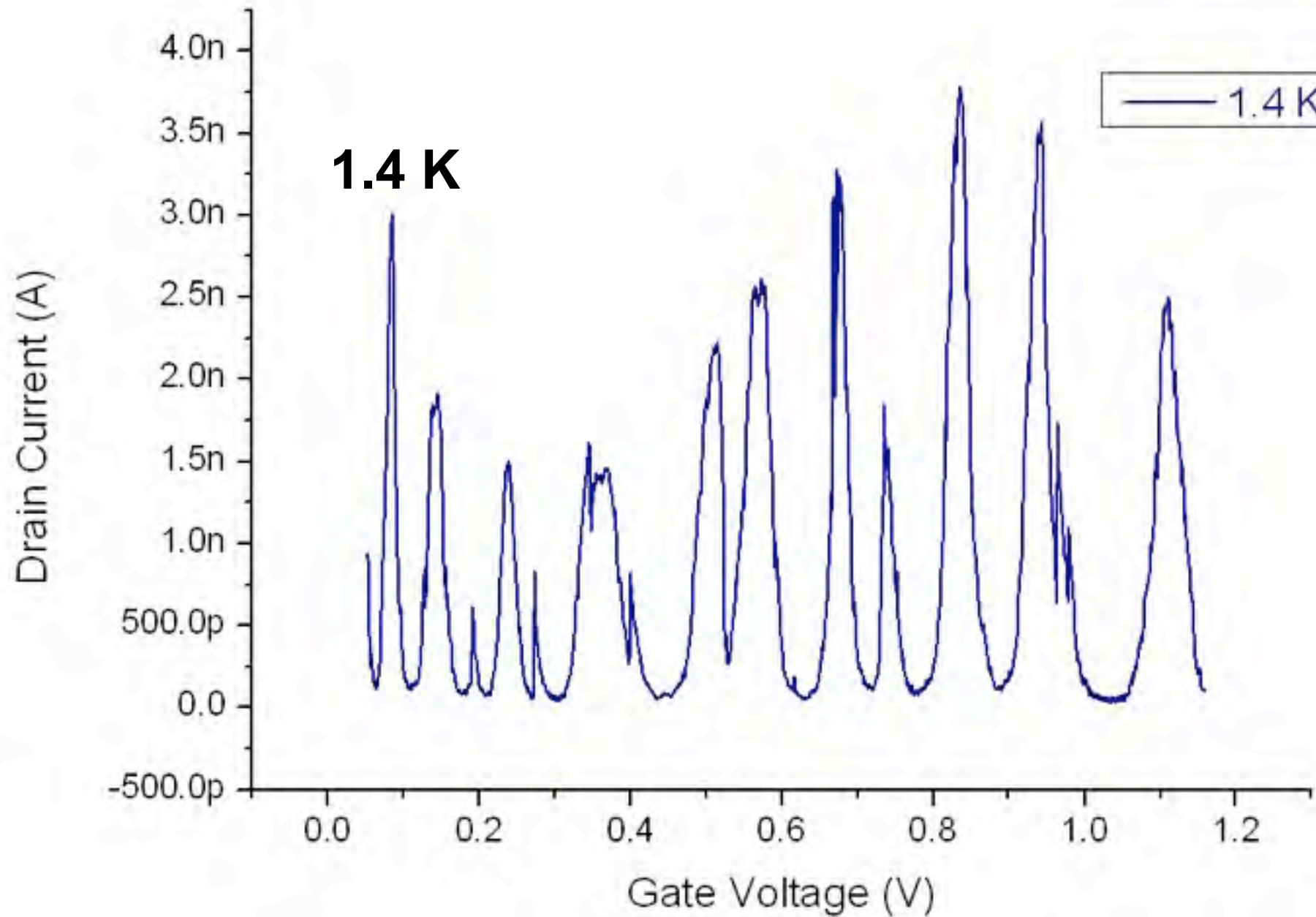


200 nm gate length
10 nm wide, 50 nm tall nanowire

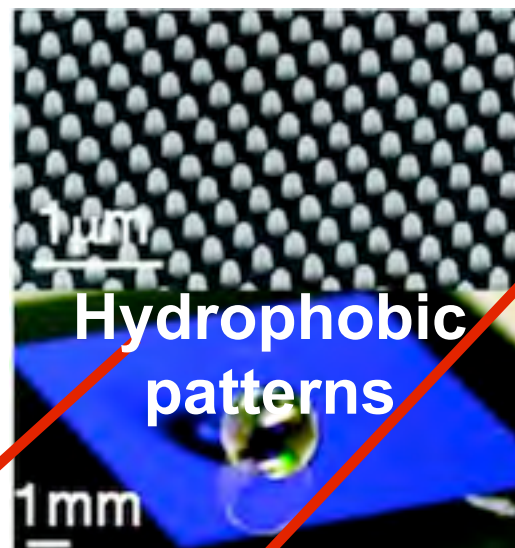
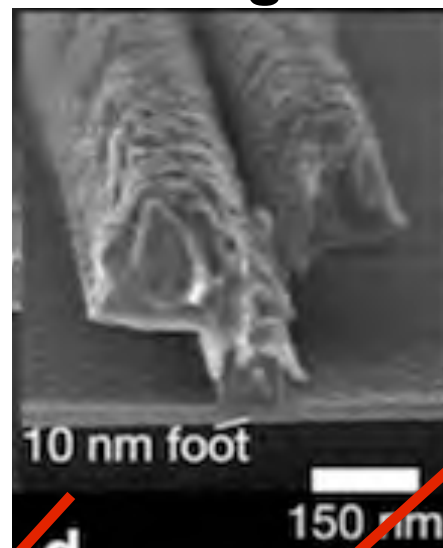
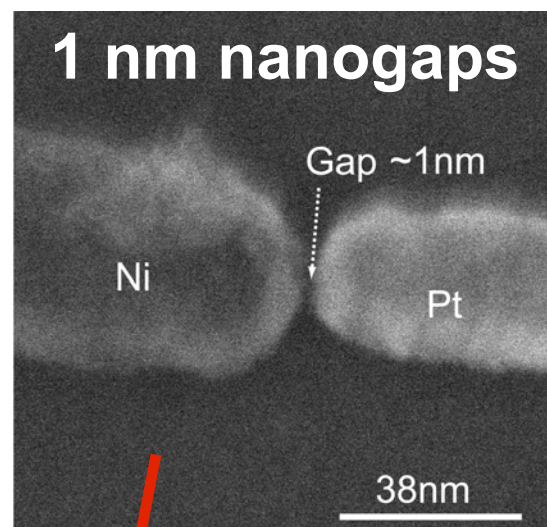




Depletion mode nanowire



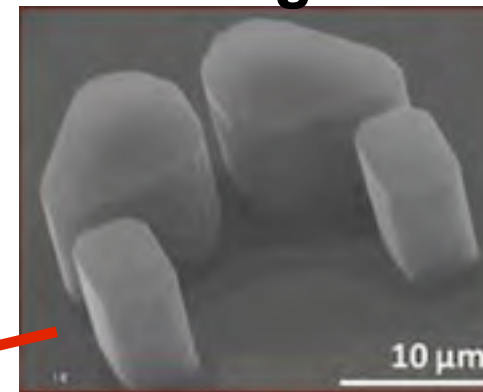
Nanoelectronics: 10 nm T-gate HEMT



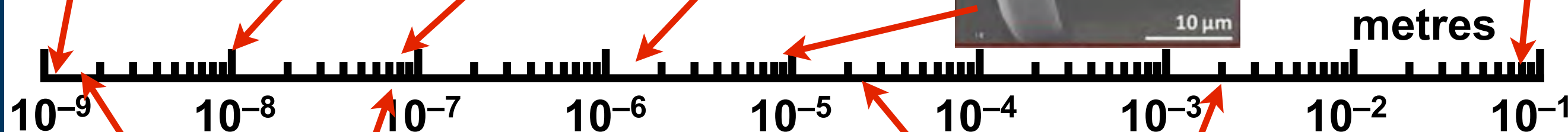
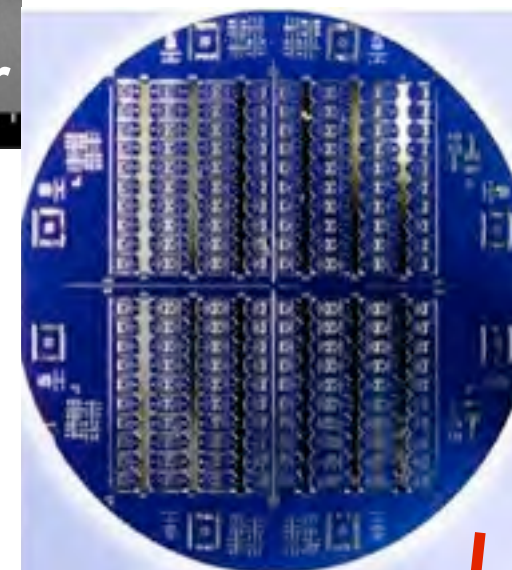
Optoelectronics: 1.55 μm DFB laser



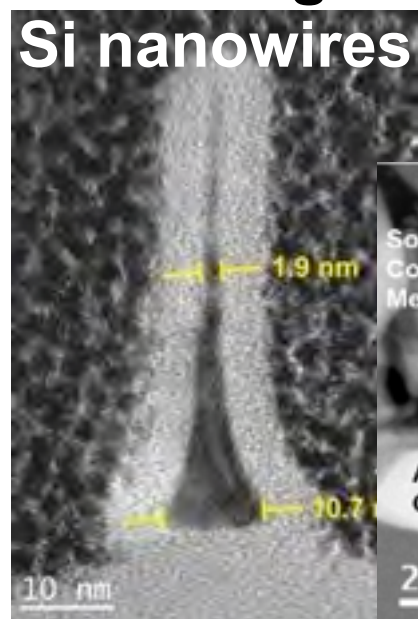
Healthcare: STEM cell interrogation



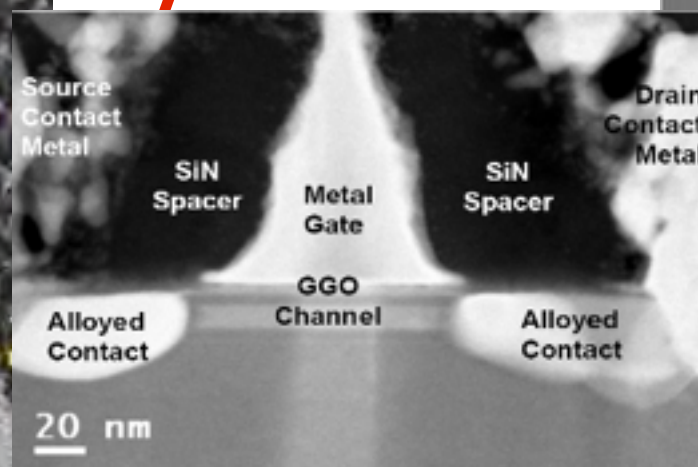
Manufacture: AFM probes



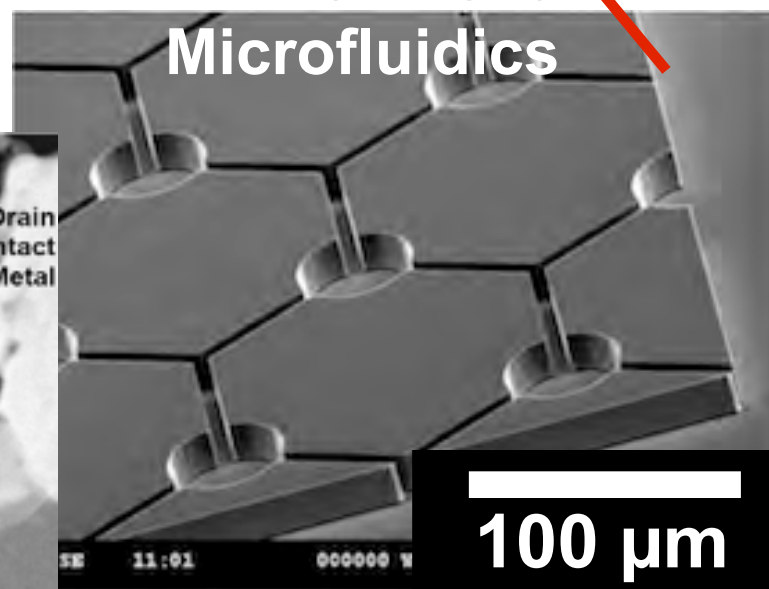
Sensing: Si nanowires



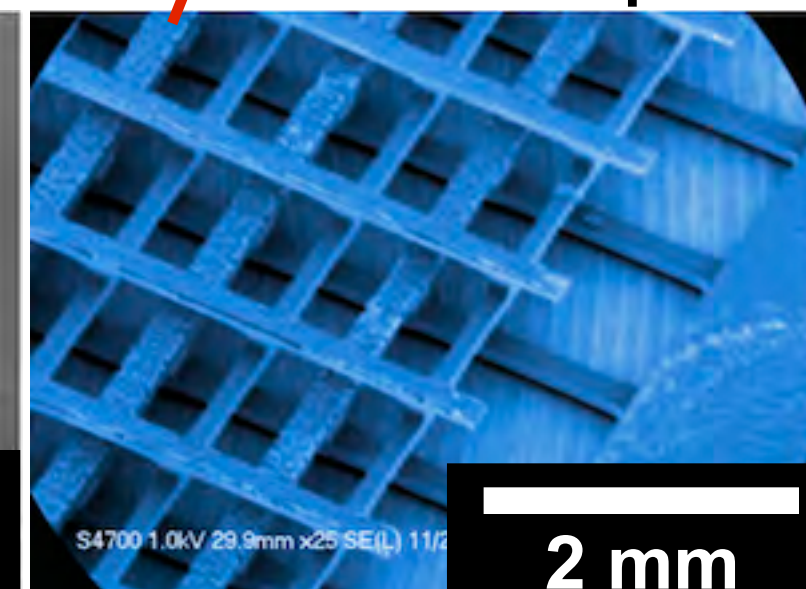
III-V CMOS



Environment: Microfluidics



MEMS: THz optics



- **History: Seebeck effect 1822**

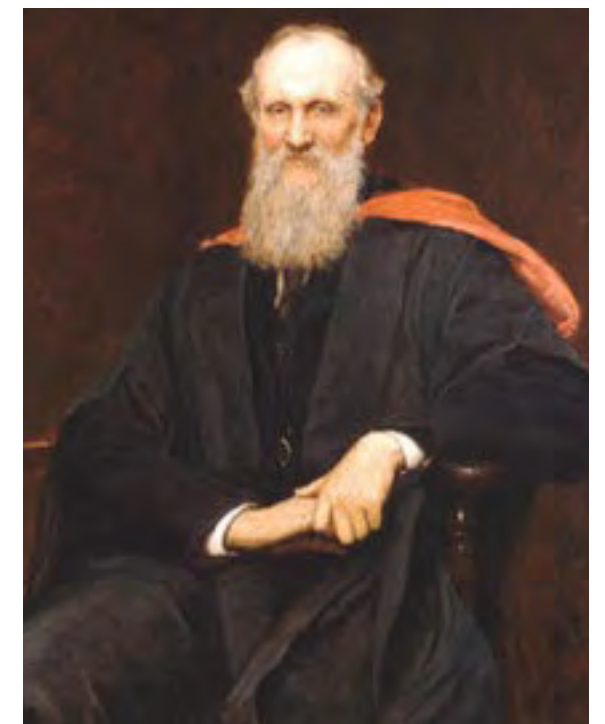


heat → electric current

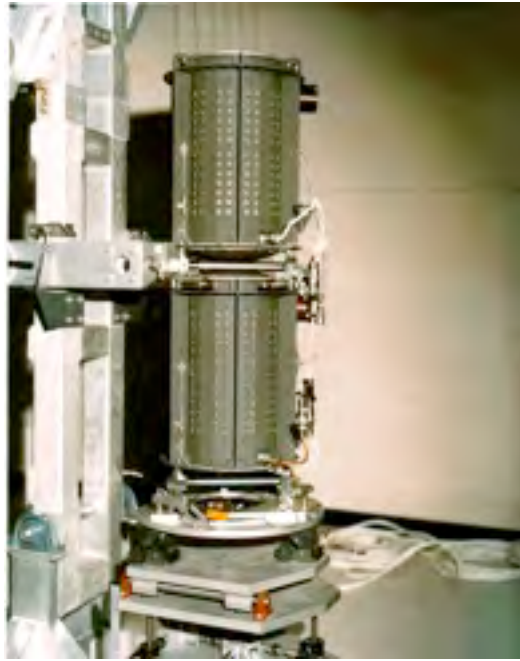


- **Peltier (1834): current → cooling**

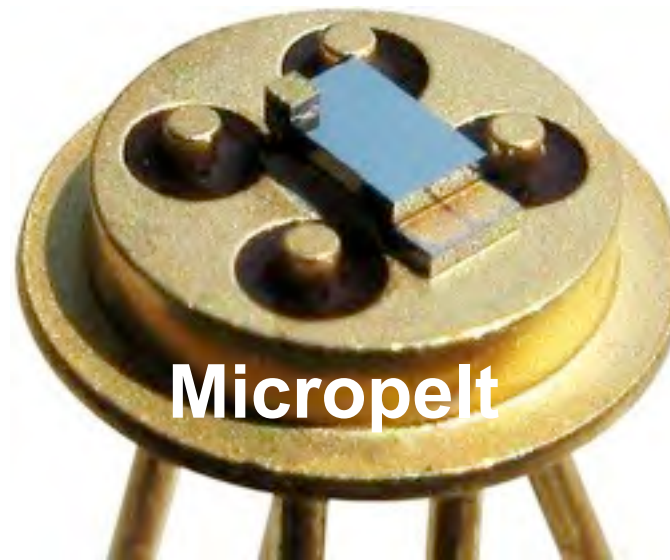
- **Thomson effect: Thomson (Lord Kelvin) 1852**



NASA Voyager I & II



Peltier cooler: telecoms lasers



Cars: replace alternator

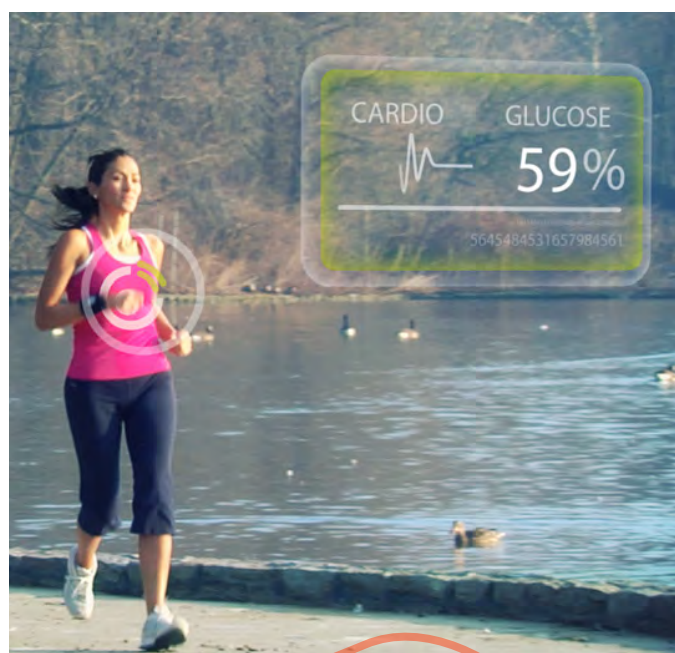


Temperature control for CO₂ sequestration



Buildings / industry temperature control – autonomous sensing

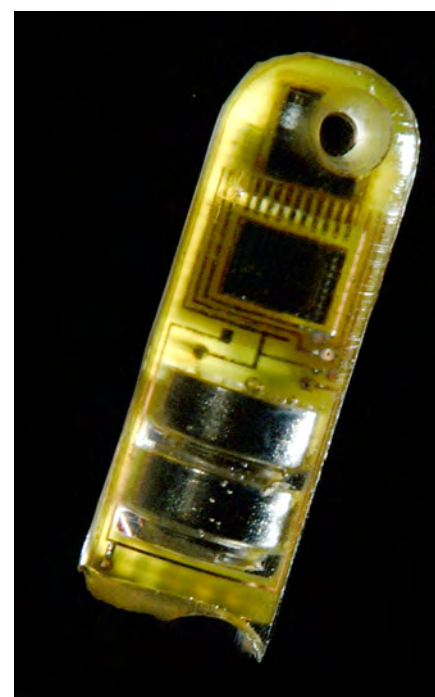
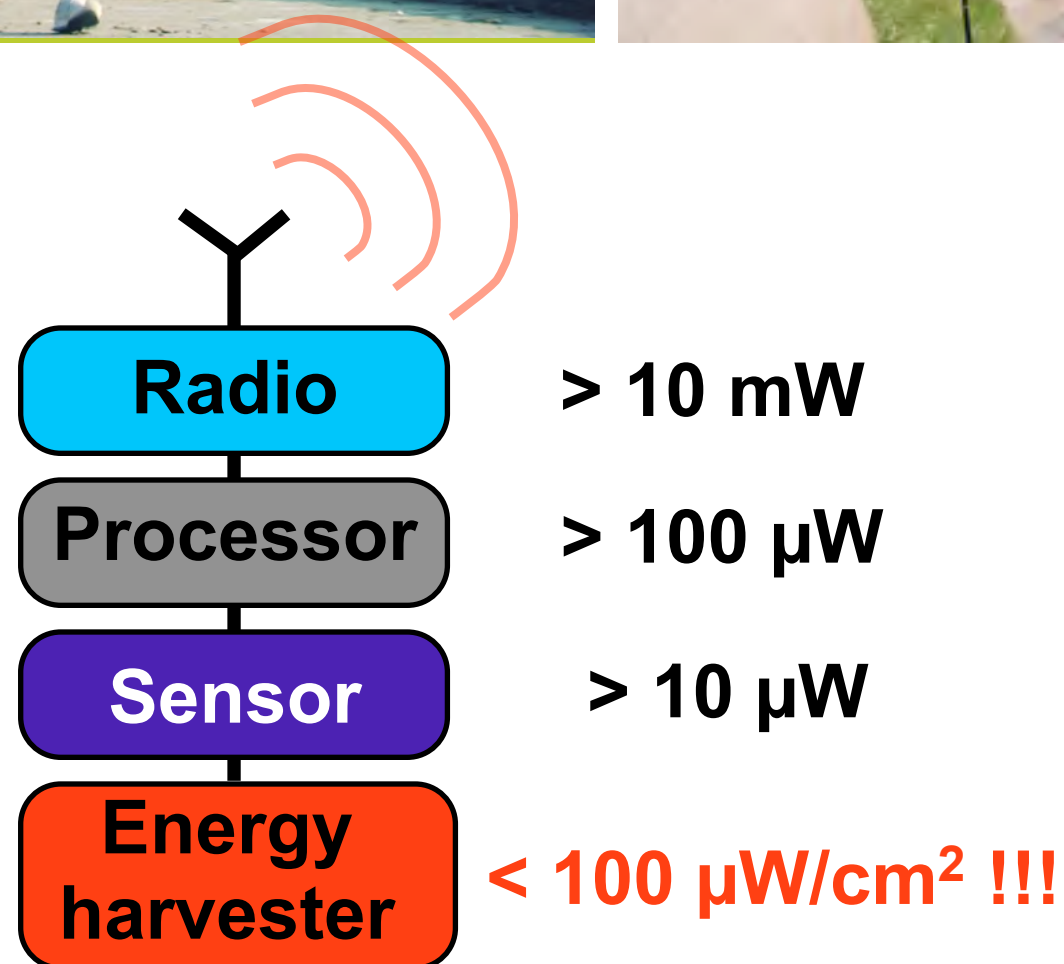
Sports performance sensors



Flood sensors



Weather monitoring



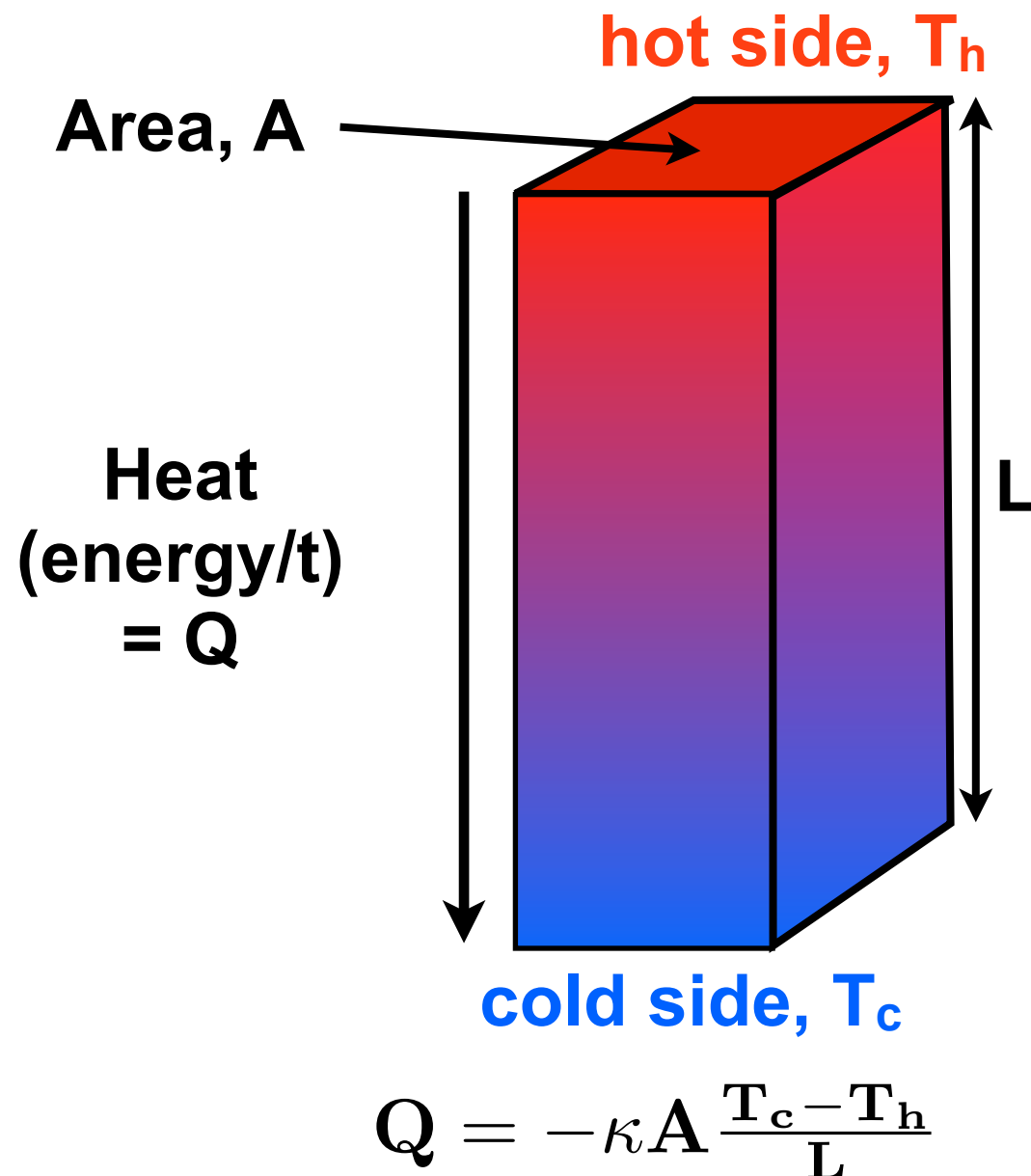
Aged well being sensors



Battery free autonomous sensors: ECG, blood pressure, etc.

Fourier thermal transport

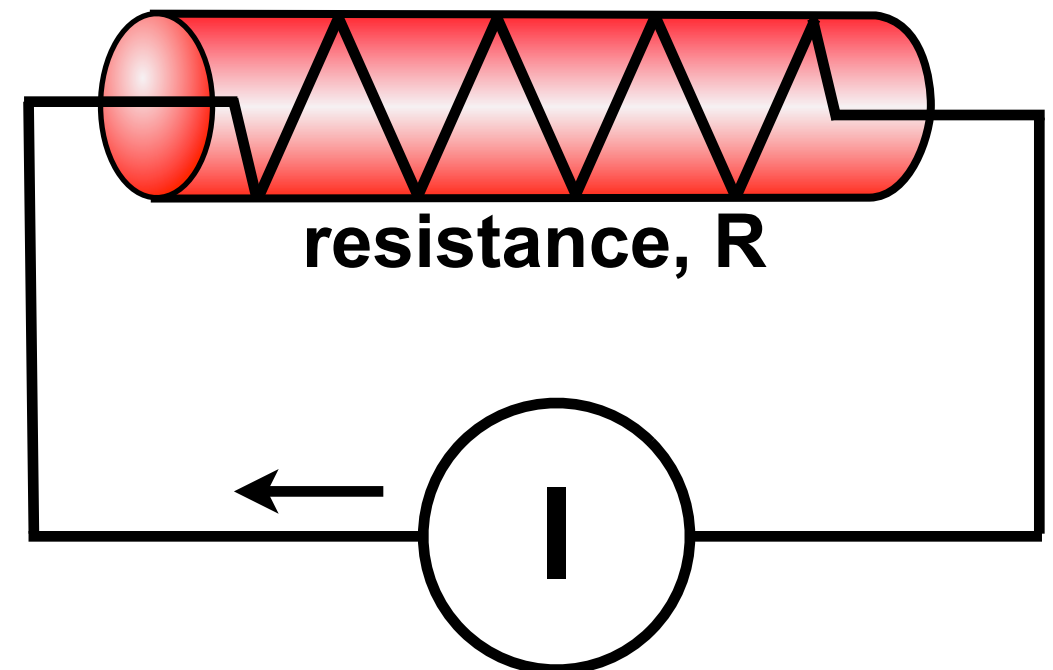
$$Q = -\kappa A \nabla T$$

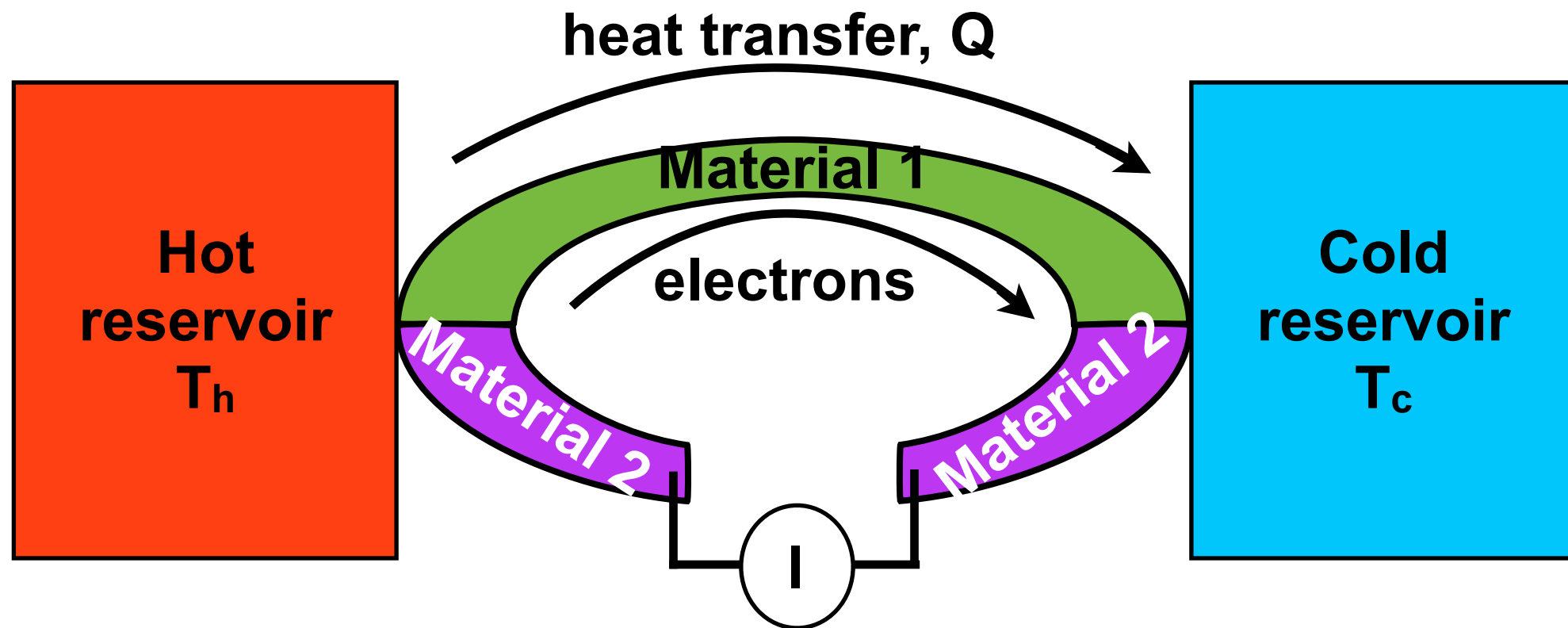


Joule heating

$$Q = I^2 R$$

$Q = \text{heat (power i.e energy / time)}$





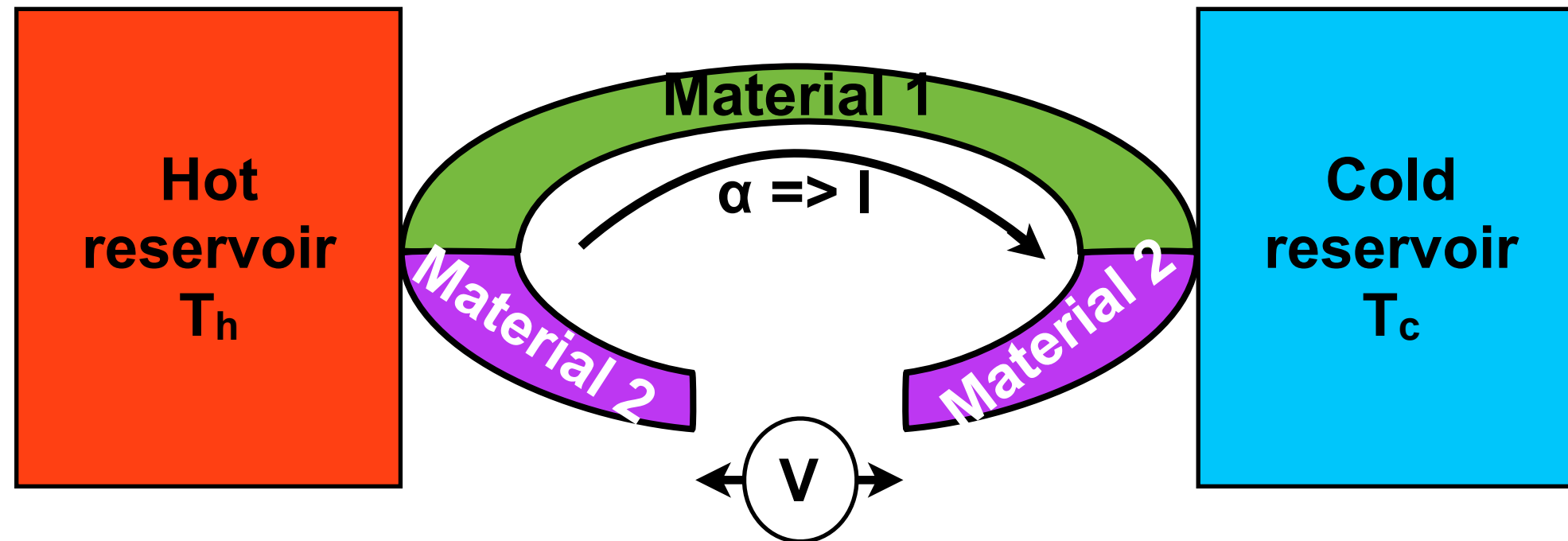
Peltier coefficient, $\Pi = \frac{Q}{I}$

units: $W/A = V$



Peltier coefficient is the heat energy carried by each electron per unit charge & time

The Seebeck Effect



- Open circuit voltage, $V = \alpha (T_h - T_c) = \alpha \Delta T$

Seebeck coefficient, $\alpha = \frac{dV}{dT}$

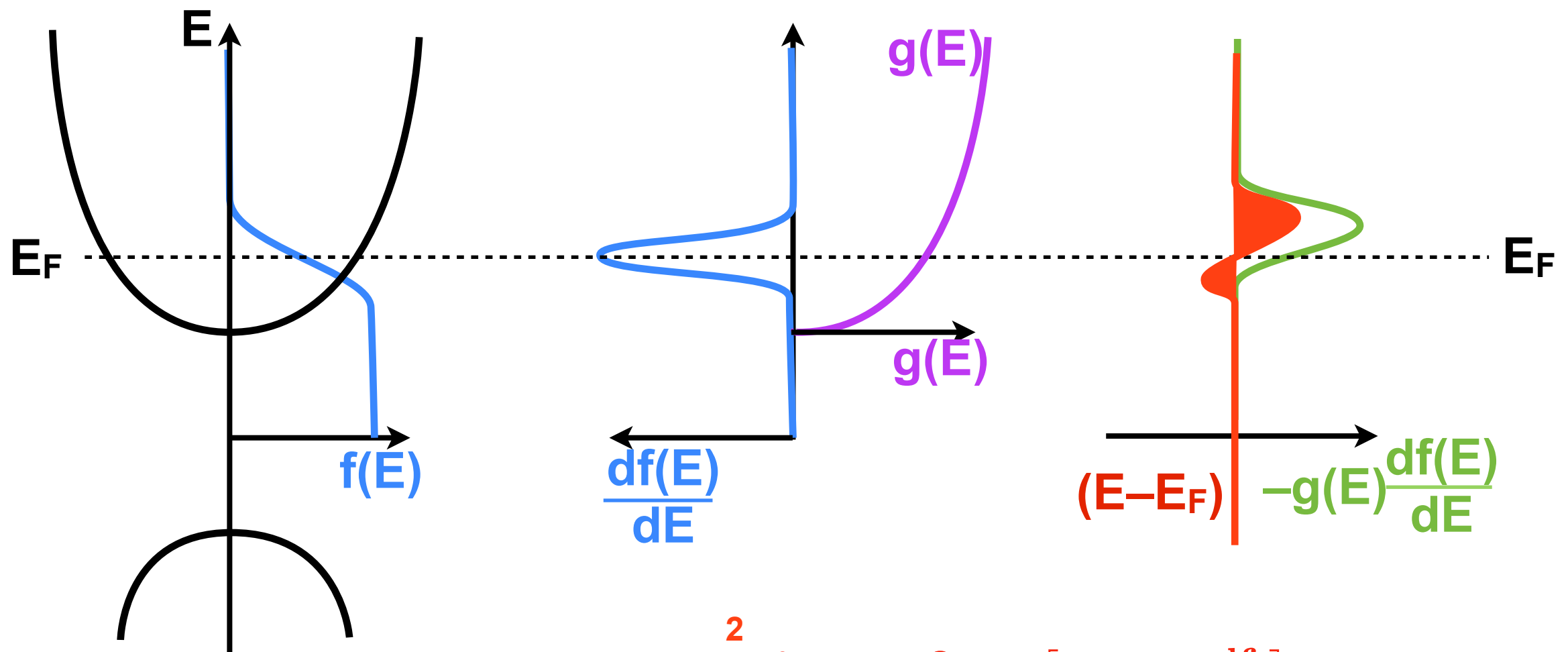
units: V/K

- Seebeck coefficient = $\frac{1}{q}$ x entropy $\left(\frac{Q}{T}\right)$ transported with electron



If we ignore energy dependent scattering (i.e. $\tau = \tau(E)$)
then from J.M. Ziman

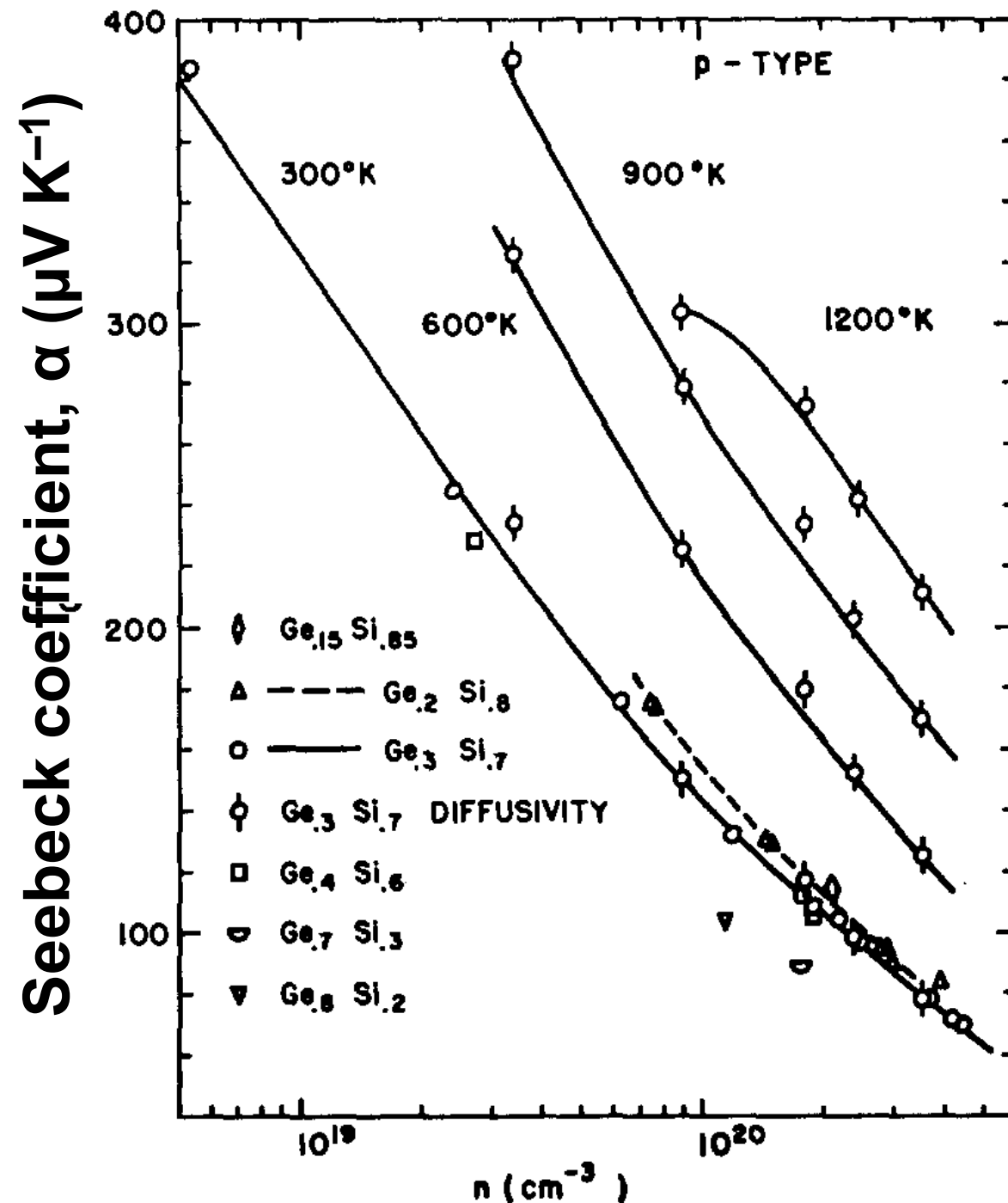
$$\sigma = \frac{q^2}{3} \int \tau(E) v^2(E) \left[-g(E) \frac{df}{dE} \right] dE$$



$$\alpha = \frac{q}{3T\sigma} \int \tau(E) v^2(E) \left[-g(E) \frac{df}{dE} \right] (E - E_F) dE$$



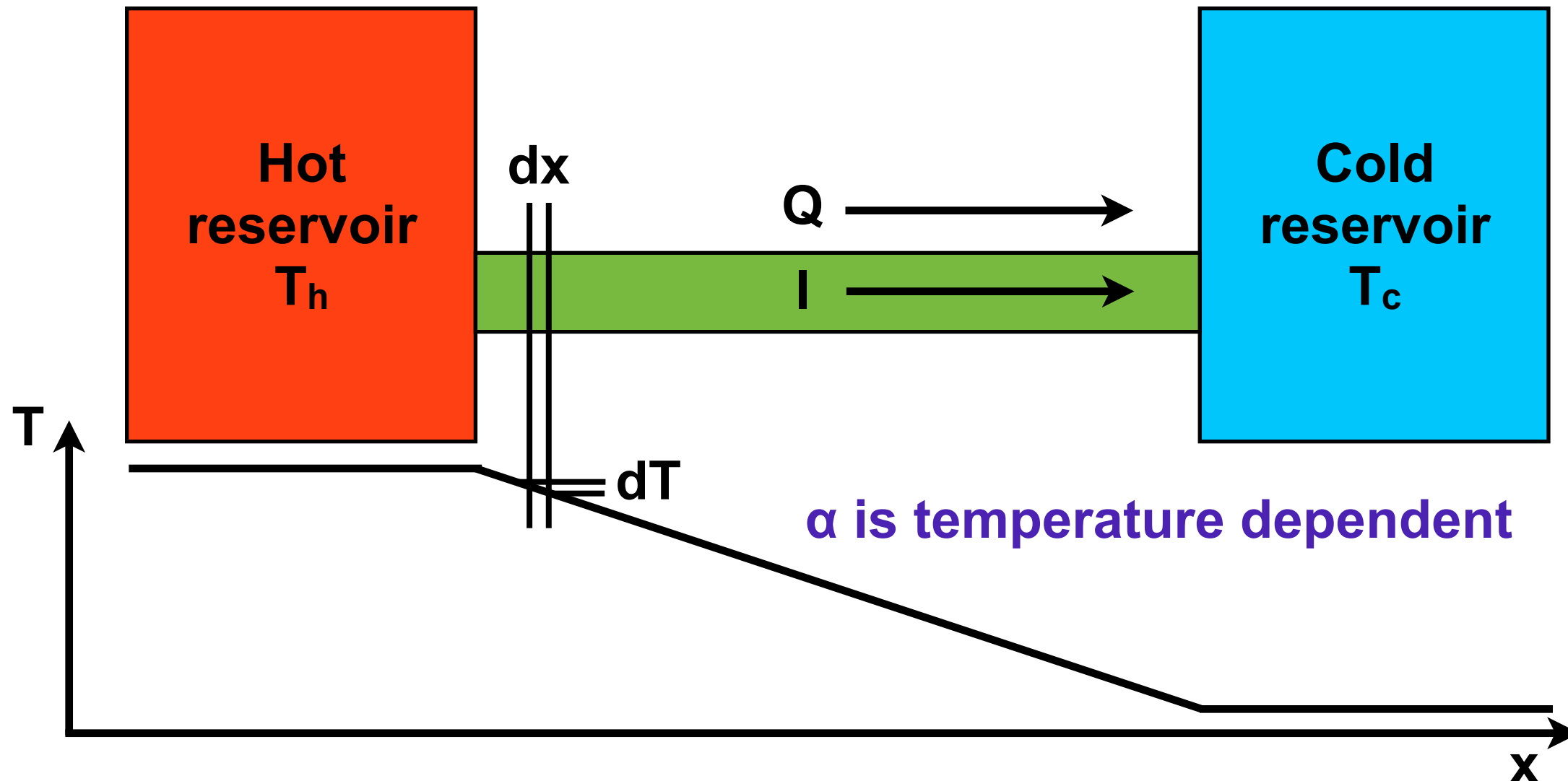
Thermoelectric power requires asymmetry in red area under curve



- Mott criteria $\sim 2 \times 10^{18} \text{ cm}^{-3}$
- Degenerately doped p- $\text{Si}_{0.7}\text{Ge}_{0.3}$
- α decreases for higher n
- For SiGe, α increases with T

$$\alpha = \frac{8\pi^2 k_B^2}{3eh^2} m^* T \left(\frac{\pi}{3n} \right)^{\frac{2}{3}}$$

The Thomson Effect



● $\frac{dQ}{dx} = \beta I \frac{dT}{dx}$

Thomson coefficient, β : $dQ = \beta I dT$

units: V/K

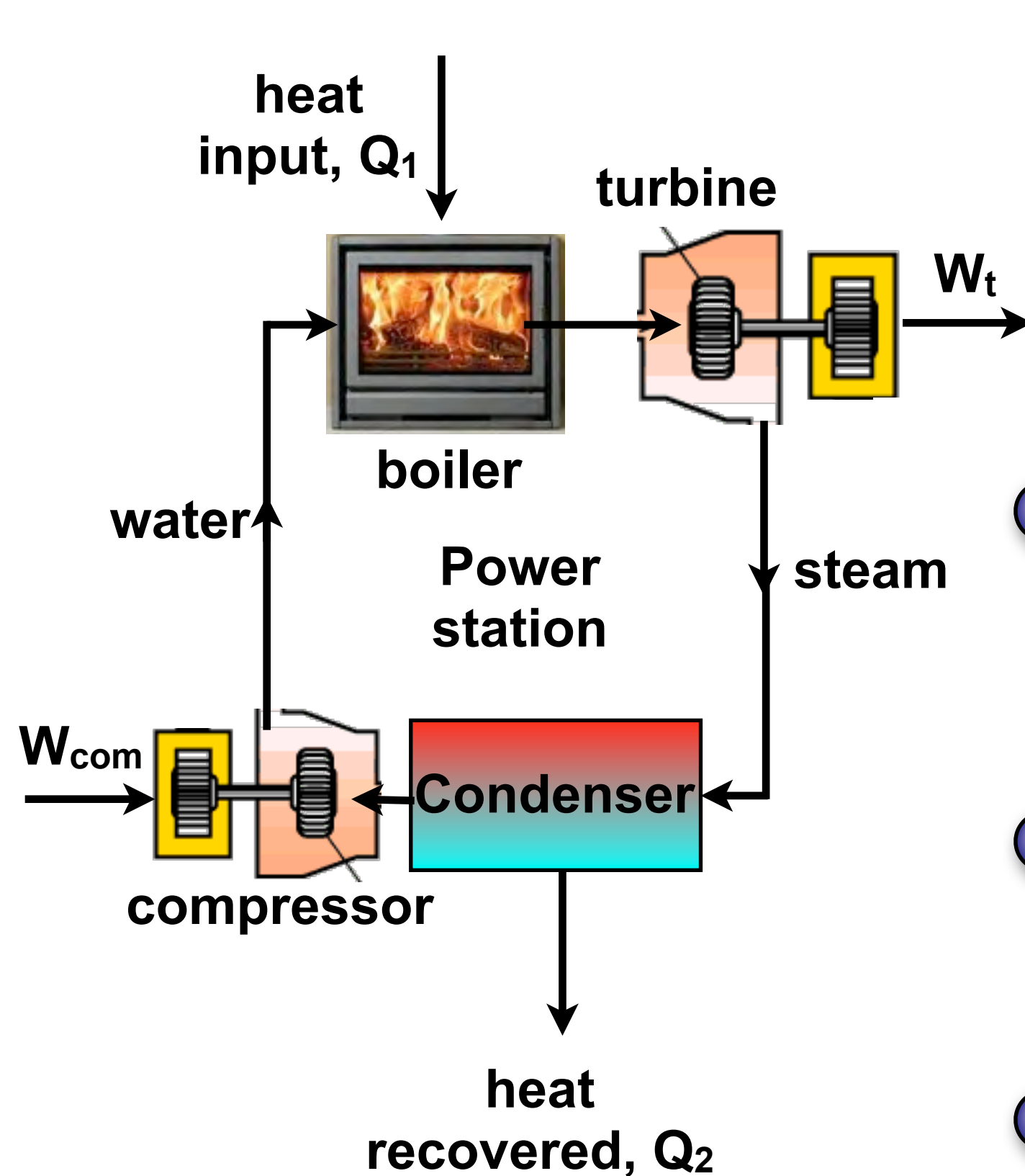
- Derived using irreversible thermodynamics

$$\Pi = \alpha T$$

$$\beta = T \frac{d\alpha}{dT}$$

- These relationships hold for all materials
- Seebeck, α is easy to measure experimentally
- Therefore measure α to obtain Π and β

Carnot Efficiency for Thermal Engines



$$\text{Efficiency} = \eta = \frac{\text{net work output}}{\text{heat input}}$$

$$= \frac{W_t - W_{com}}{Q_1}$$

● 1st law thermodynamics
 $(Q_1 - Q_2) - (W_t - W_{com}) = 0$

● $\eta = \frac{Q_1 - Q_2}{Q_1}$

● $\eta = 1 - \frac{Q_2}{Q_1}$

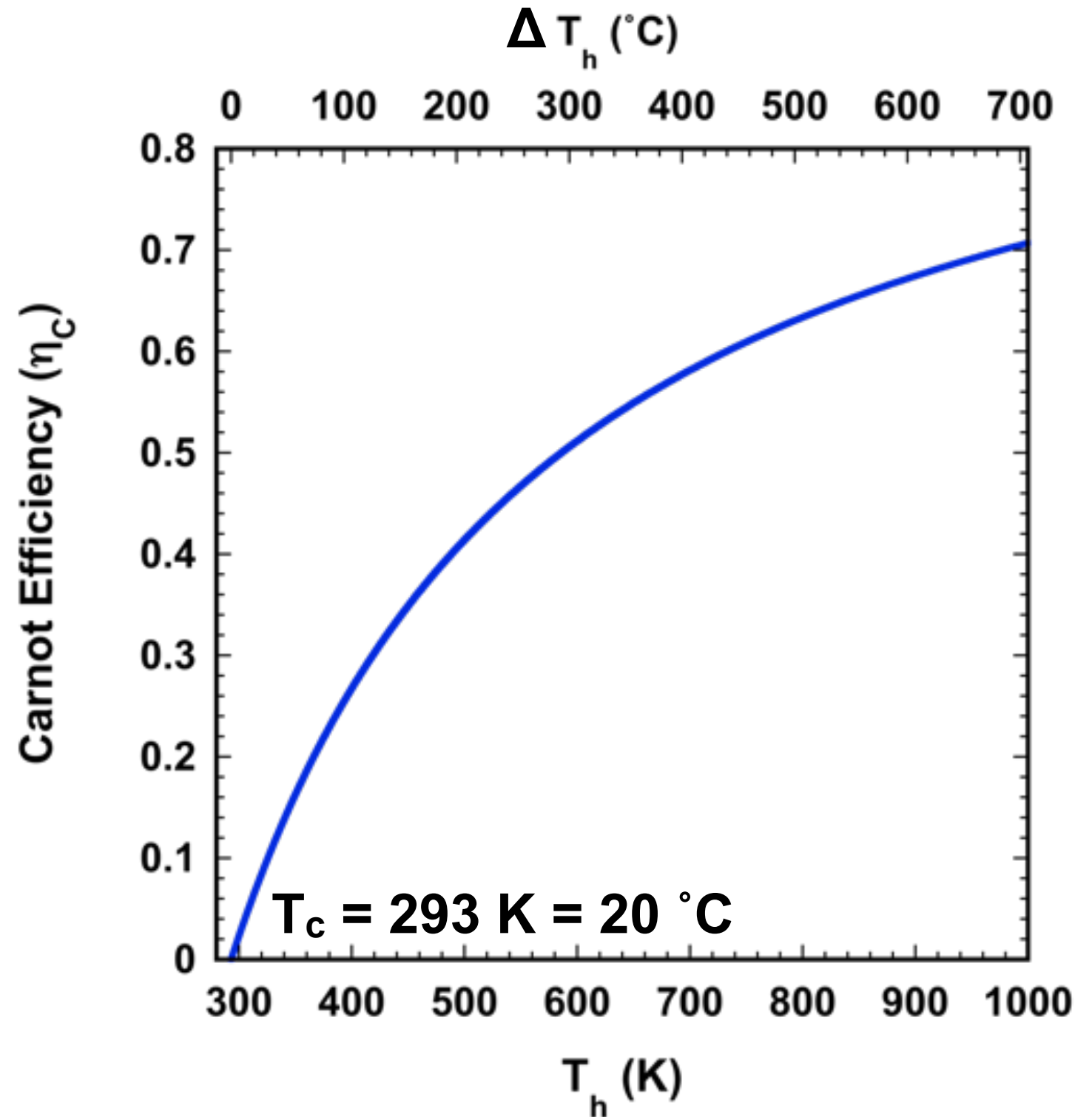
Efficiency =

$$\eta = \frac{\text{net work output}}{\text{heat input}}$$

$$\eta = 1 - \frac{Q_2}{Q_1}$$

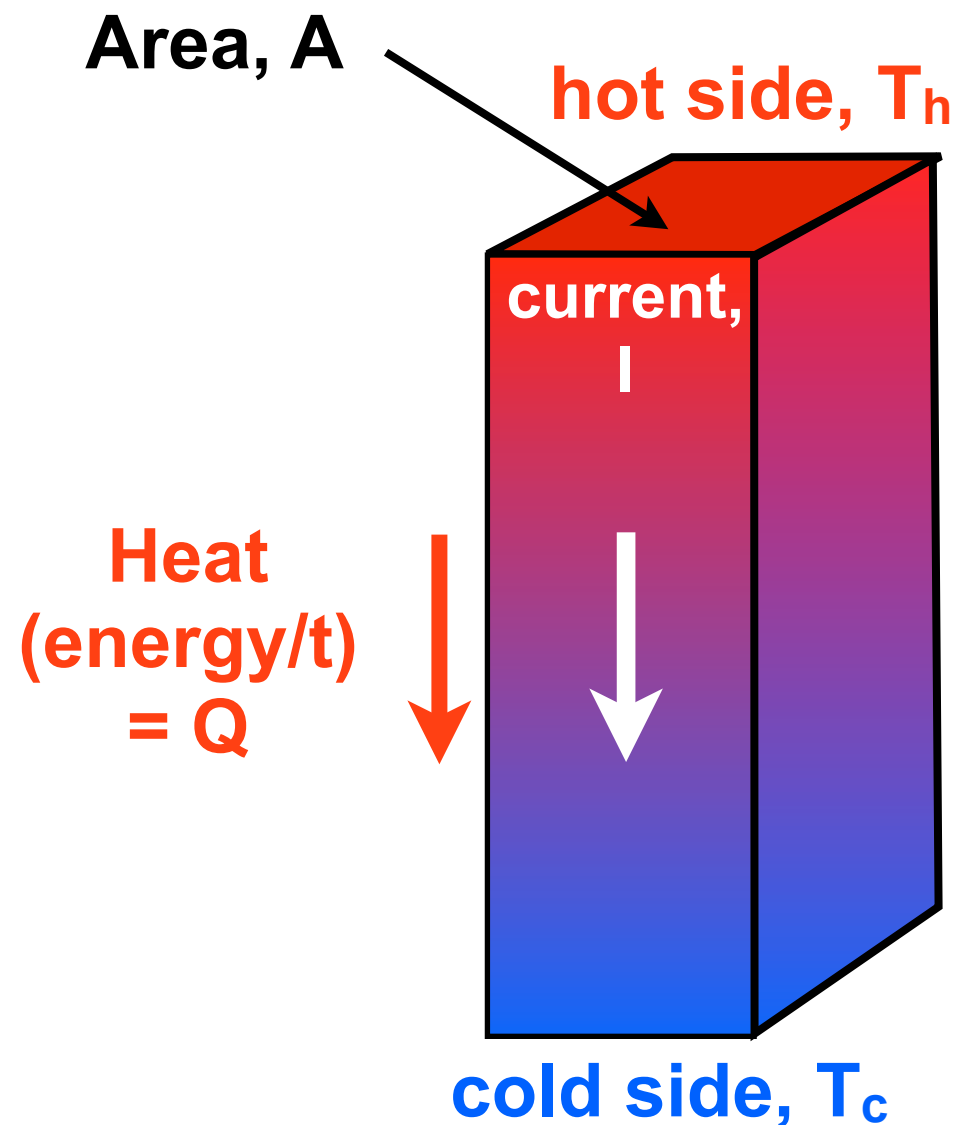
Carnot: maximum η only
depends on T_c and T_h

$$\eta_c = 1 - \frac{T_c}{T_h}$$



Higher temperatures give higher efficiencies

- If a current of I flows through a thermoelectric material between hot and cold reservoirs:



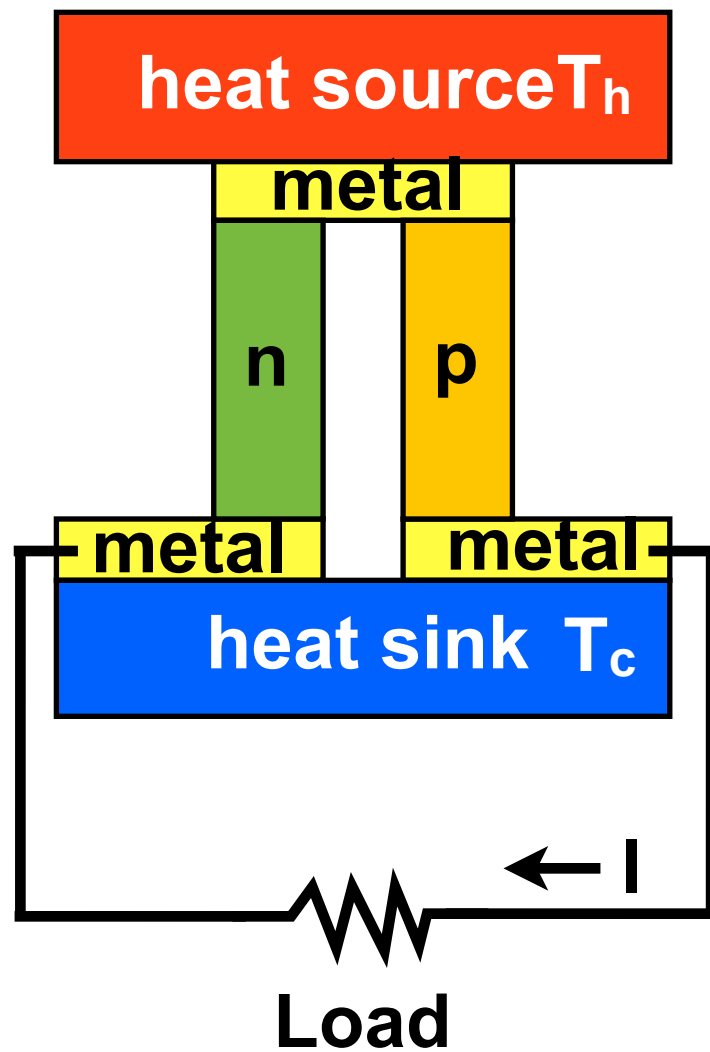
- Heat flux per unit area =
(= Peltier + Fourier)

- $$\frac{Q}{A} = \Pi J - \kappa \nabla T$$

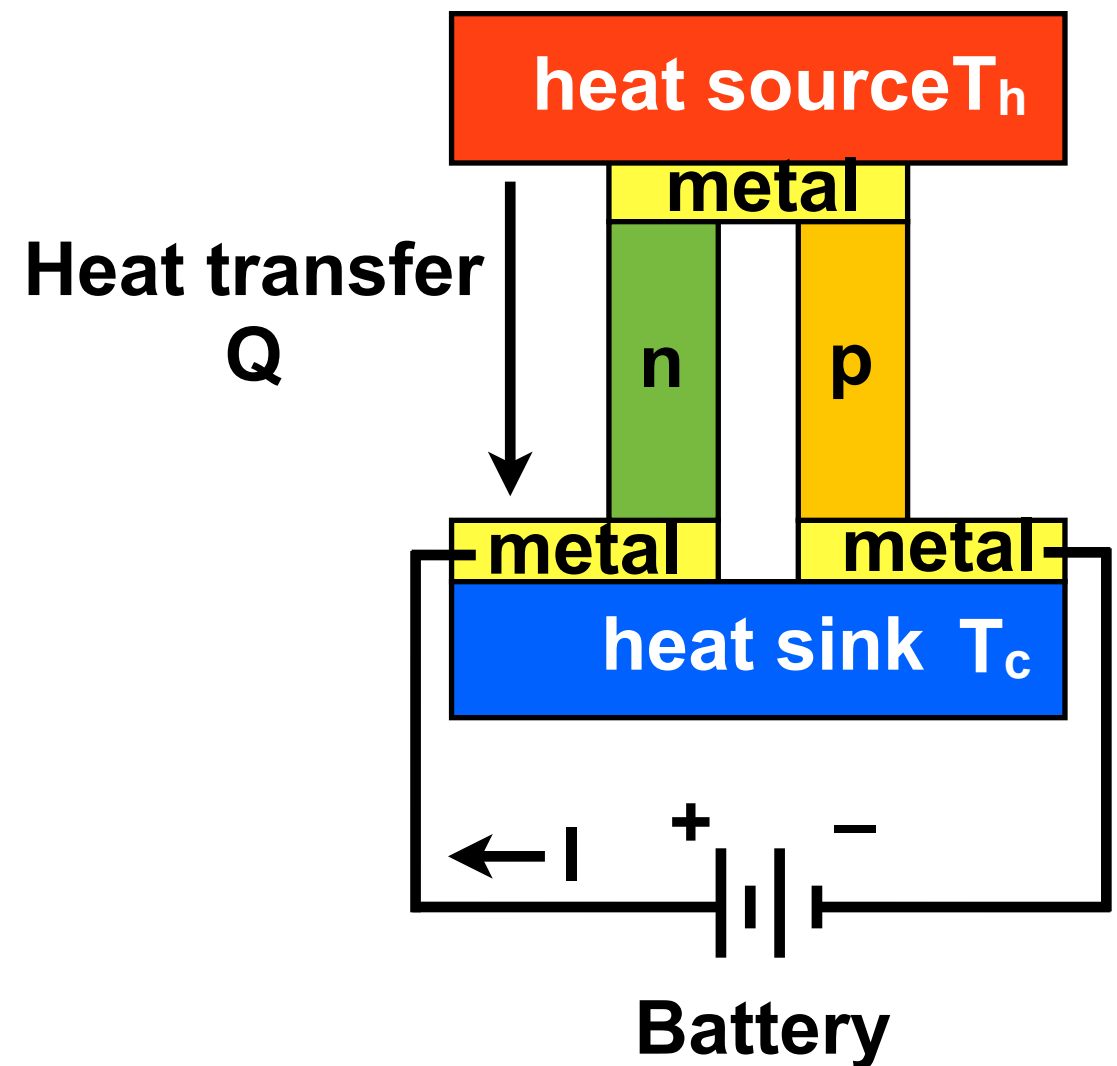
but $\Pi = \alpha T$ and $J = \frac{I}{A}$

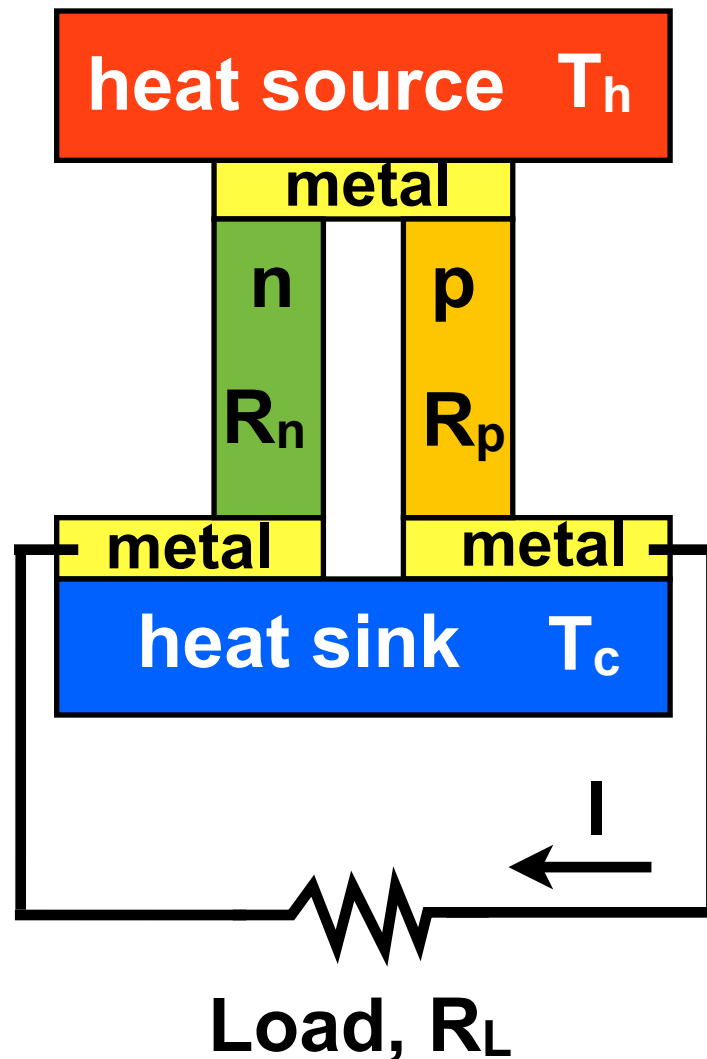
$$Q = \alpha IT - \kappa A \nabla T$$

**Seebeck effect:
electricity
generation**



**Peltier effect:
electrical cooling
i.e. heat pump**





$$R = R_n + R_p$$

- $\eta = \frac{\text{power supplied to load}}{\text{heat absorbed at hot junction}}$
- Power to load (Joule heating) = $I^2 R_L$
- Heat absorbed at hot junction = Peltier heat + heat withdrawn from hot junction
- Peltier heat = $\Pi I = \alpha I T_h$
- $I = \frac{\alpha(T_h - T_c)}{R + R_L}$ (Ohms Law)
- Heat withdrawn from hot junction

$$= \kappa A (T_h - T_c) - \frac{1}{2} I^2 R$$

↑

NB half Joule heat returned to hot junction

● $\eta = \frac{\text{power supplied to load}}{\text{heat absorbed at hot junction}}$

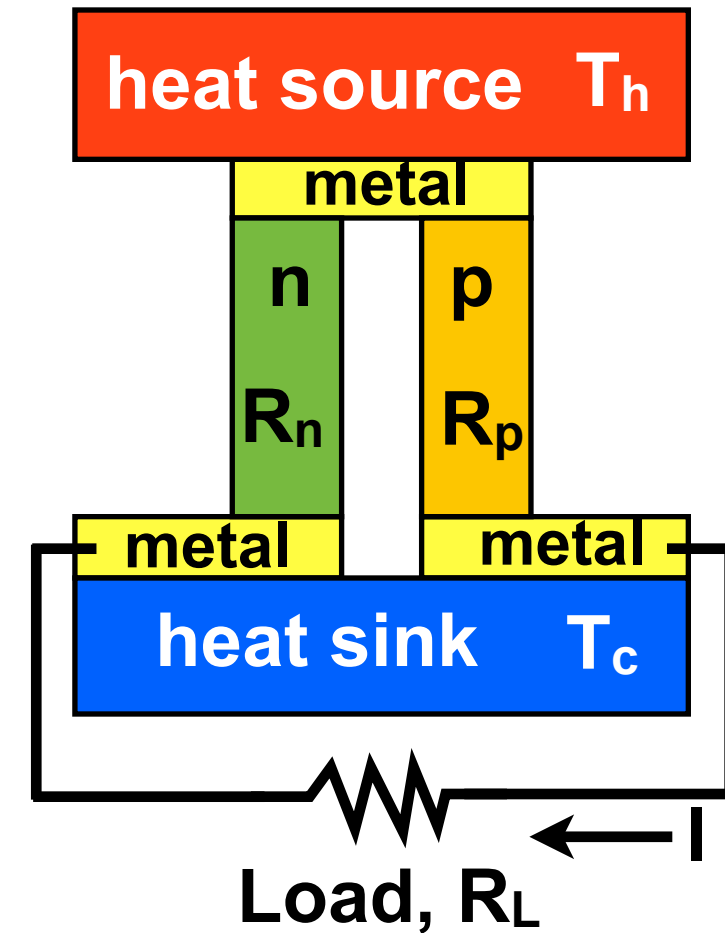
$= \frac{\text{power supplied to load}}{\text{Peltier} + \text{heat withdrawn}}$

$$\eta = \frac{I^2 R_L}{\alpha I T_h + \kappa A (T_h - T_c) - \frac{1}{2} I^2 R}$$

● For maximum value $\frac{d\eta}{d(\frac{R_L}{R})} = 0$

$$\eta_{\max} = \frac{T_h - T_c}{T_h} \frac{\sqrt{1 + ZT} - 1}{\sqrt{1 + ZT} + \frac{T_c}{T_h}}$$

= **Carnot** x **Joule losses and irreversible processes**

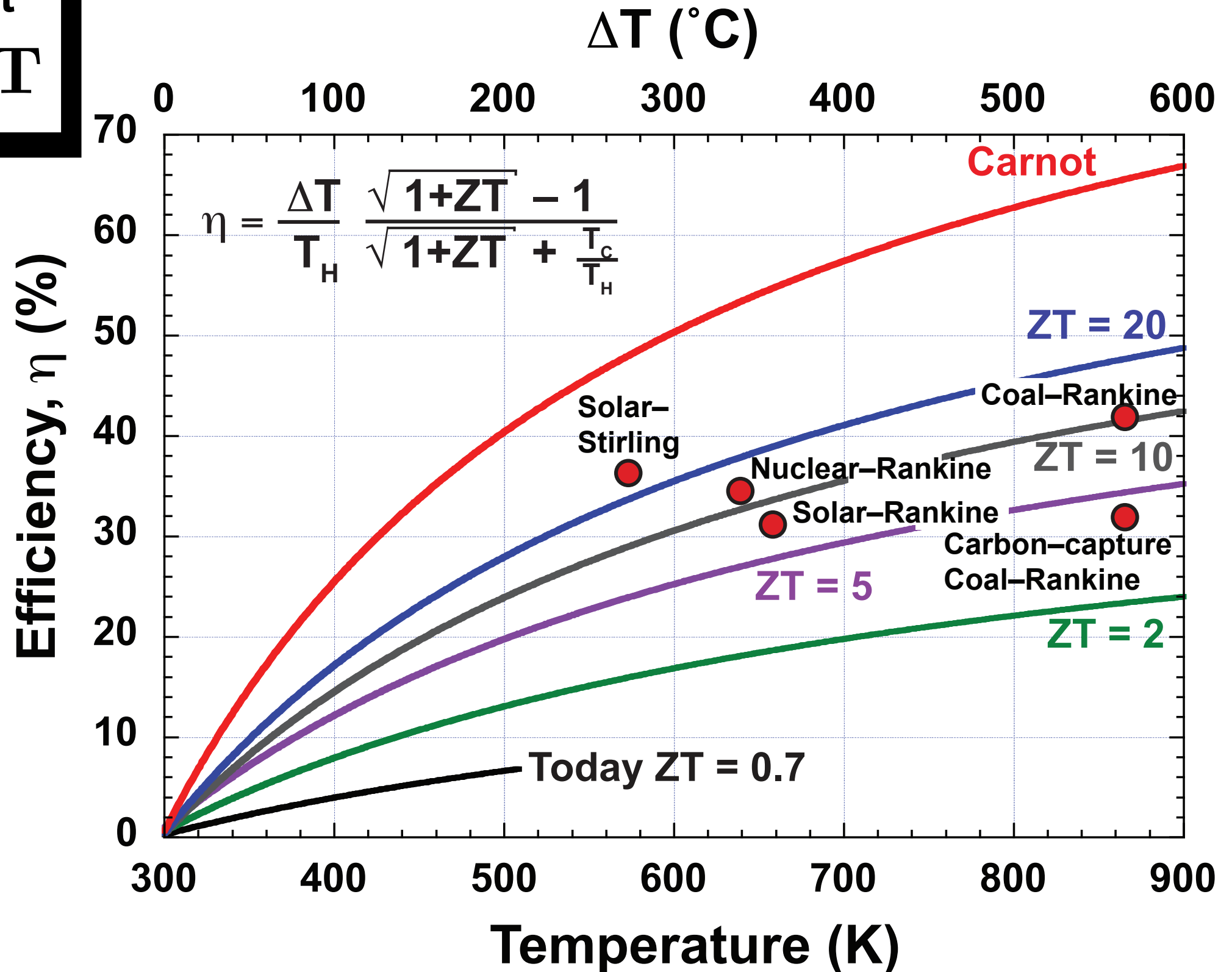


$$T = \frac{1}{2} (T_h + T_c)$$

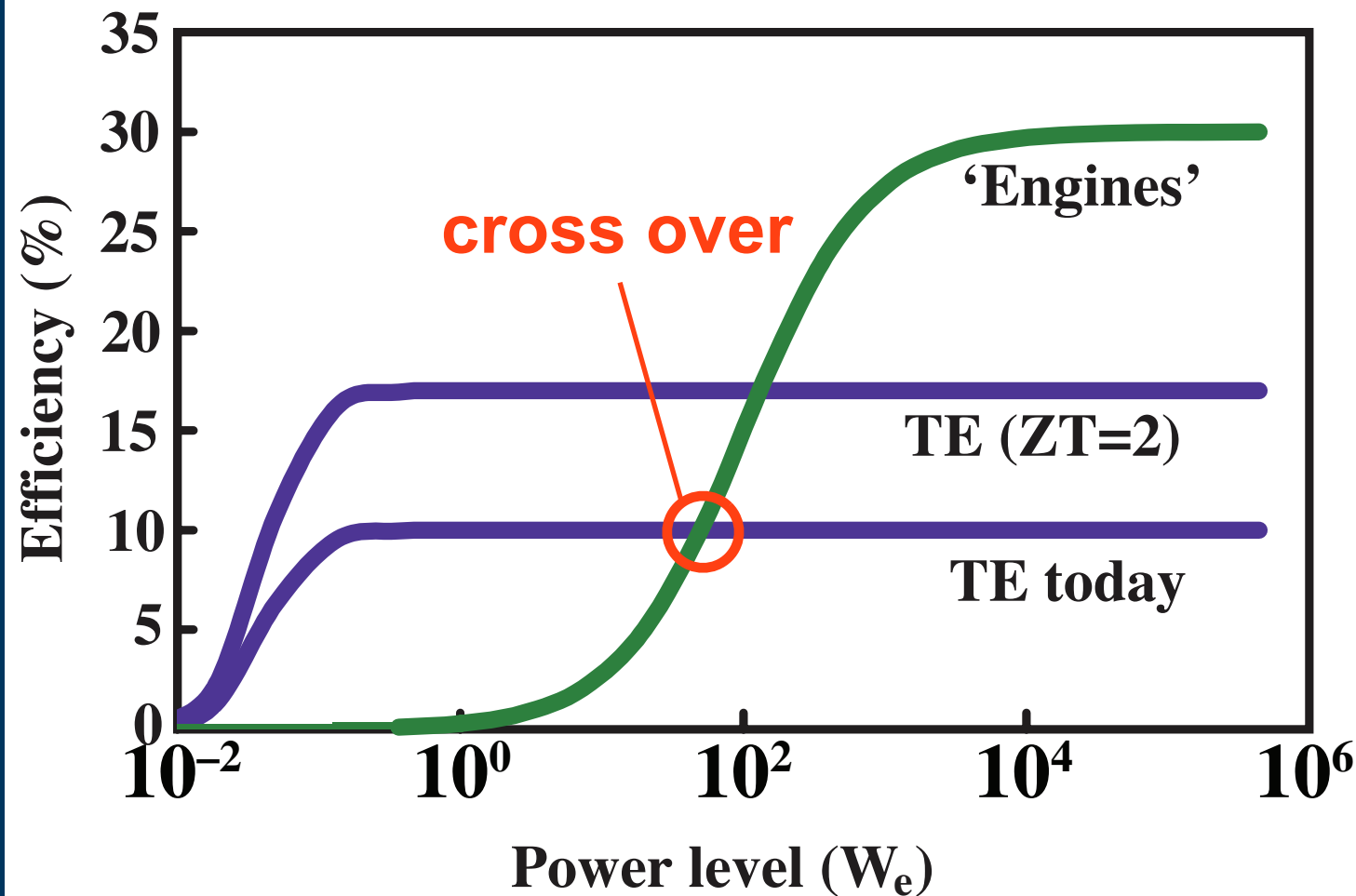
where $Z = \frac{\alpha^2}{R \kappa A} = \frac{\alpha^2 \sigma}{\kappa}$

Figure of merit

$$ZT = \frac{\alpha^2 \sigma}{\kappa} T$$



Illustrative schematic diagram



At large scale, thermodynamic engines more efficient than TE

ZT average for both n and p over all temperature range

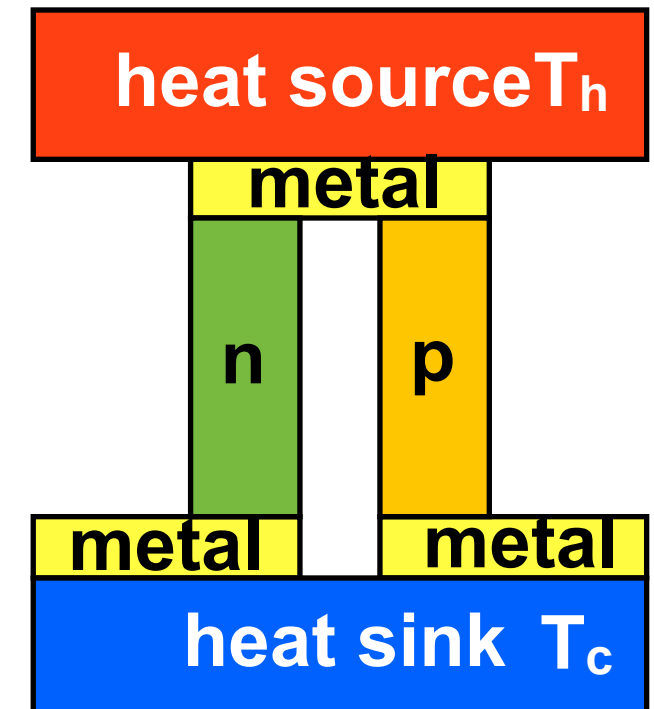
Diagram assumes high ΔT

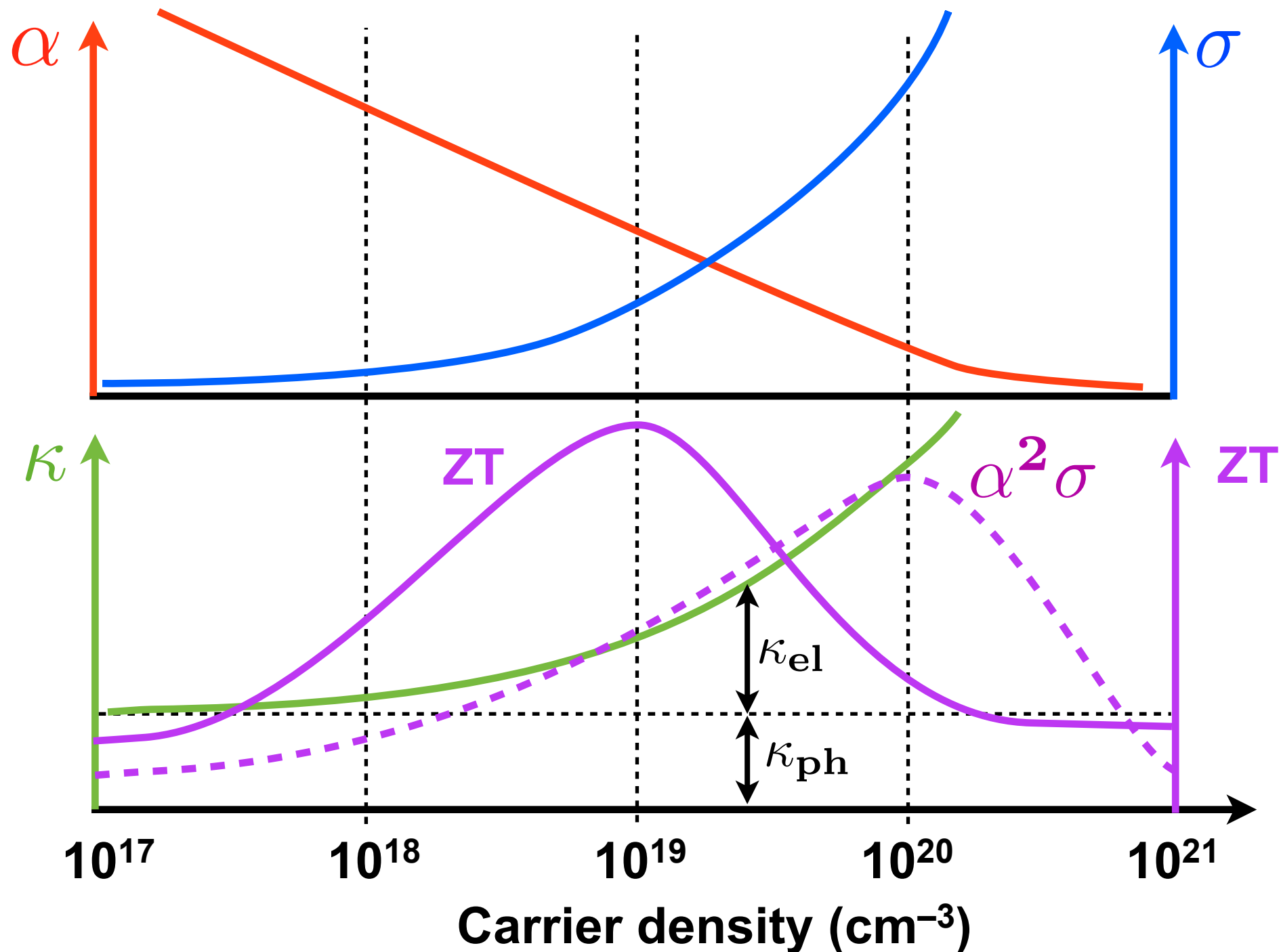
At the mm and μm scale with powers $\ll 1\text{W}$, thermoelectrics are more efficient than thermodynamic engines (Reynolds no. etc..)

- **NASA with finite Pu fuel for RTG requires high efficiency**
- **Automotive requires high power (heat is abundant)**
- **Industrial sensing requires high power (heat is abundant)**
- **Autonomous sensing requires high power (heat is abundant)**
- **As heat is abundant the issue is how to maximise power output NOT efficiency for most applications**

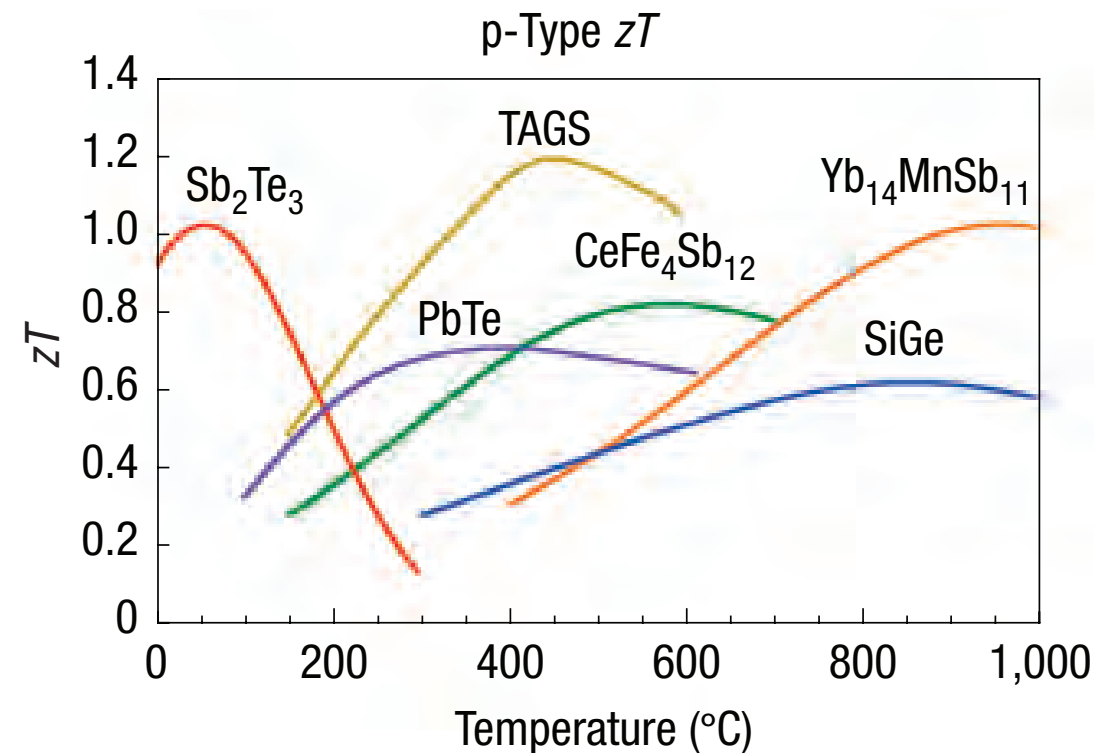
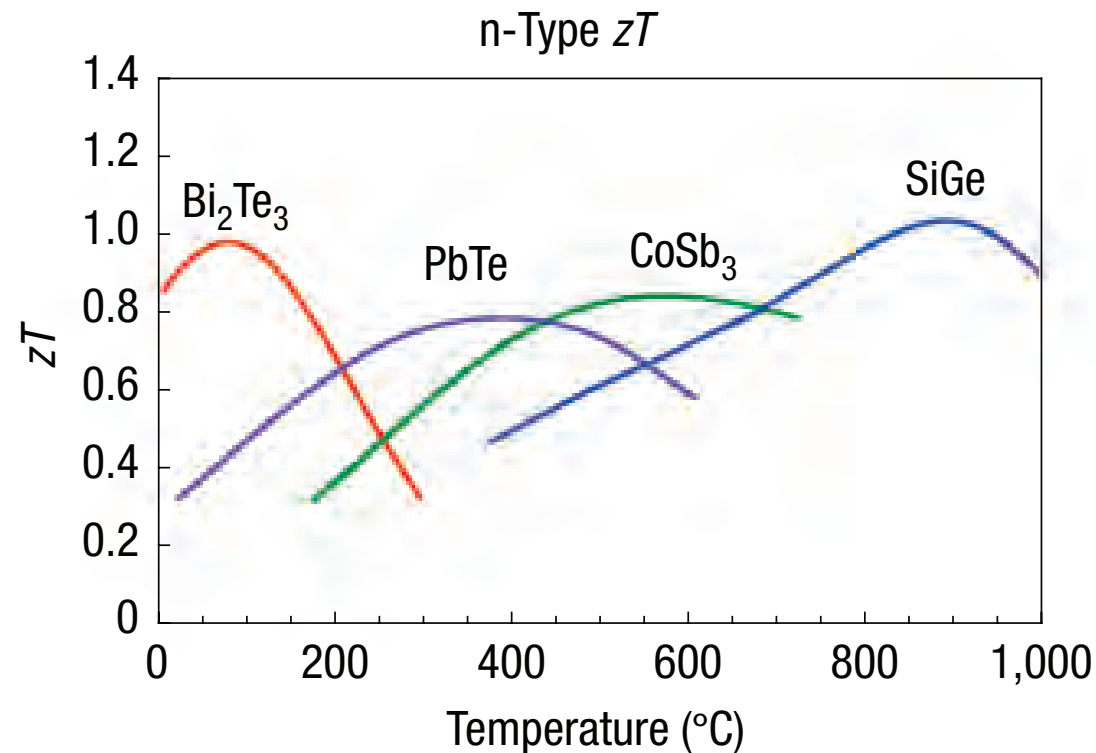
$$\text{Power} \propto \alpha^2 \sigma$$

- As the system has thermal conductivity κ a maximum ΔT can be sustained across a module limited by heat transport
- $$\Delta T_{\max} = \frac{1}{2} Z T_c^2$$
- The efficiency cannot be increased indefinitely by increasing T_h
- The thermal conductivity also limits maximum ΔT in Peltier coolers
- Higher ΔT_{\max} requires better Z materials





- Electrical and thermal conductivities are not independent
- Wiedemann Franz rule: electrical conductivity \propto thermal conductivity at high doping



Nature Materials 7, 105 (2008)

- Bulk n- Bi_2Te_3 and p- Sb_2Te_3 used in most commercial thermoelectrics & Peltier coolers
- But tellurium is 9th rarest element on earth !!!
- Bulk $\text{Si}_{1-x}\text{Ge}_x$ ($x \sim 0.2$ to 0.3) used for high temperature satellite applications

Reducing thermal conductivity faster than electrical conductivity:

- e.g. skutterudite structure: filling voids with heavy atoms

Low-dimensional structures:

- Increase α by enhanced DOS $\left(\alpha = -\frac{\pi^2}{3q} k_B^2 T \left[\frac{d \ln(\mu(E)g(E))}{dE} \right]_{E=E_F} \right)$
- Make κ and σ almost independent
- Reduce κ through phonon scattering on heterointerfaces

Energy filtering:

- $$\alpha = -\frac{k_B}{q} \left[\frac{E_c - E_F}{k_B T} + \frac{\int_0^\infty \frac{(E - E_c)}{k_B T} \sigma(E) dE}{\int_0^\infty \sigma(E) dE} \right]$$

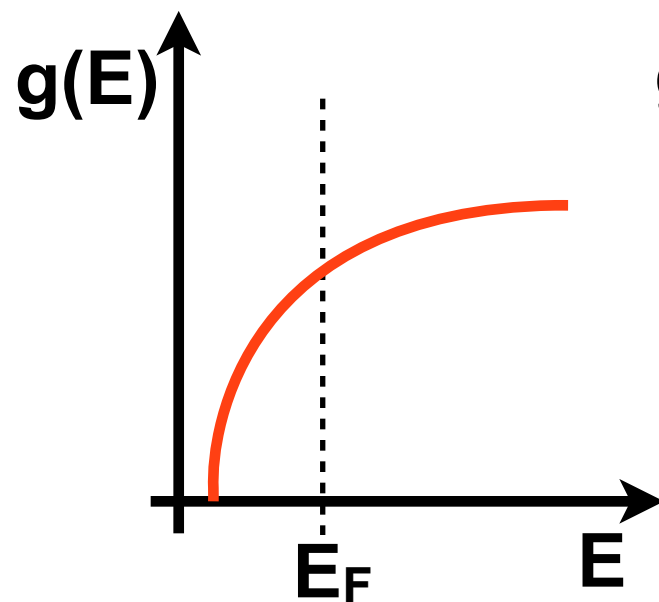
Y.I. Ravich et al., Phys. Stat. Sol. (b) 43, 453 (1971)

enhance

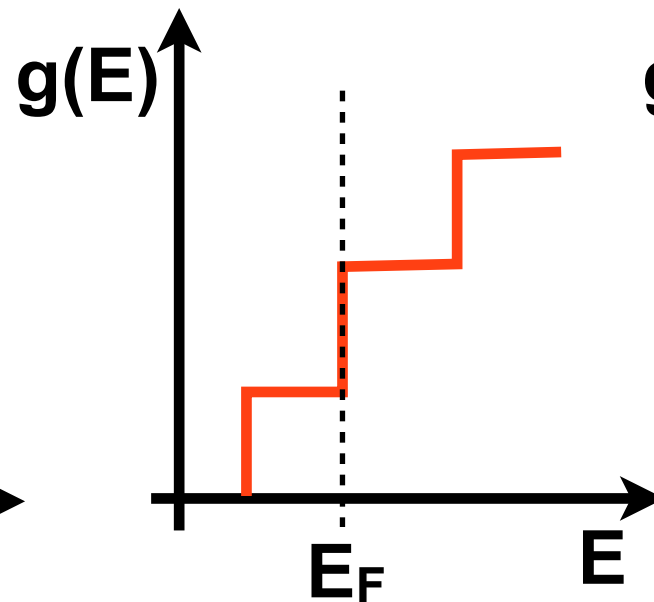
- Increase α through enhanced DOS:

$$\alpha = -\frac{\pi^2}{3q} k_B^2 T \left[\frac{d \ln(\mu(E)g(E))}{dE} \right]_{E=E_F}$$

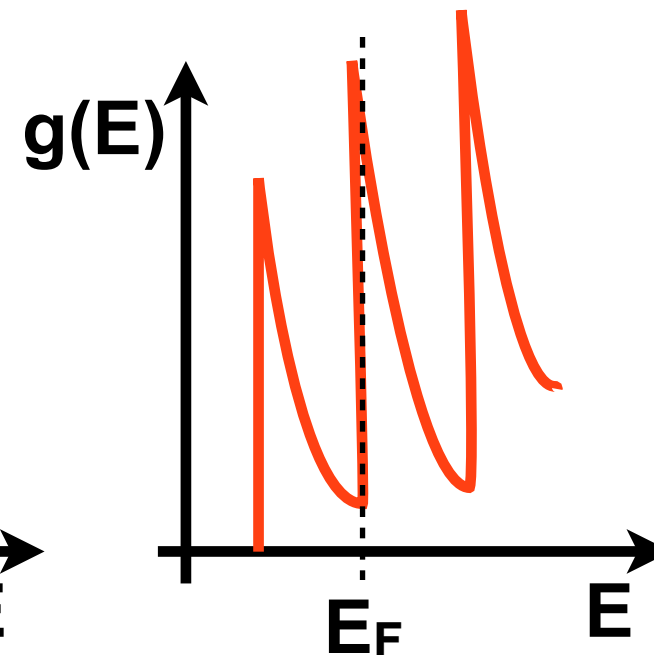
3D
bulk



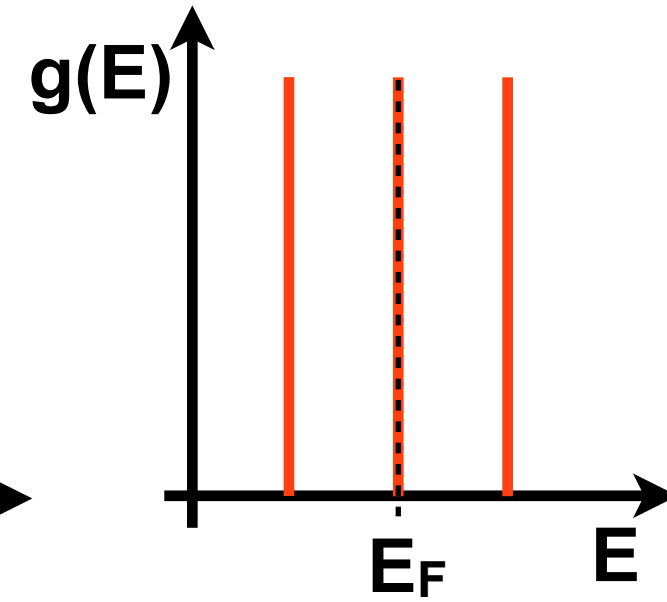
2D
quantum well



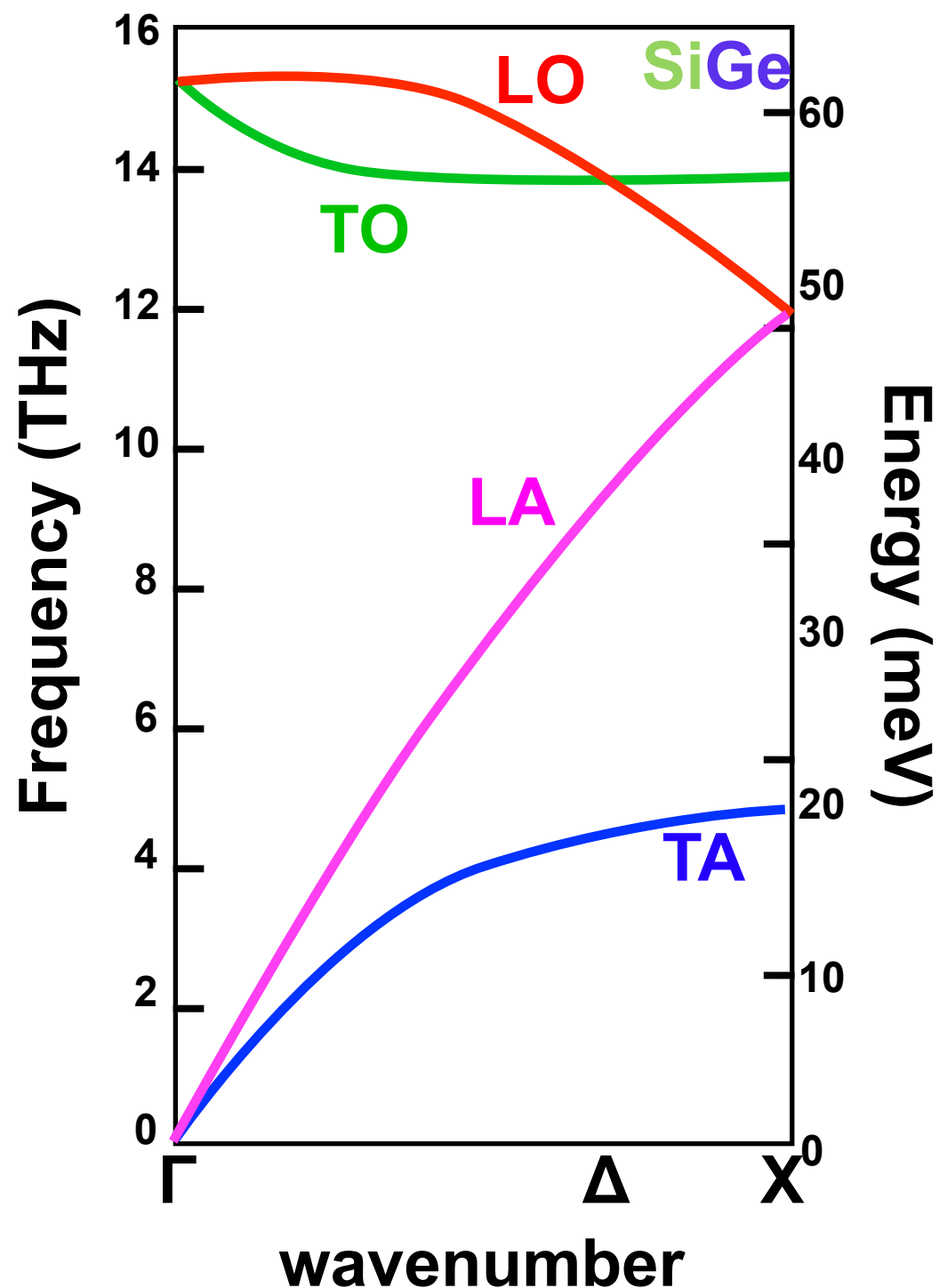
1D
quantum wire



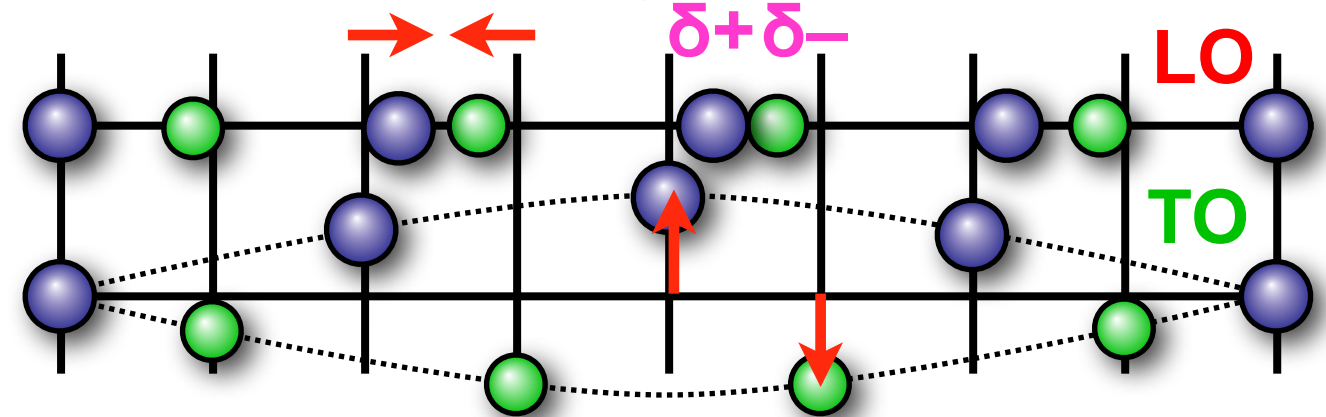
0D
quantum dot



————— α increasing —————→

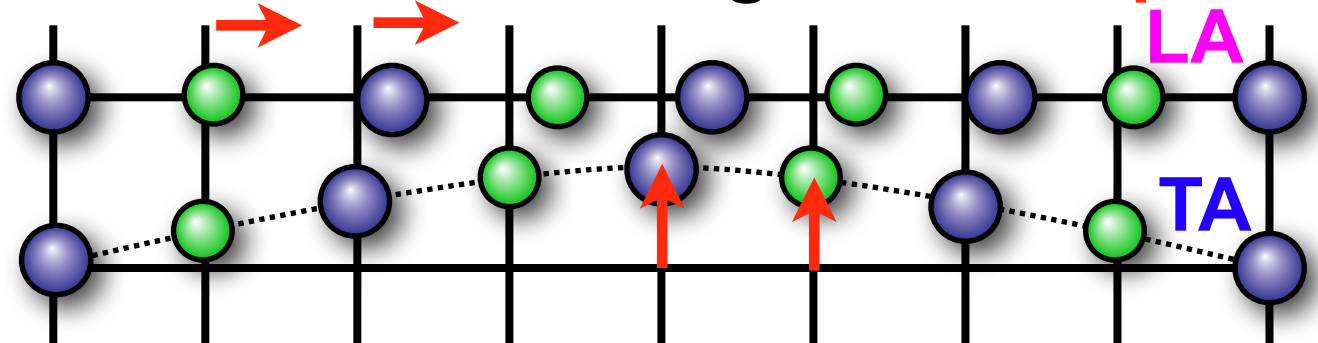


optic modes - neighbours in **antiphase**

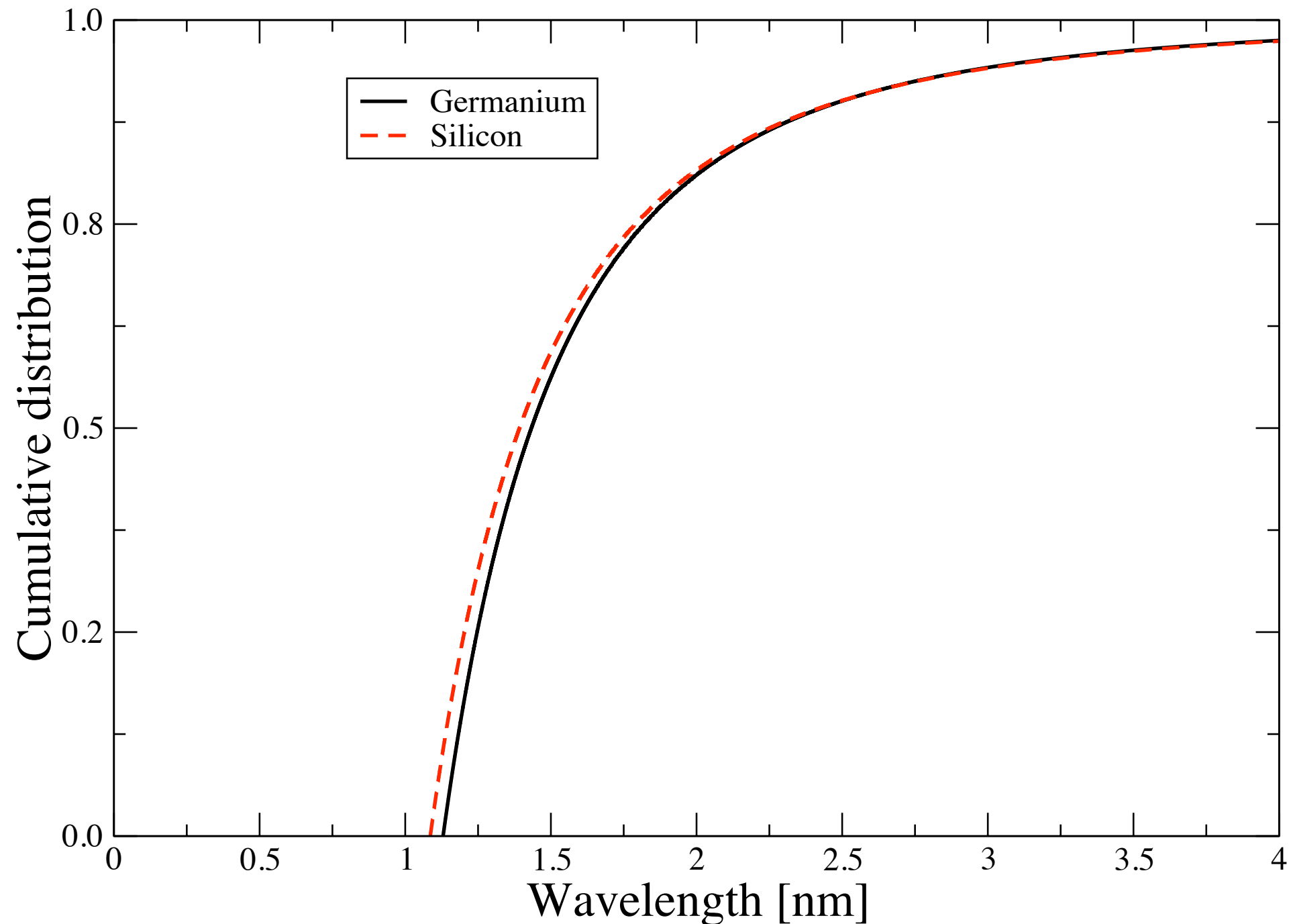


NB acoustic phonons transmit
most thermal energy

acoustic modes - neighbours in **phase**



 The majority of heat in solids is transported by acoustic phonons



Greater than 95% of heat conduction in Si / Ge from phonons with wavelengths between 1.2 and 3.5 nm

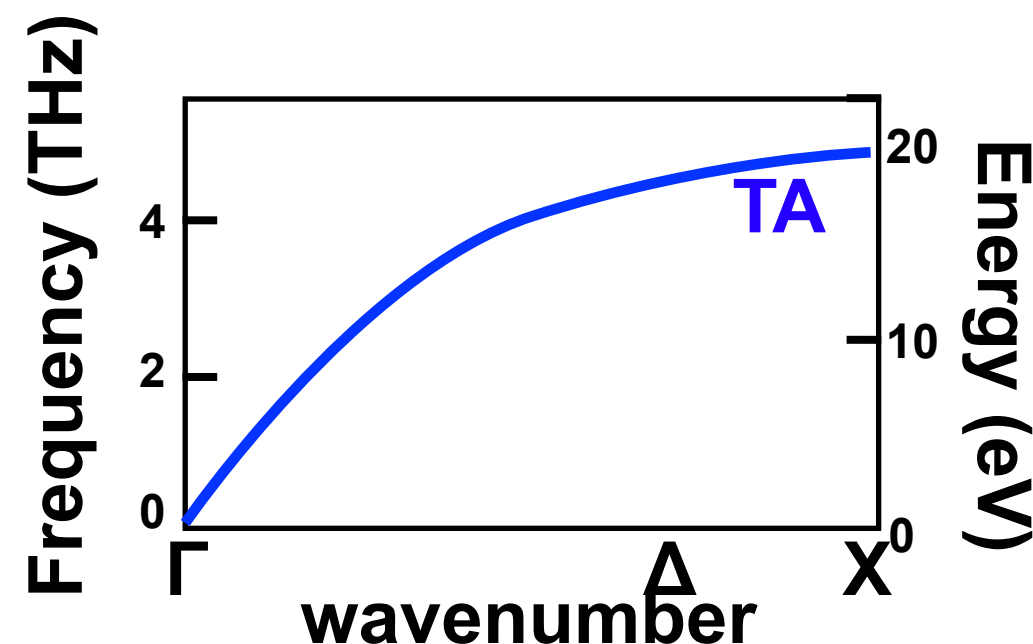
Phonon scattering:

- Require structures below the phonon mean free path (10s nm)

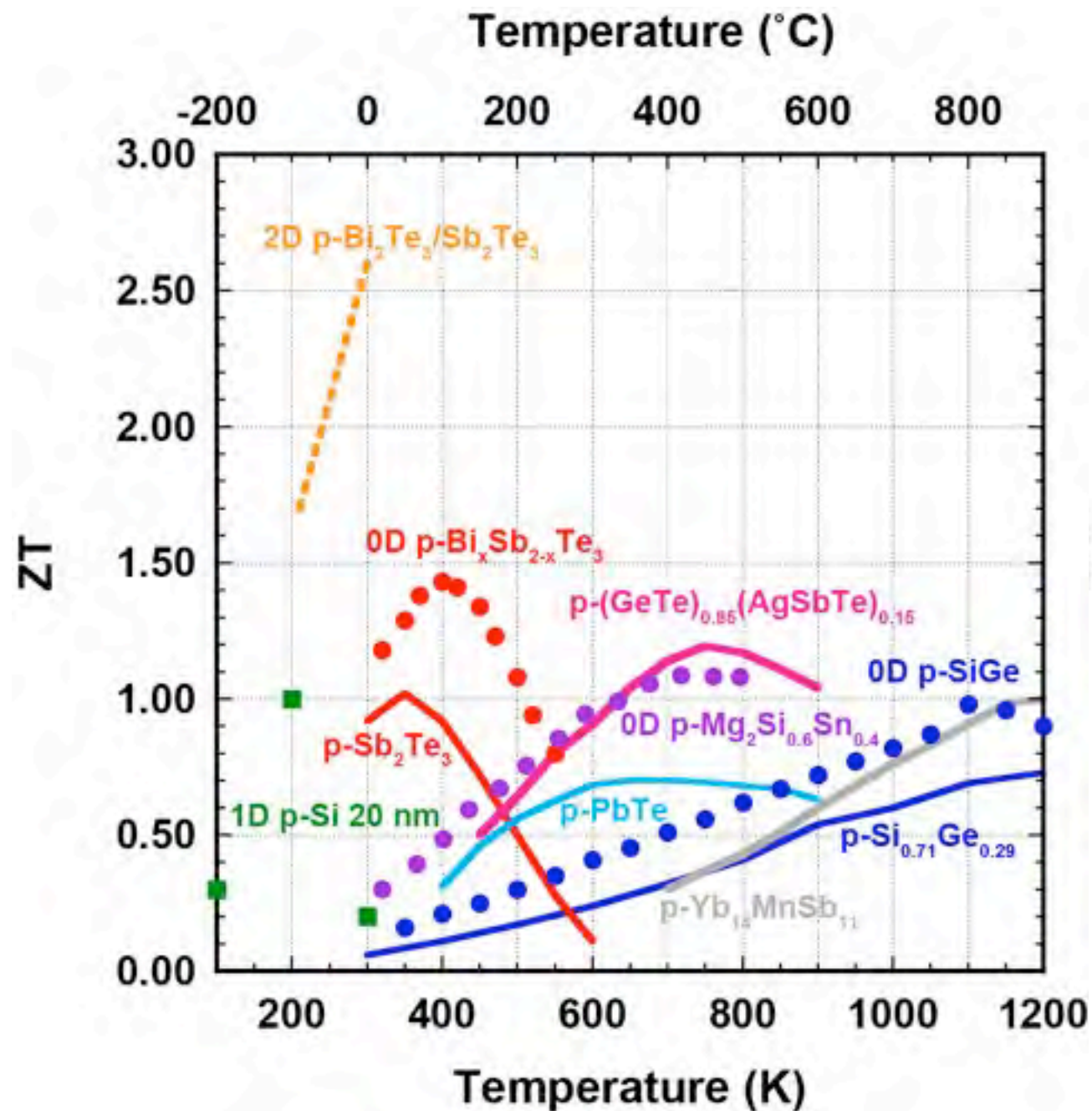
Phonon Bandgaps:

- Change the acoustic phonon dispersion → stationary phonons or bandgaps
- Require structures with features at the phonon wavelength (< 5 nm)

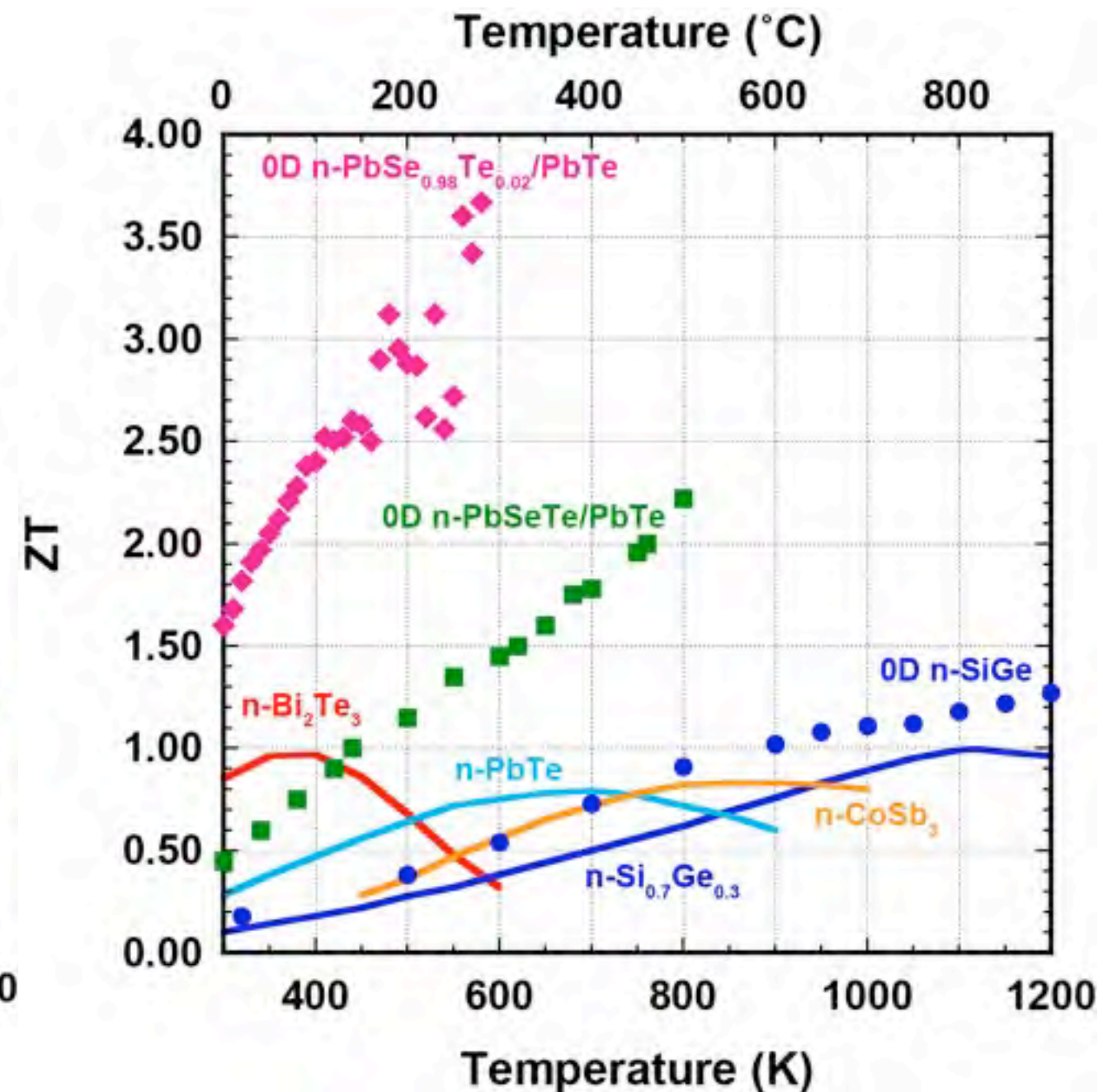
- Phonon group velocity $\propto \frac{dE}{dk_q}$



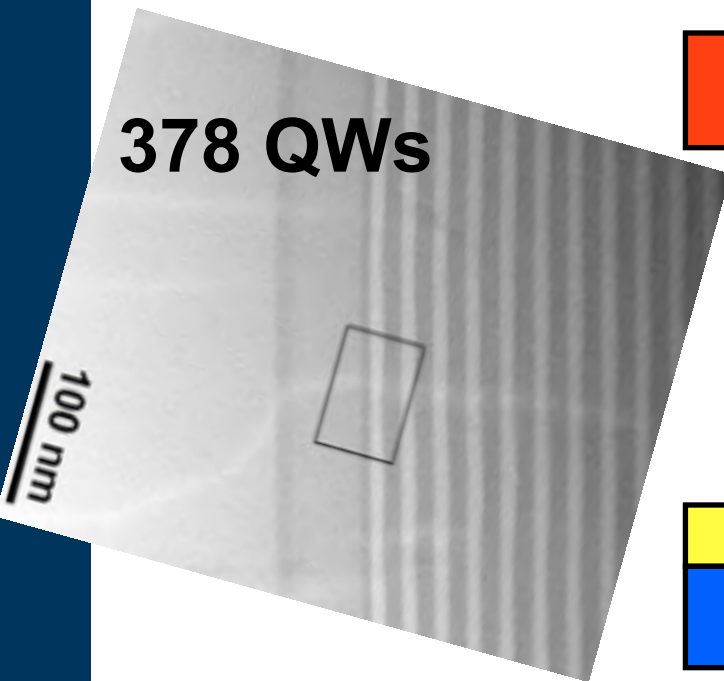
p-type



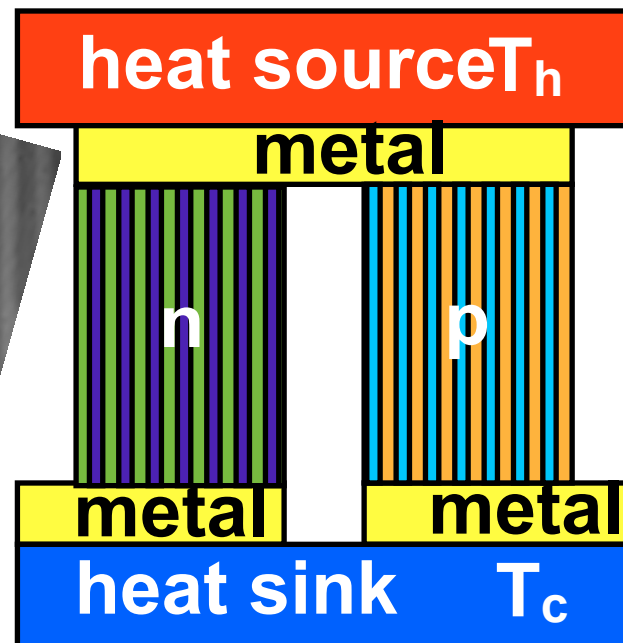
n-type



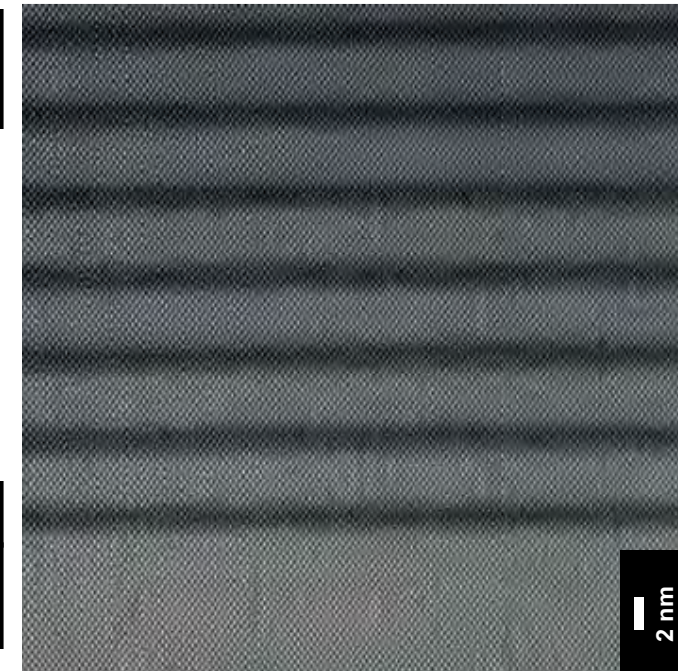
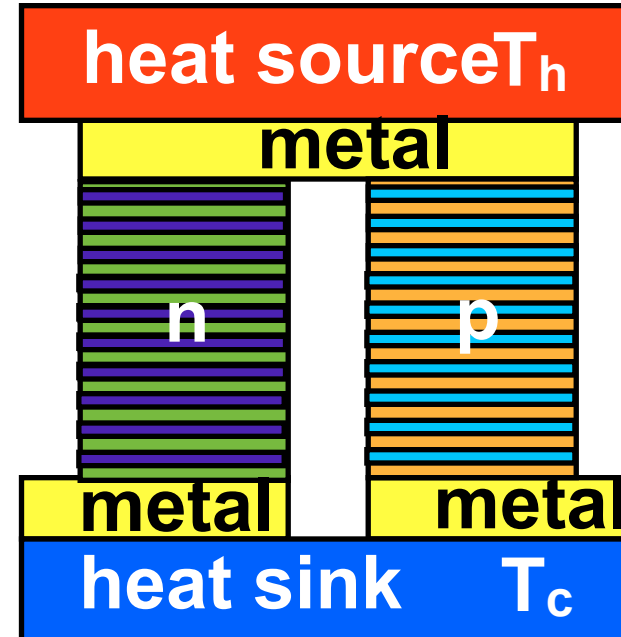
Nanostructures can improve Seebeck coefficient and/or decrease thermal conductivity



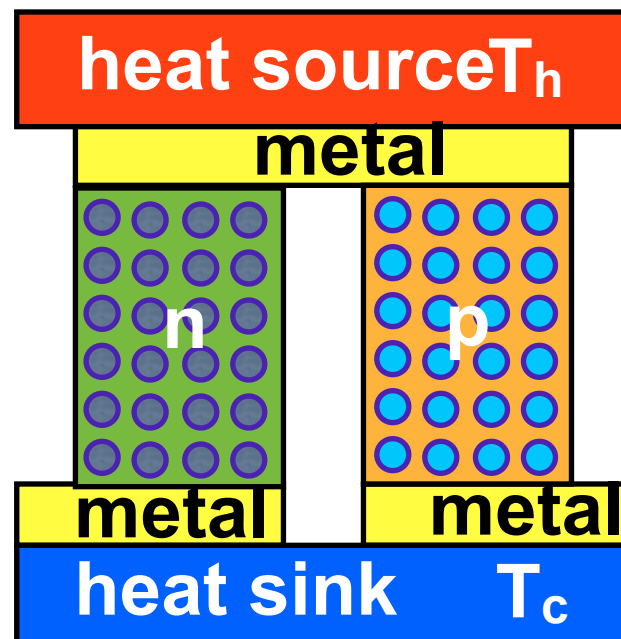
Lateral superlattice



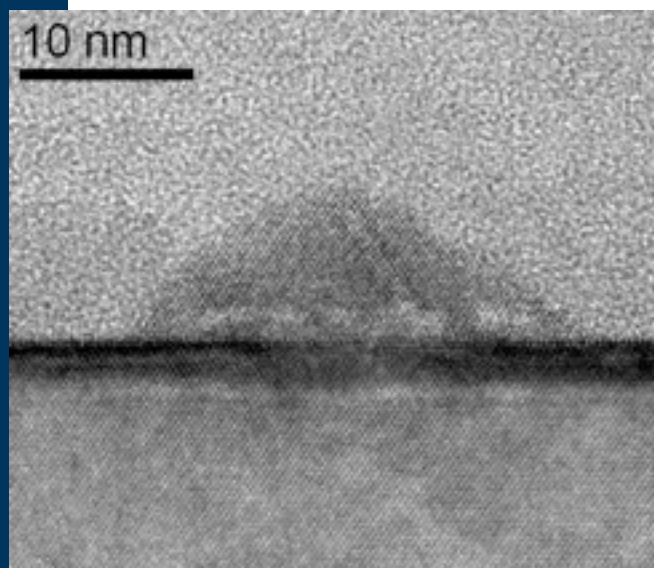
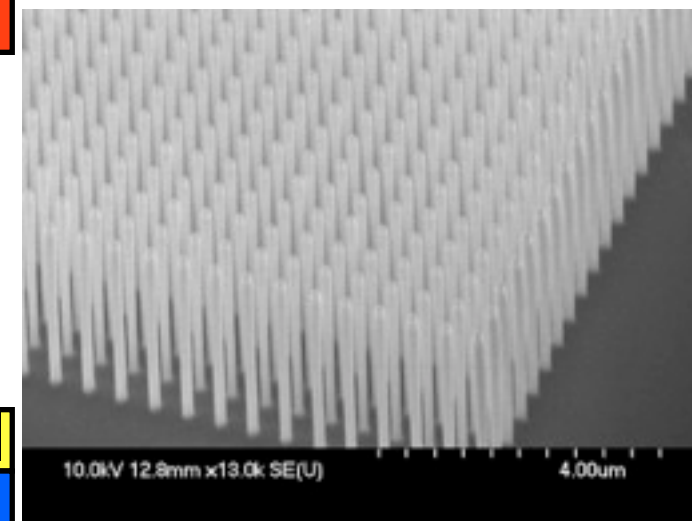
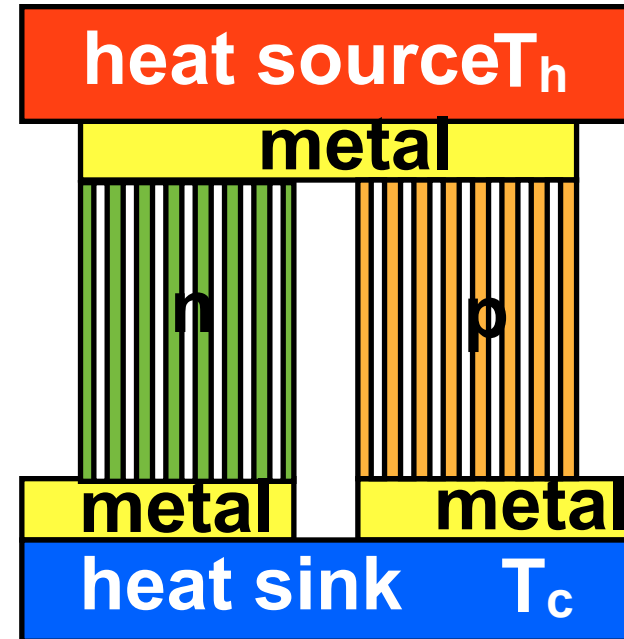
Vertical superlattice



Quantum Dots



Nanowires



- Use of transport perpendicular to superlattice quantum wells
- Higher α from the higher density of states
- Lower electron conductivity from tunnelling
- Lower κ_{ph} from phonon scattering at heterointerfaces
- Able to engineer lower κ_{ph} with phononic bandgaps
- Overall Z and ZT should increase

Vertical superlattice

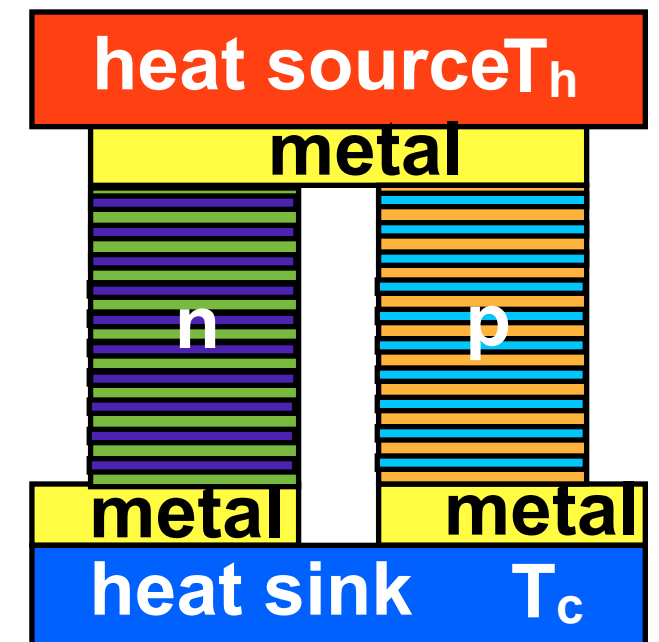


Figure of merit

$$ZT = \frac{\alpha^2 \sigma}{\kappa} T$$

SL1 to SL4: 922 x

2.85 ± 1.5 nm p-Ge QW

1.1 ± 0.6 nm p-Si_{0.5}Ge_{0.5}

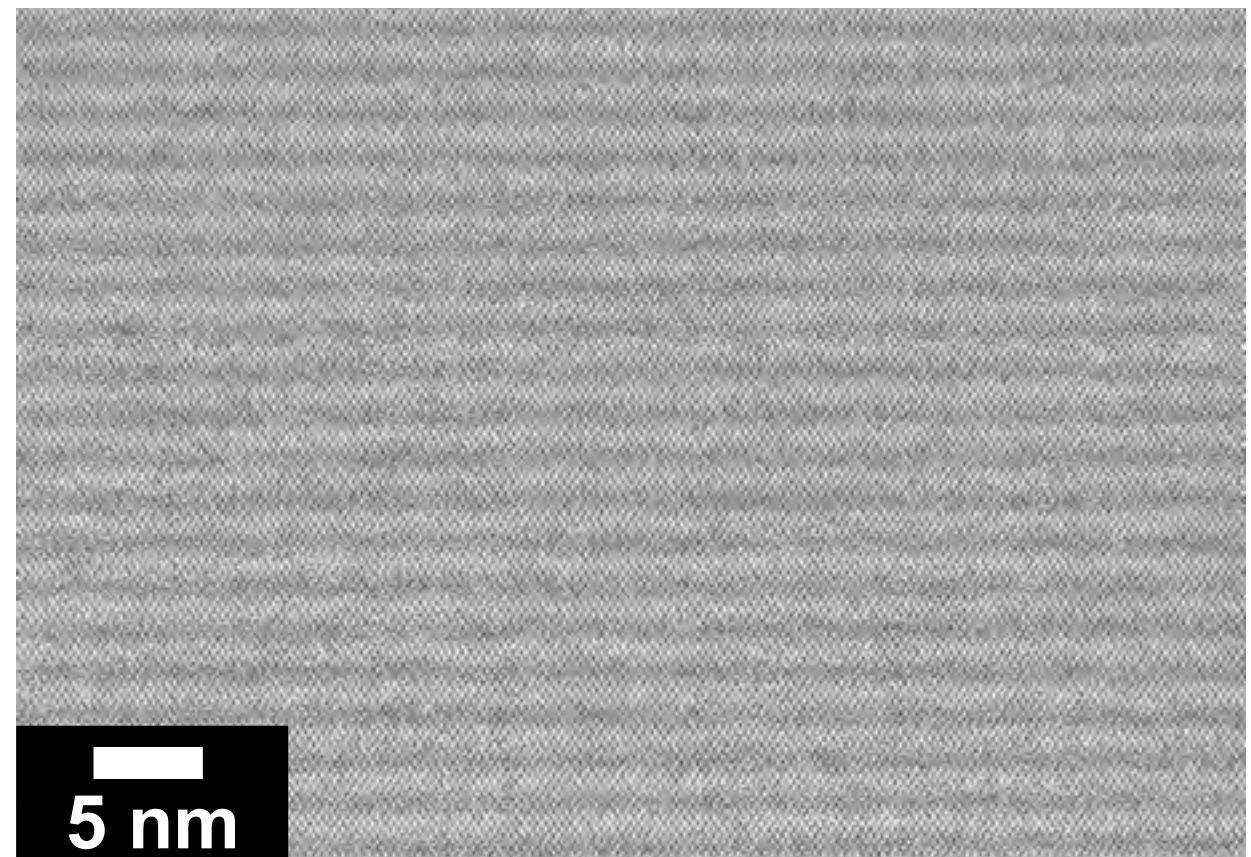
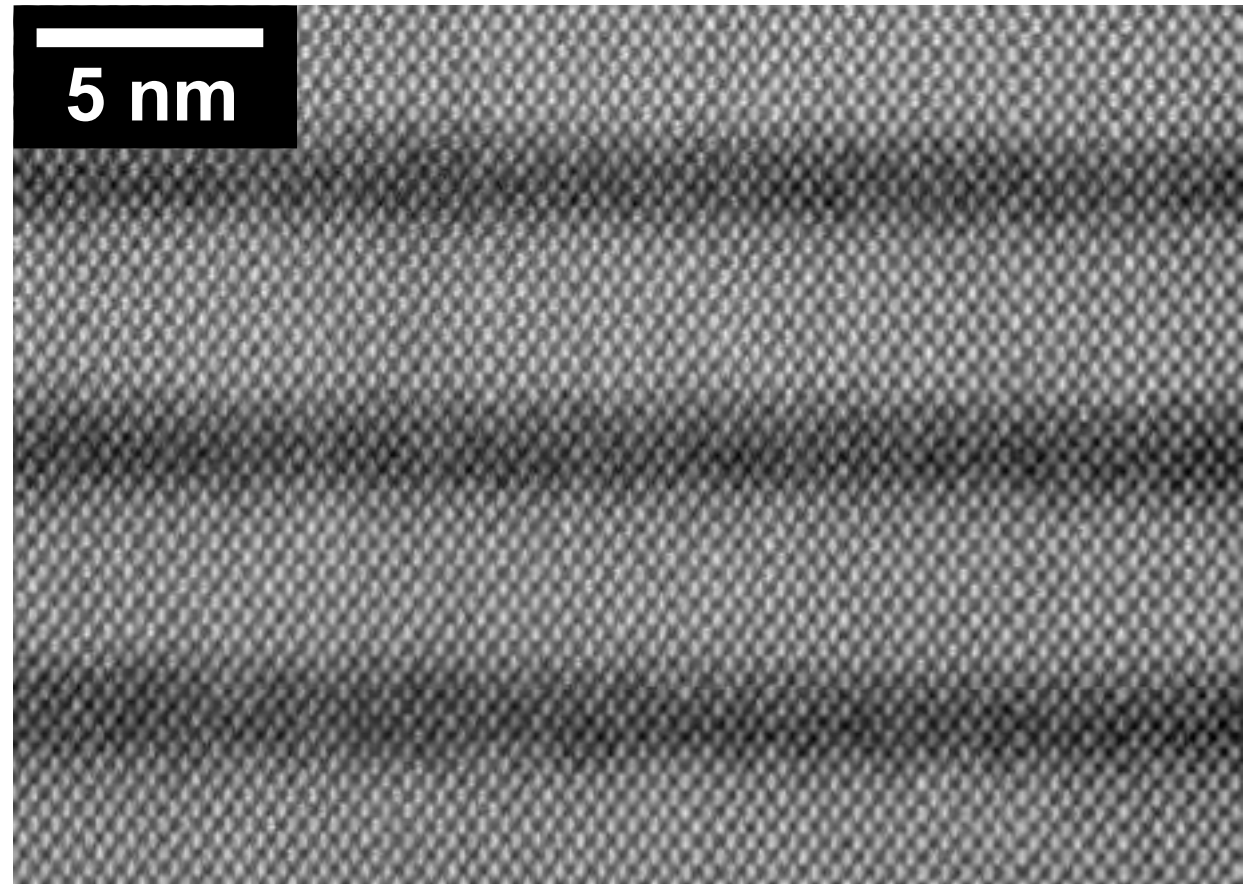
Si_{0.175}Ge_{0.825}

SL5: 2338 x

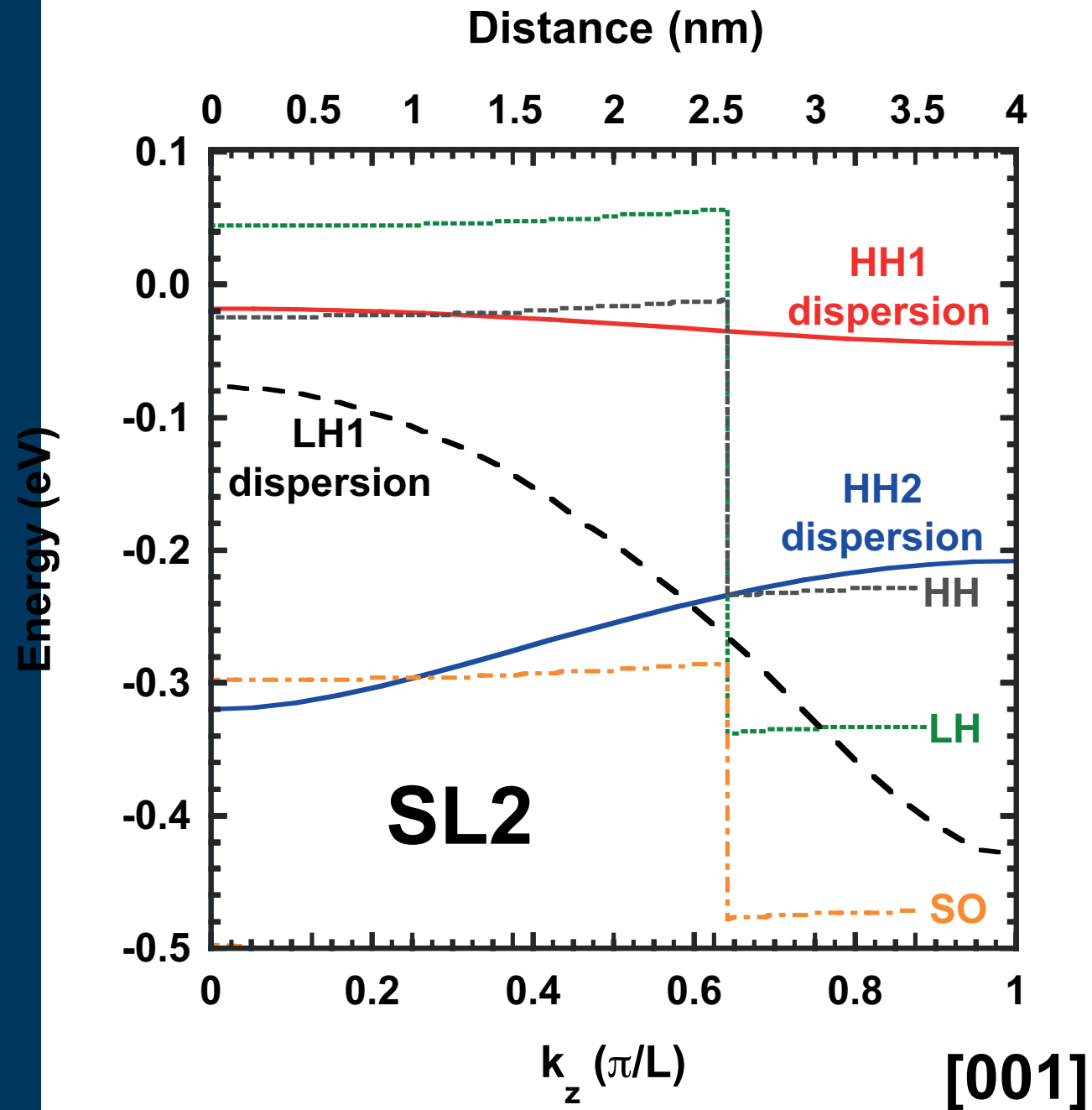
1.1 ± 0.2 nm p-Ge QW

0.5 ± 0.1 nm p-Si_{0.5}Ge_{0.5}

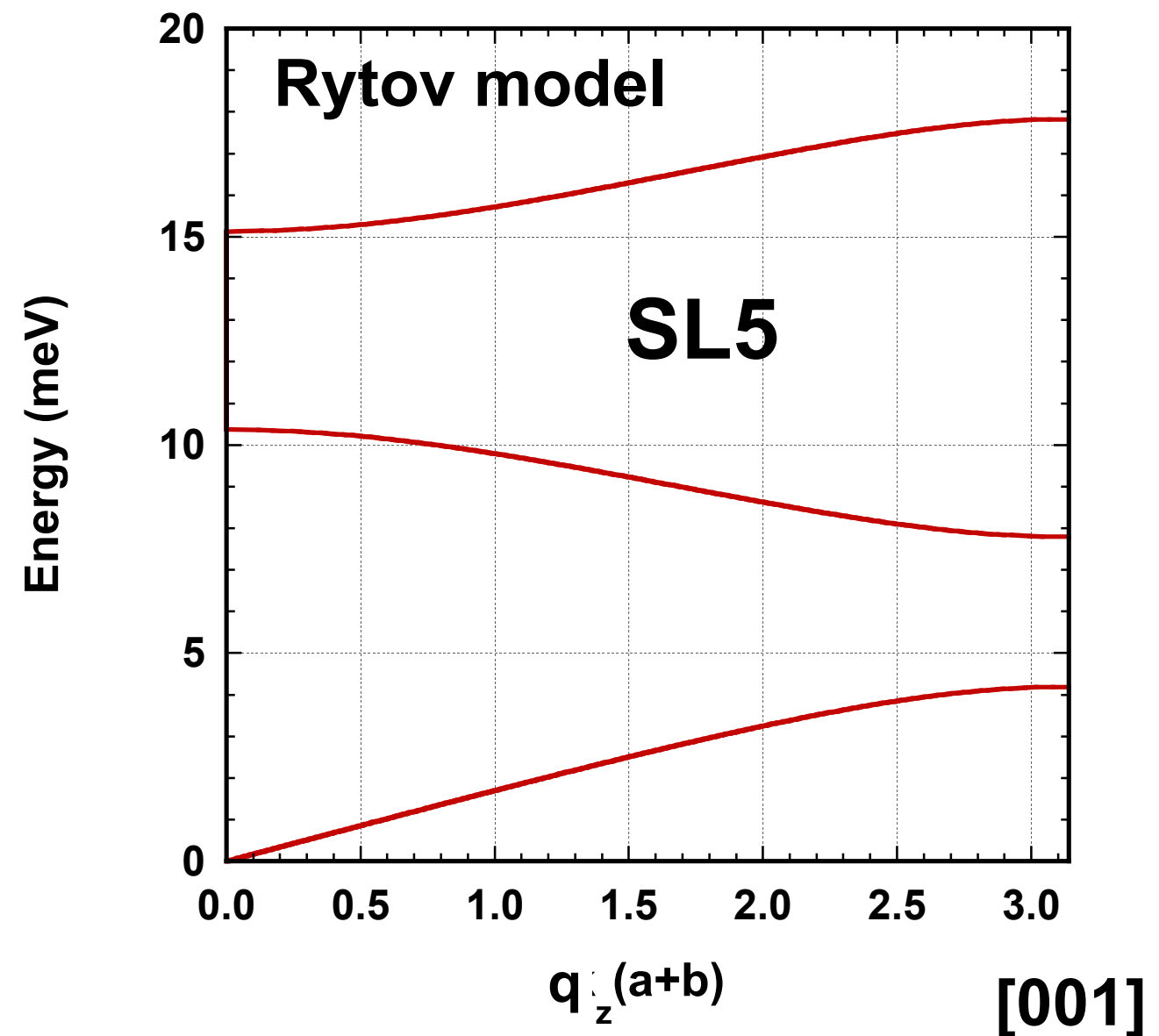
Si_{0.175}Ge_{0.825}

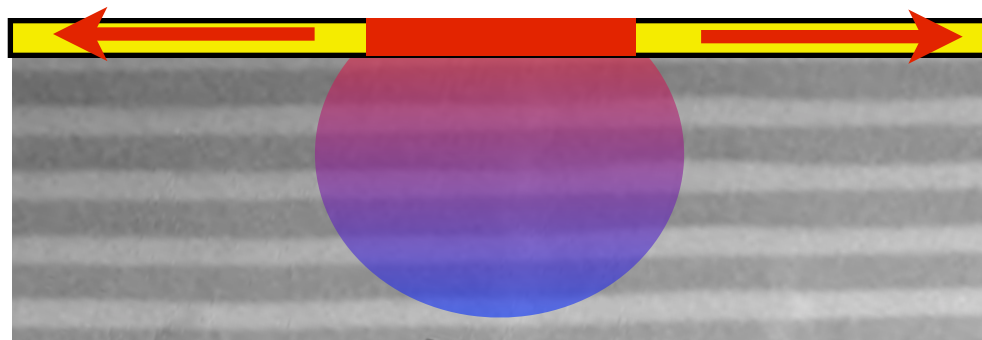
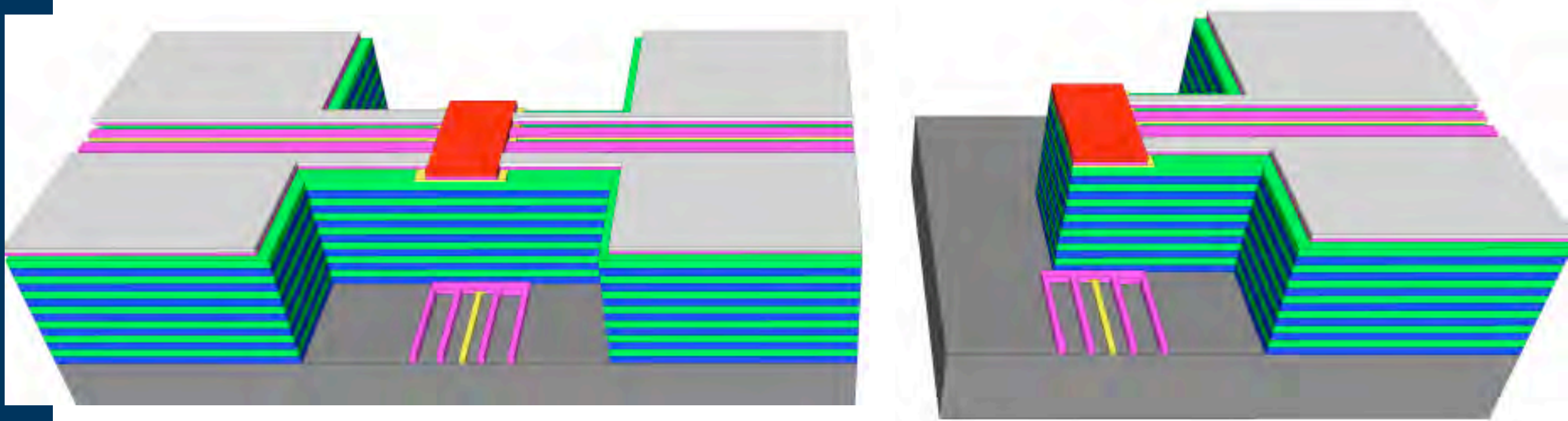


Holes (Electronic Dispersion)

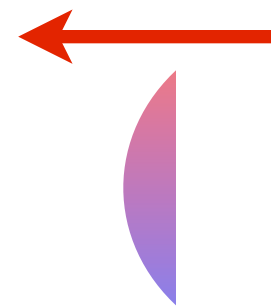


Phonon Dispersion

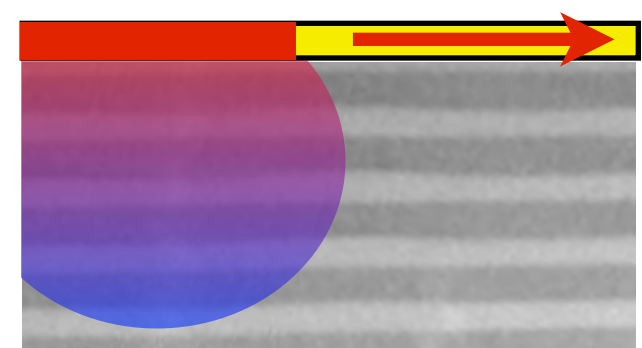




Isotropic structure



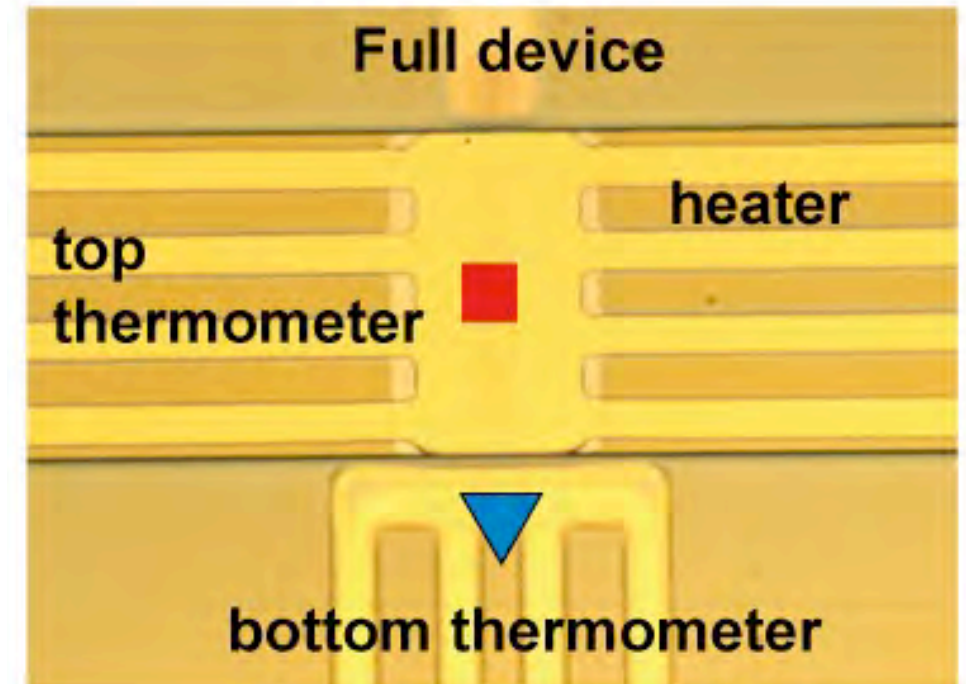
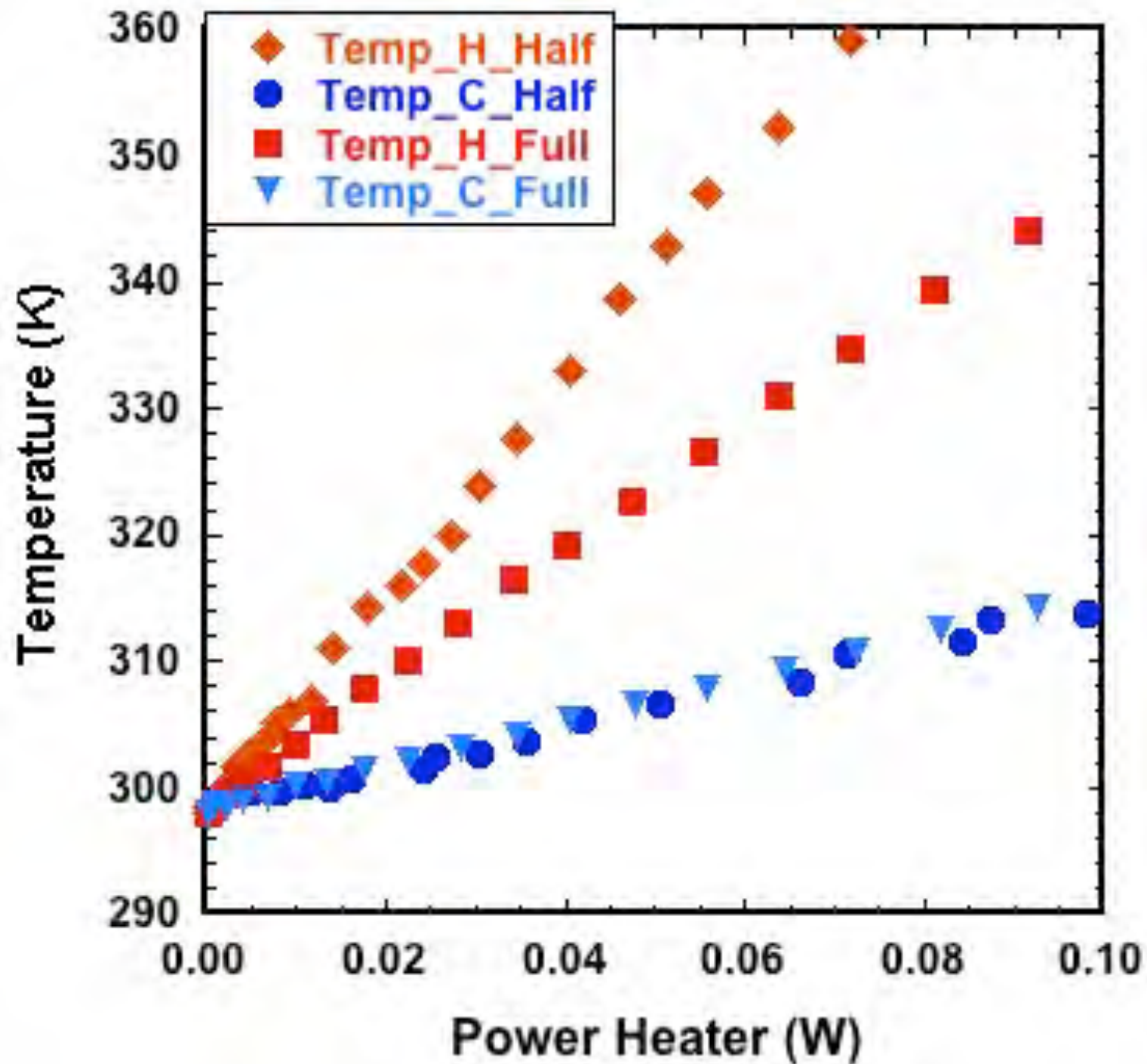
1/2 lateral
parasitic
contribution



half structure

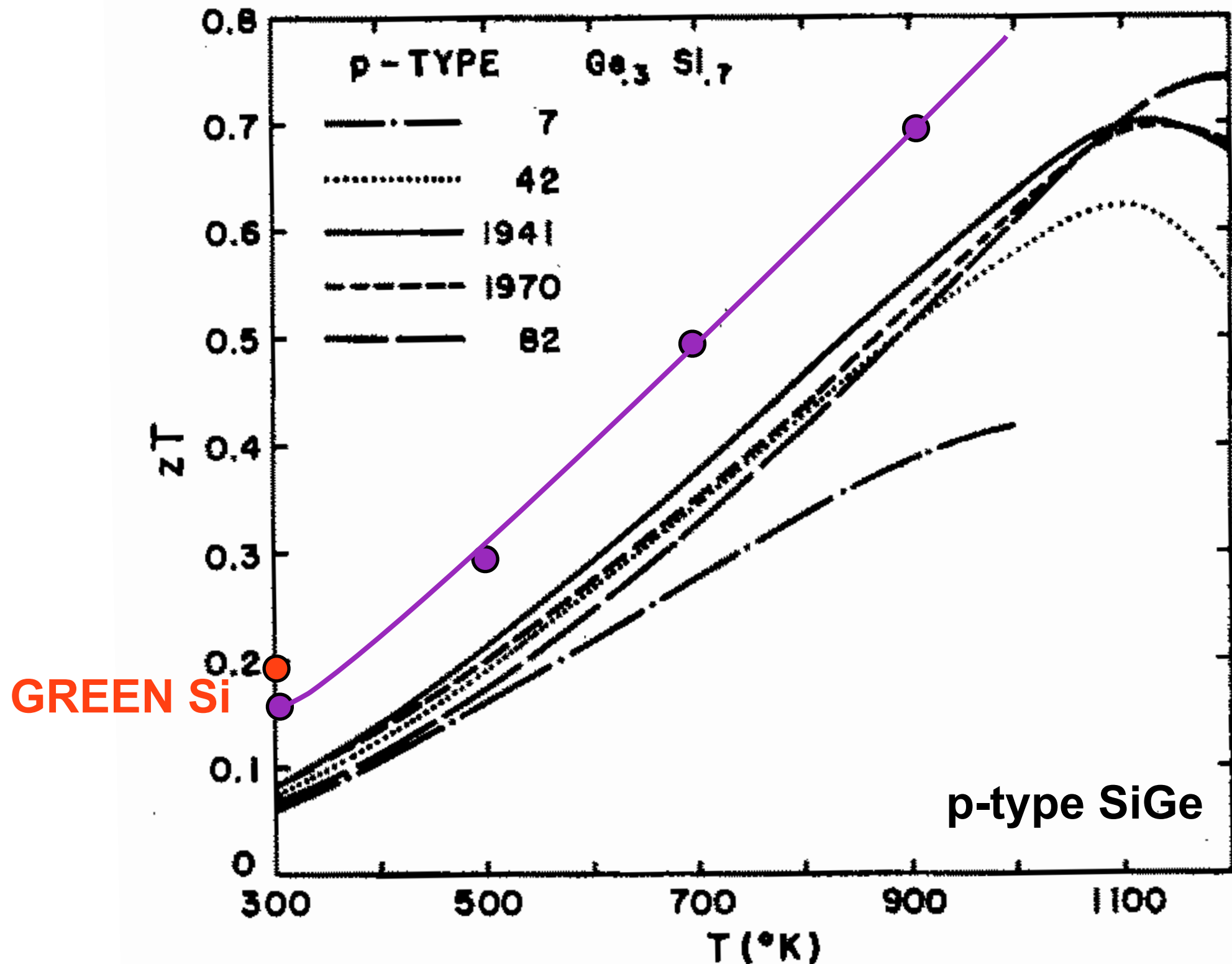


Half structure allows parasitics to be measured and removed for more accurate heat flux determination



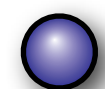
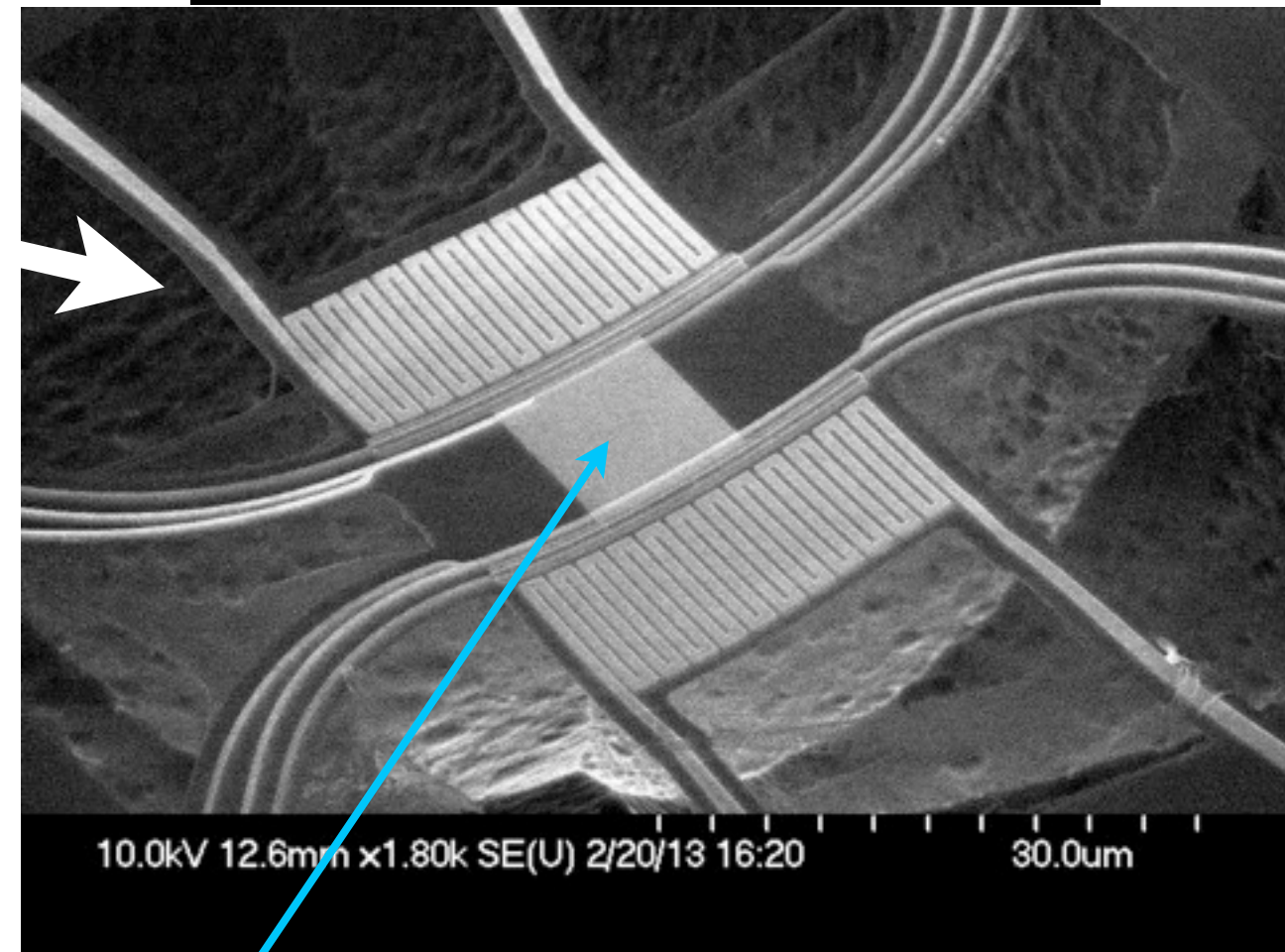
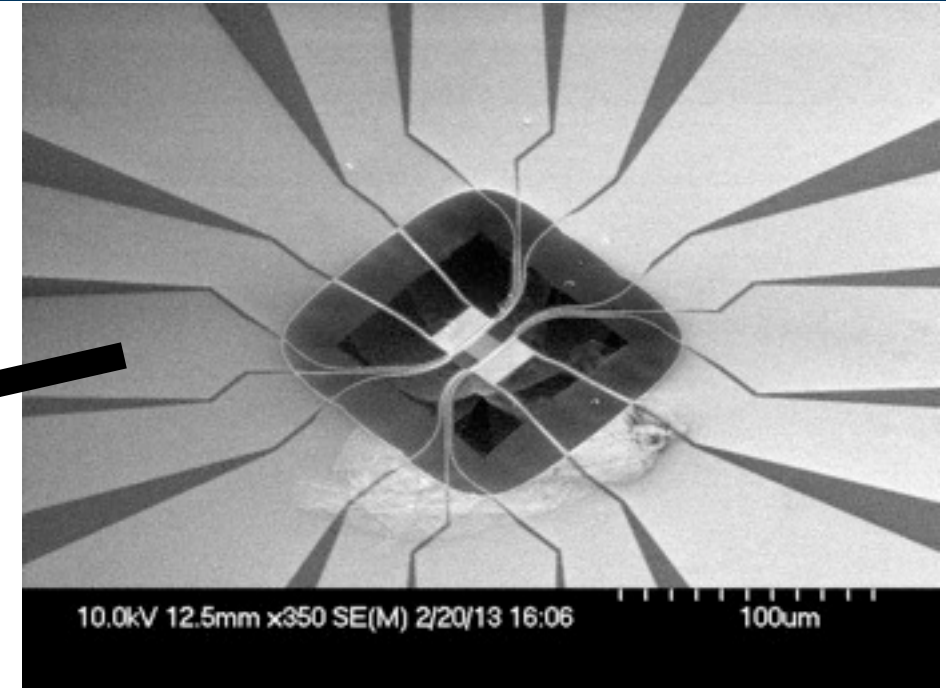
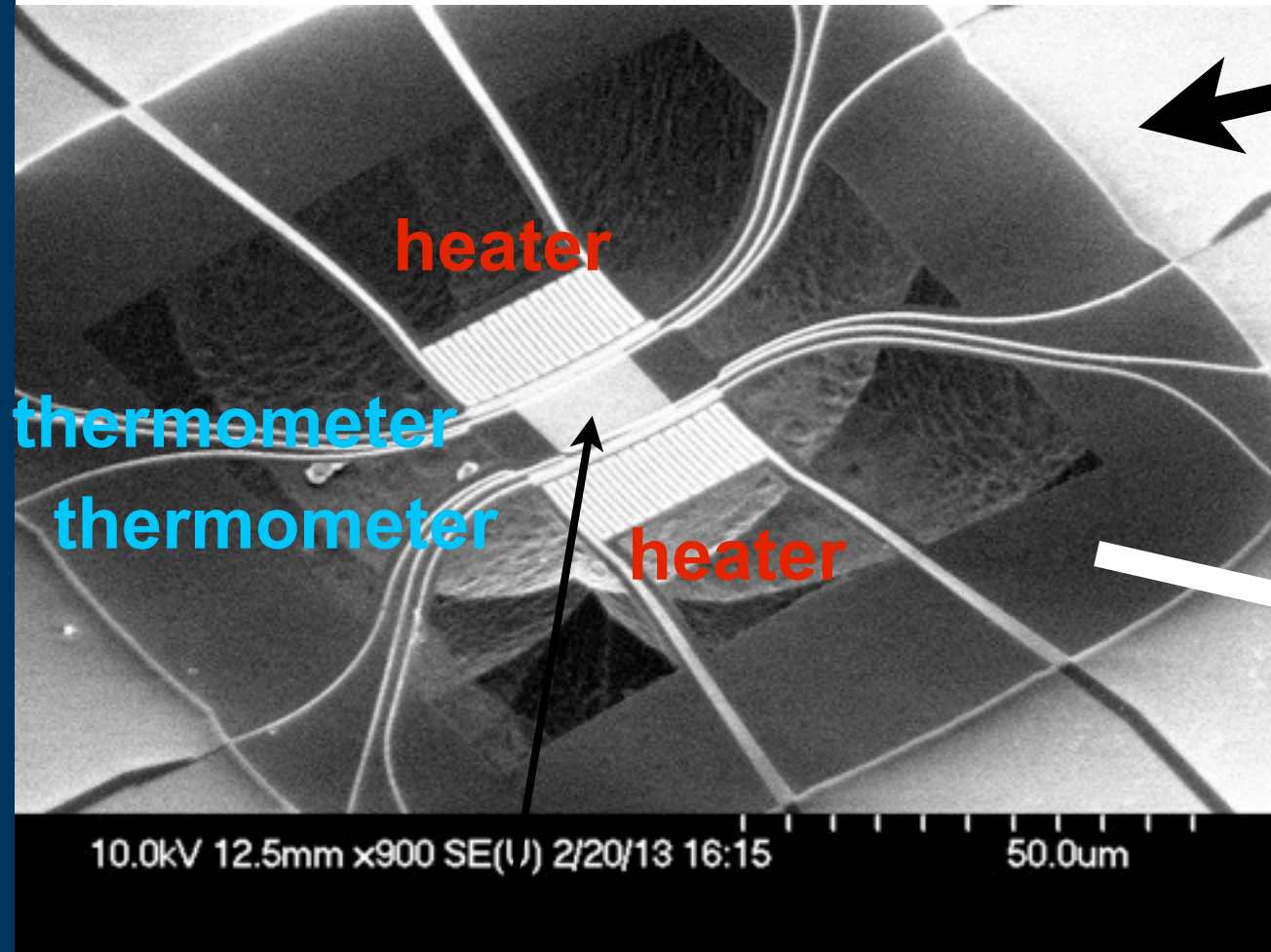
Measured 41% of heat in
vertical transport

MIT, Nano Lett. 8, 4670 (2008)



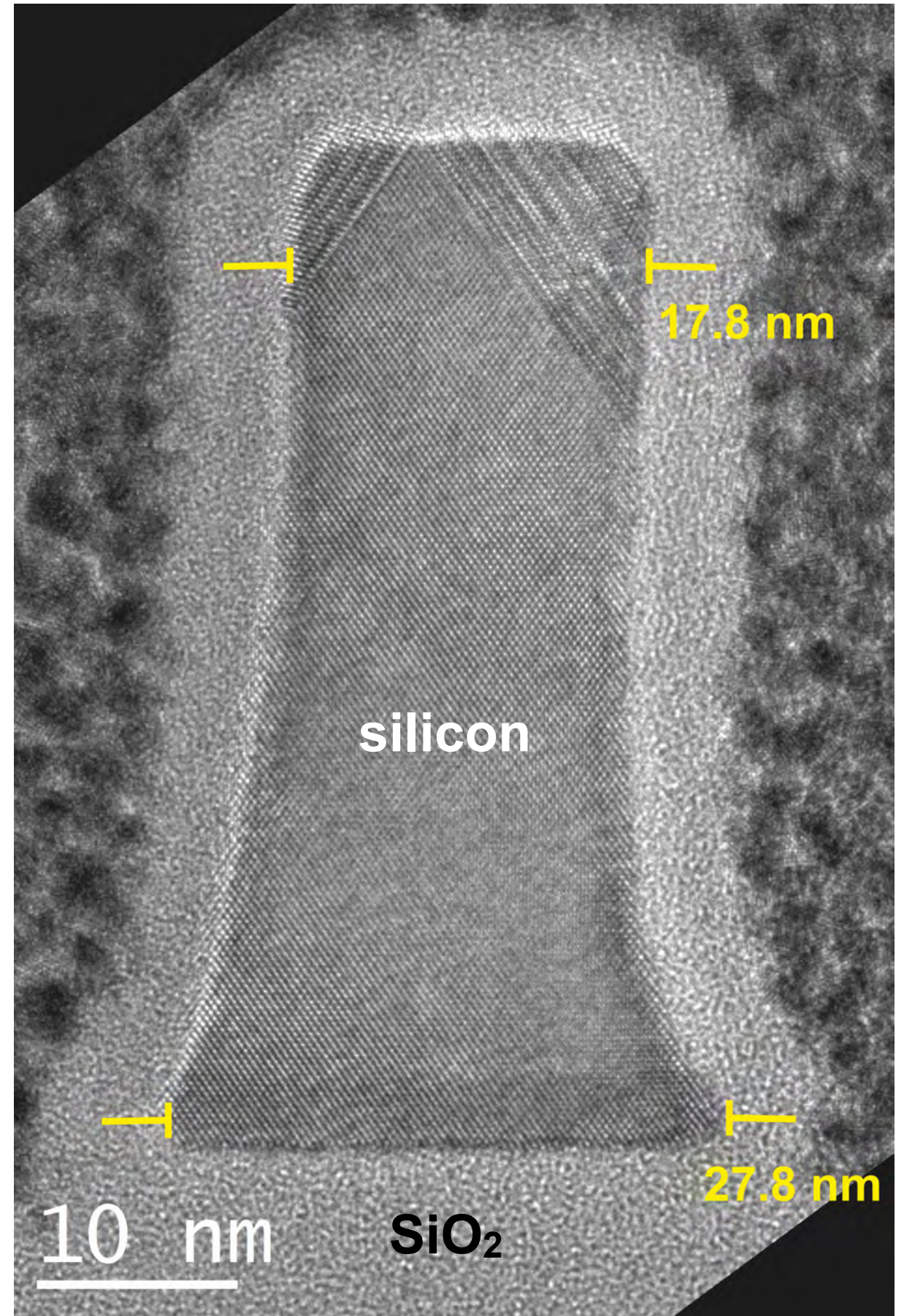
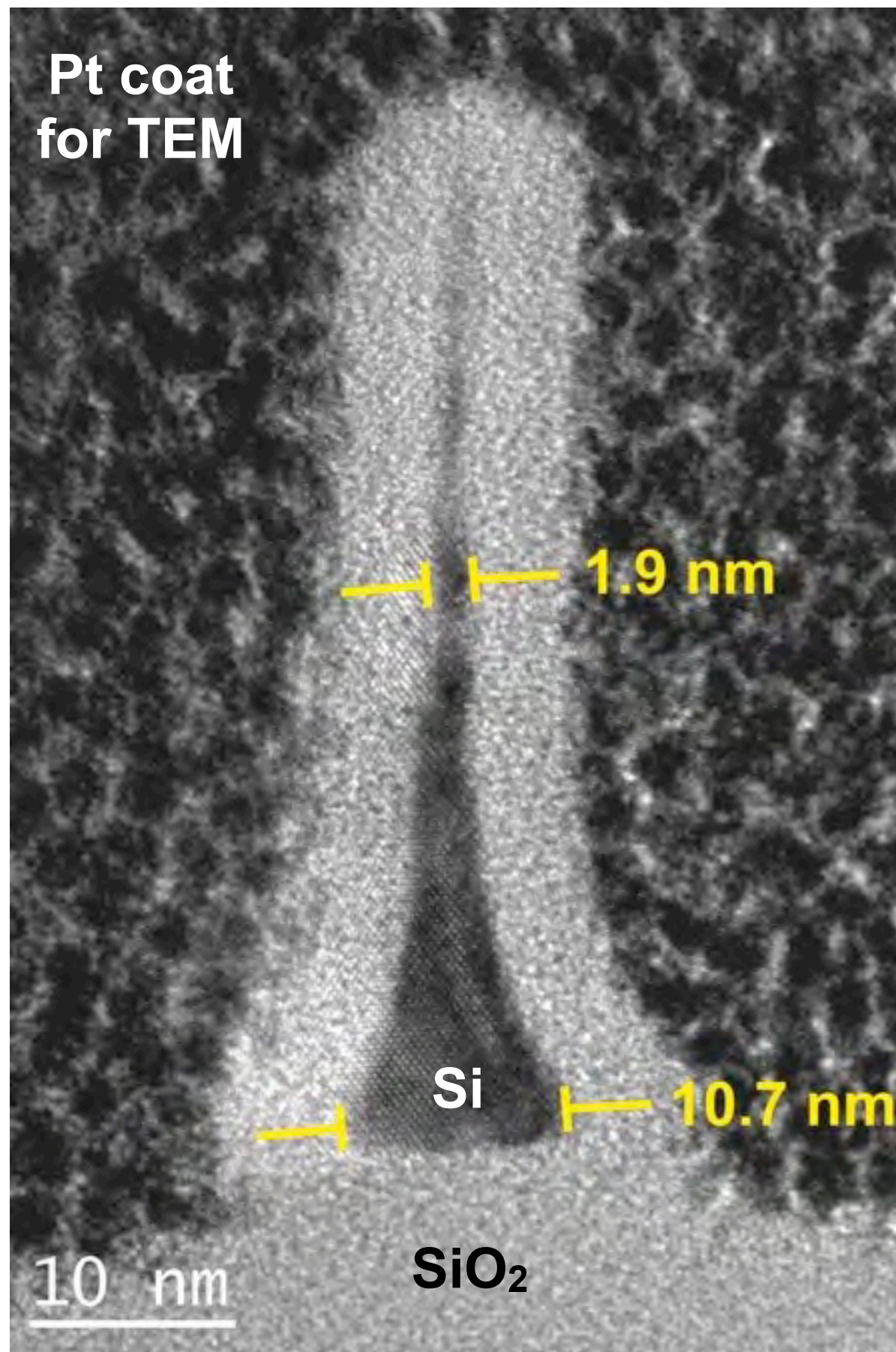
J.P. Dismukes et al., J. Appl. Phys. 35, 2899 (1964)

Nanowire Fabrication on Suspended Hall Bar

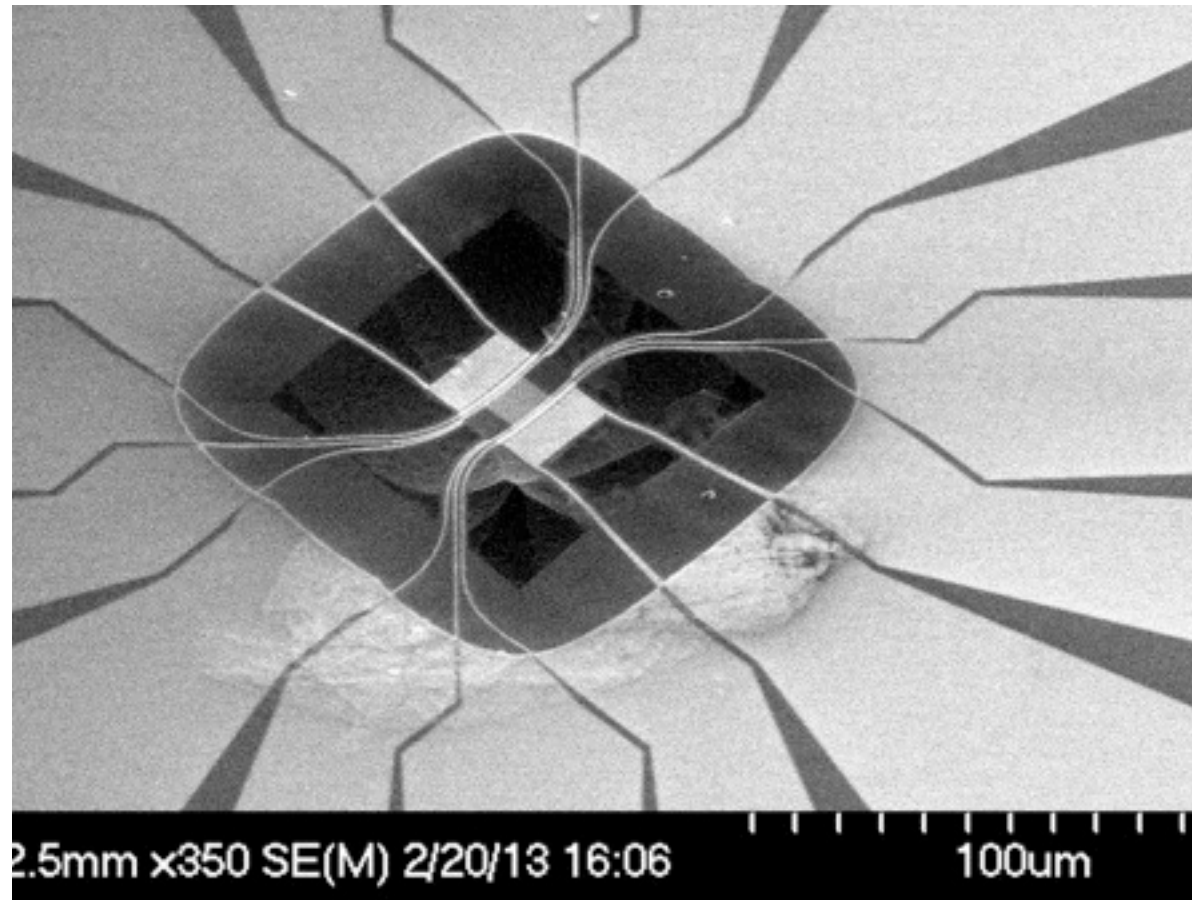


100 x 45 nm wide Si nanowires with integrated heaters, thermometers and electrical probes

Si Nanowires: How many atoms wide?



45 nm Wide n-Silicon Nanowires

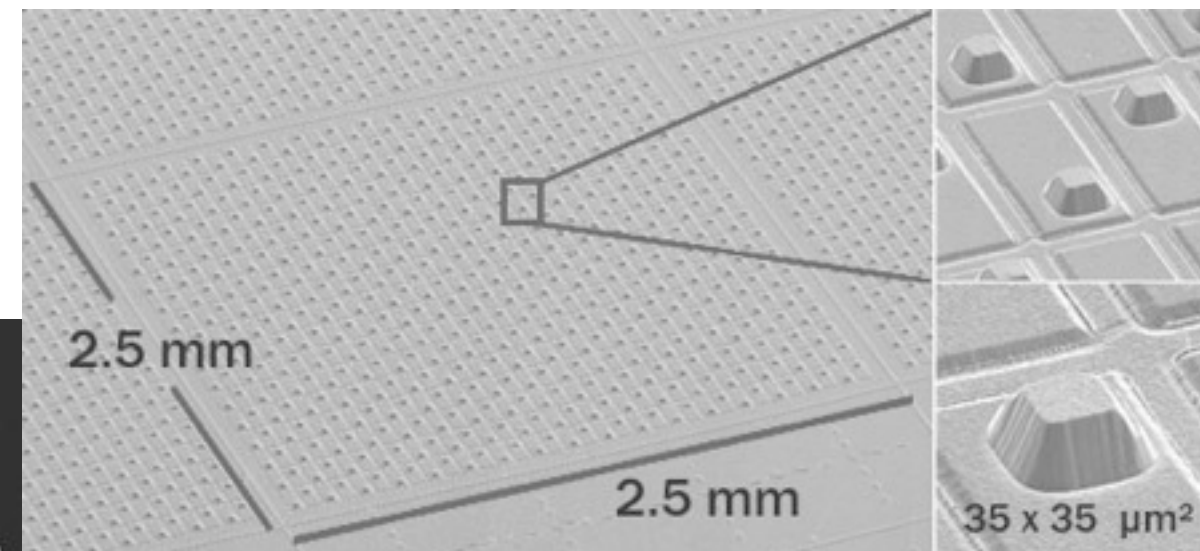
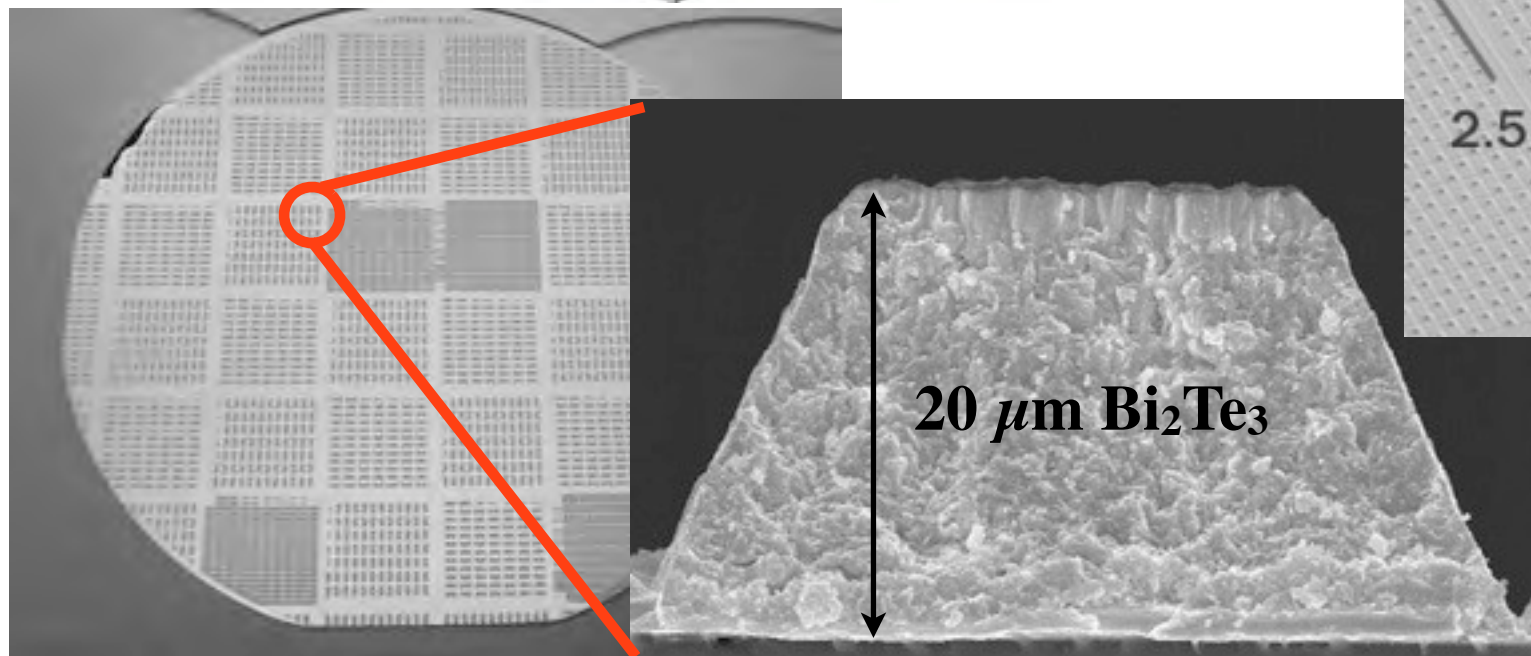
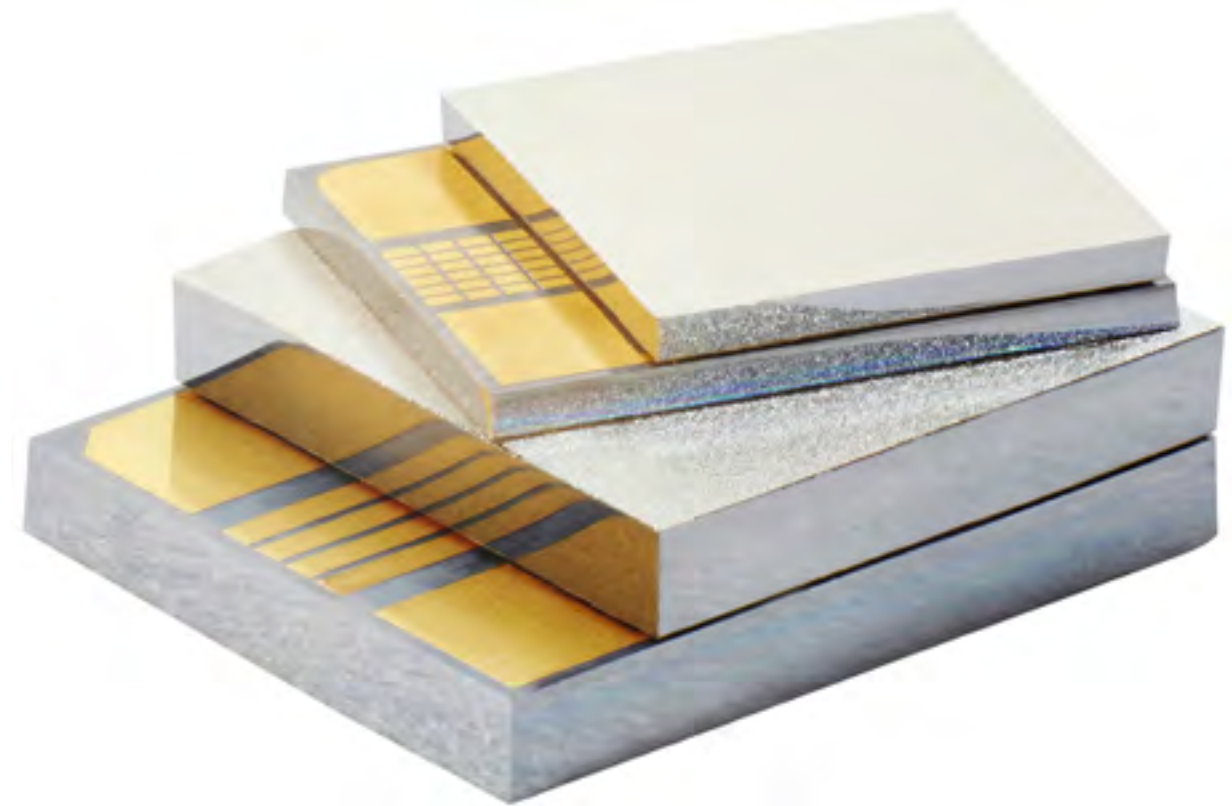
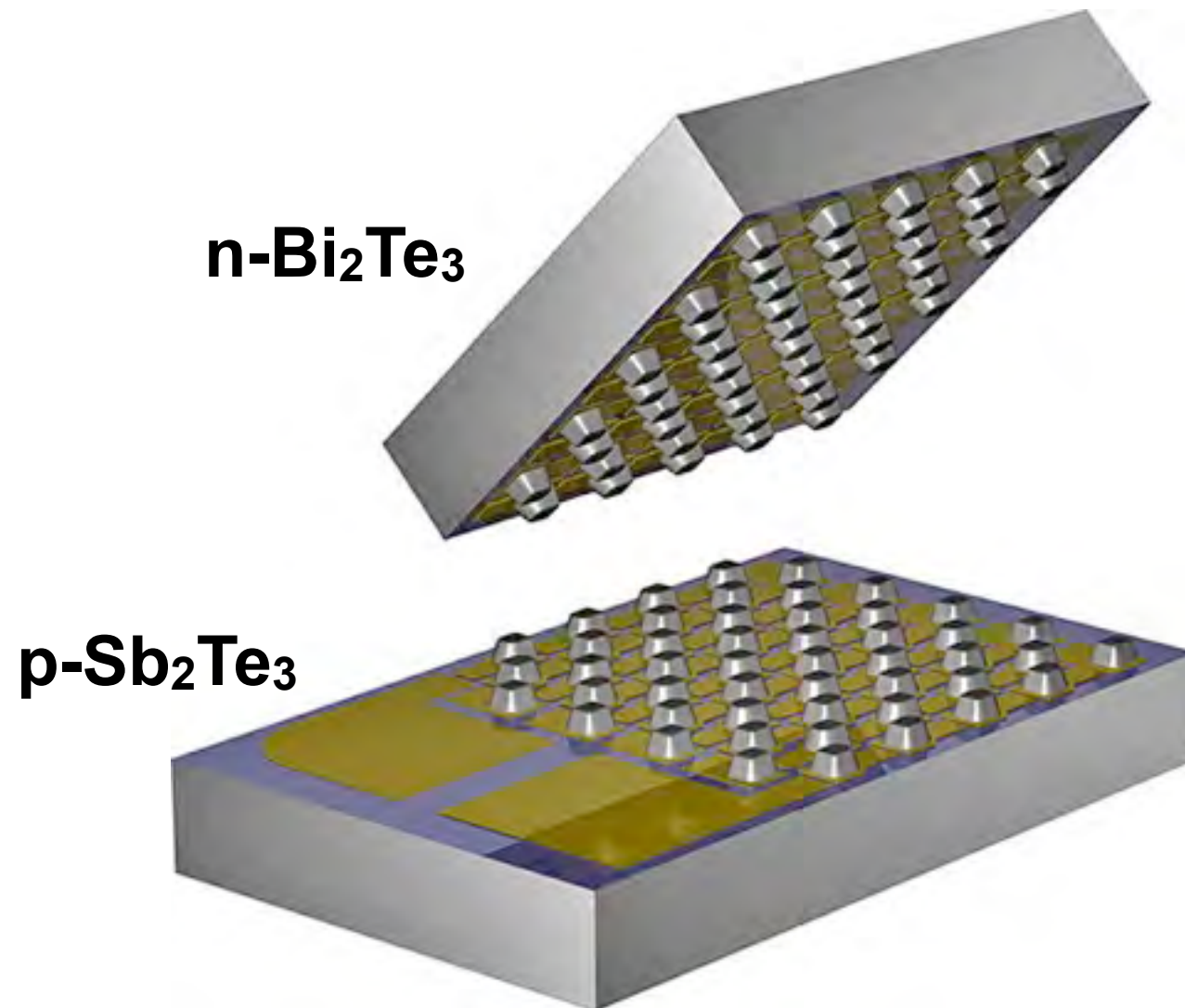


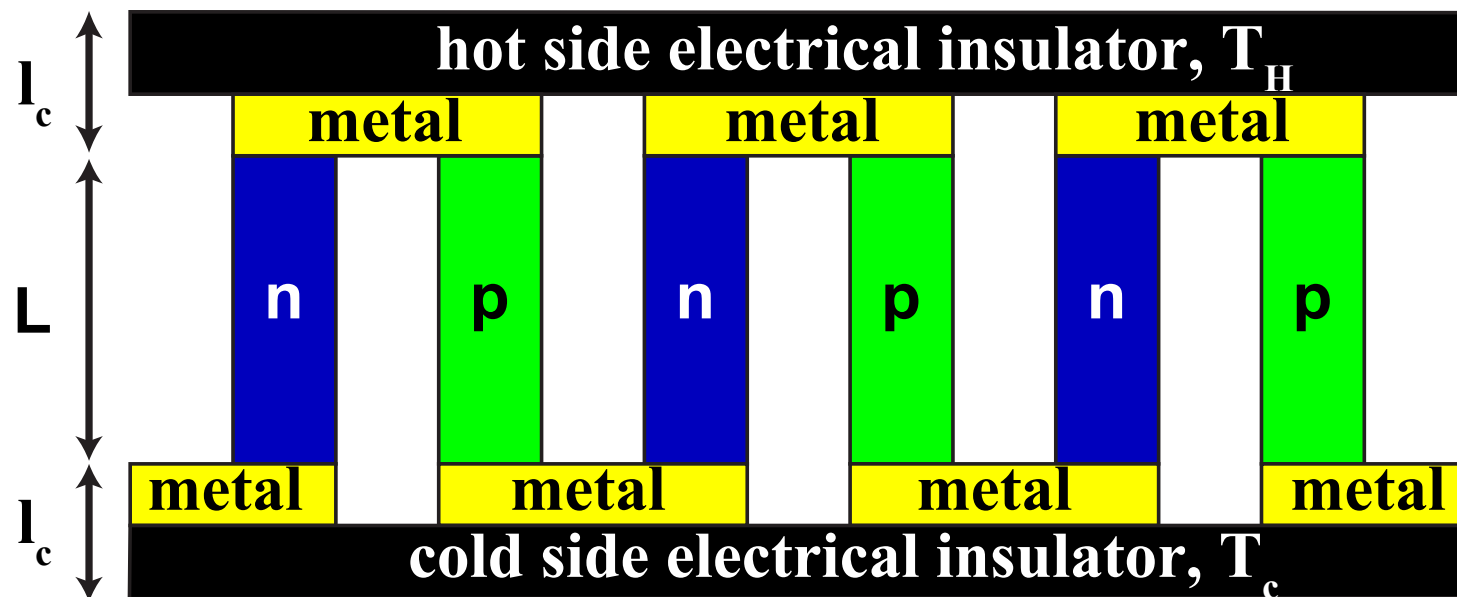
@ 300 K:

- $\sigma = 20,300 \text{ S/m}$
4 terminal
- $\kappa = 7.78 \text{ W/mK}$
- $\alpha = -271 \text{ } \mu\text{V/K}$
- $ZT = 0.057$



- ZT enhanced by x117
- $\alpha^2\sigma = 1.49 \text{ mW m}^{-1}\text{K}^{-2}$
- What enhancements with SiGe ?





A = module leg area

L = module leg length

N = number of modules

κ_c = thermal contact conductivity

ρ_c = electrical contact resistivity

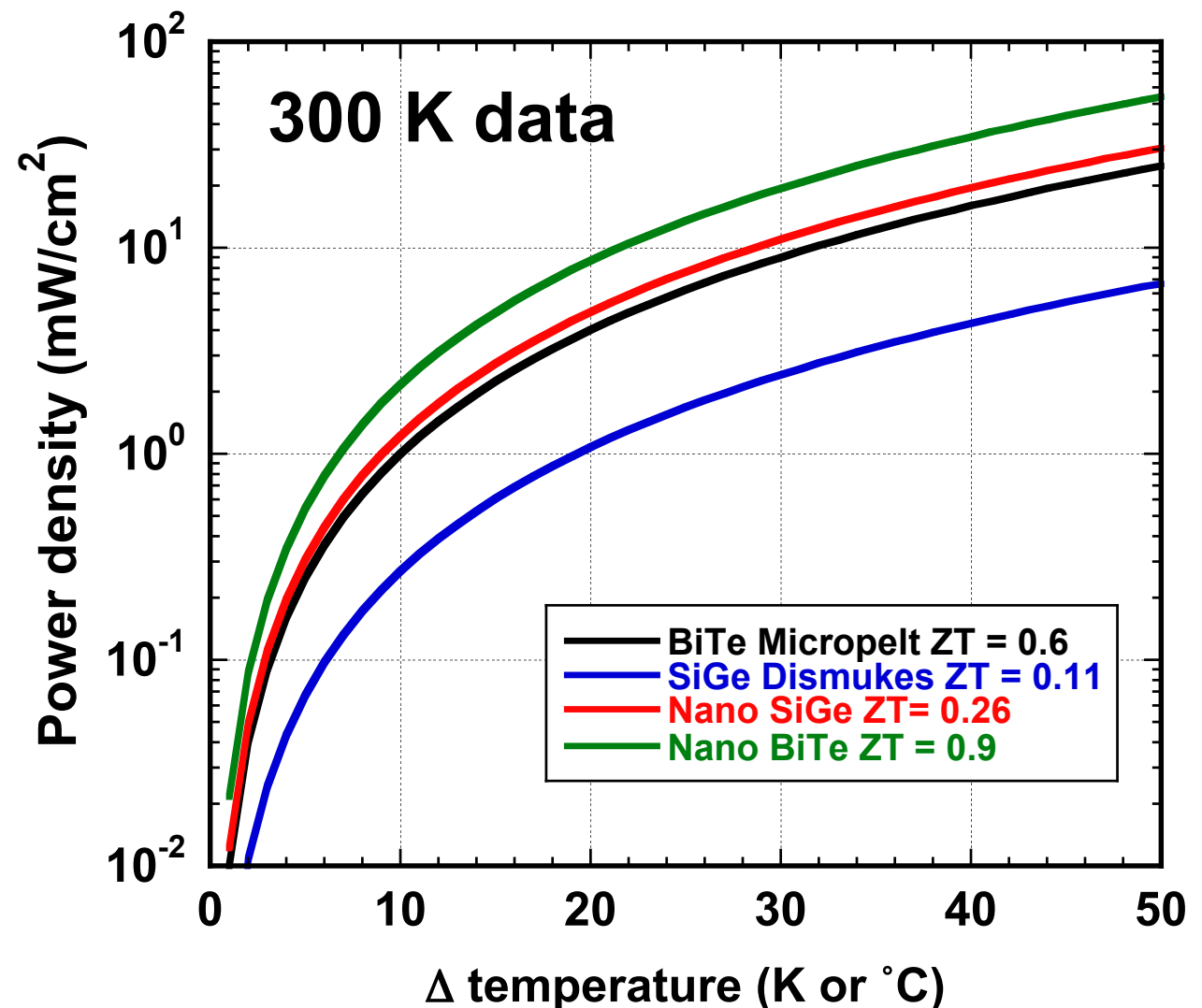
$$P = \frac{\alpha^2 \sigma A N \Delta T^2}{2(\rho_c \sigma + L) \left(1 + 2 \frac{\kappa l_c}{\kappa_c L}\right)^2}$$

D.M. Rowe & M. Gao, IEE Proc. Sci. Meas. Technol. 143, 351 (1996)

● System: power in BiTe alloys limited by Ohmic contacts

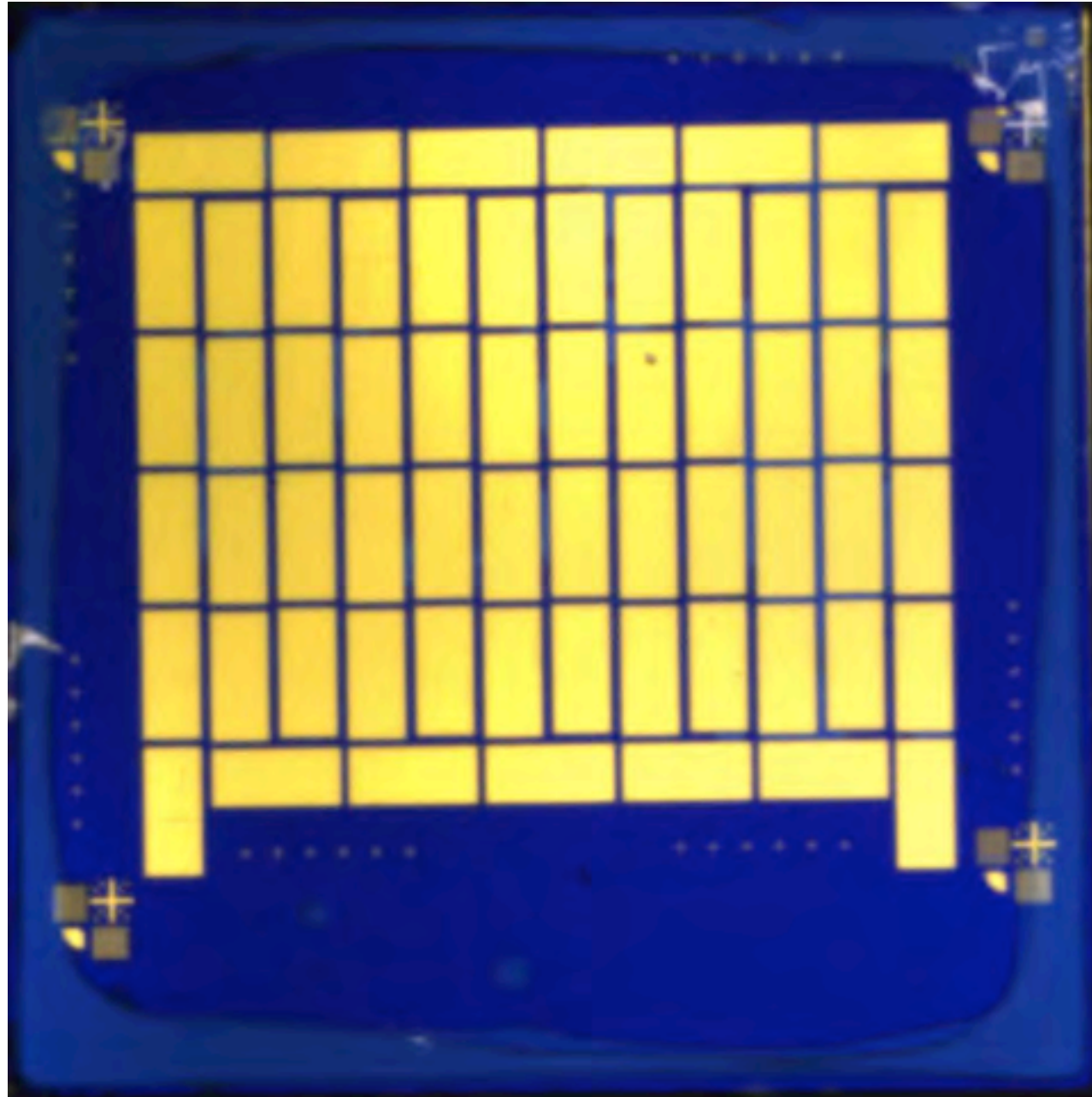
● $\rho_c (\text{Bi}_2\text{Te}_3) \cong 1 \times 10^{-7} \Omega\text{-cm}^2$

● $\rho_c (\text{Si}_{1-x}\text{Ge}_x) = 1.2 \times 10^{-8} \Omega\text{-cm}^2$

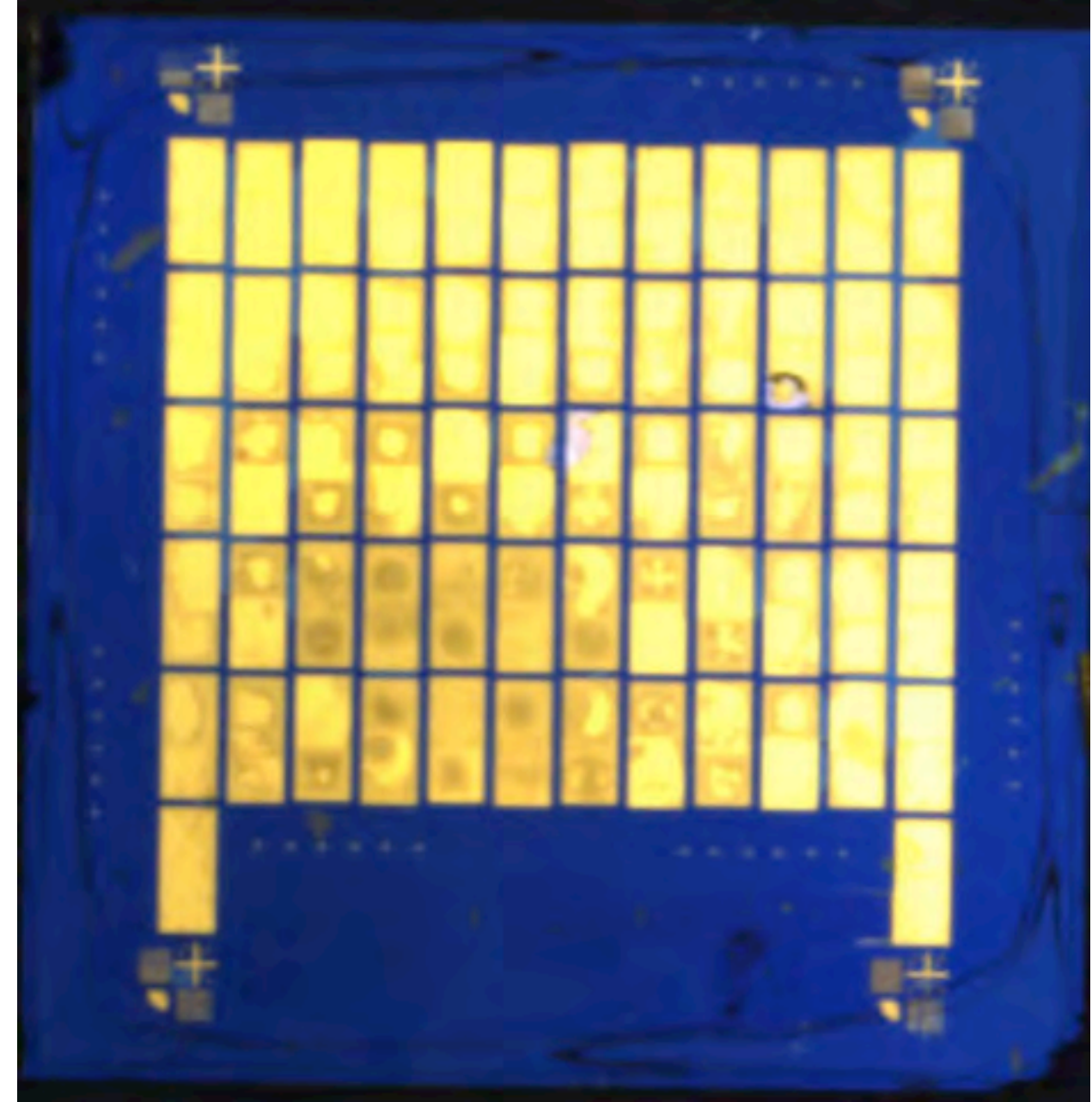


122 Leg Modules

n-type



p-type



- **Process tested and works well**
- **SOI growths now in progress for final modules**

- D.M. Rowe (Ed.), “*Thermoelectrics Handbook: Macro to Nano*” CRC Taylor and Francis (2006) ISBN 0-8494-2264-2
- G.S. Nolas, J. Sharp and H.J. Goldsmid “*Thermoelectrics: Basic Principles and New Materials Development*” (2001) ISBN 3-540-41245-X
- M.S. Dresselhaus et al. “*New directions for low-dimensional thermoelectric materials*” Adv. Mat. 19, 1043 (2007)
- D.J. Paul, “*Thermoelectric Energy Harvesting*” Intech Open Access from “ICT - Energy - Concepts Towards Zero - Power Information & Communication Technology ” (2014) - DOI: [10.5772/57347](https://doi.org/10.5772/57347)

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Tel:- +44 141 330 5219

<http://userweb.eng.gla.ac.uk/douglas.paul/index.html>

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<http://www.greensilicon.eu/GREENSilicon/index.html>