

**Prof Douglas J. Paul**  
**School of Engineering**  
**University of Glasgow**

**[Douglas.Paul@glasgow.ac.uk](mailto:Douglas.Paul@glasgow.ac.uk)**



- **An overview of some applications needing energy harvesting**
- **How to convert thermal energy into electricity through thermoelectric generation**
- **The amount of energy available from the sun at different points on the planet**
- **How photovoltaic solar cells generate electricity**
- **What is the optimum absorption wavelength**
- **How can we maximise PV electricity generation efficiency**



## Cars: replace alternator



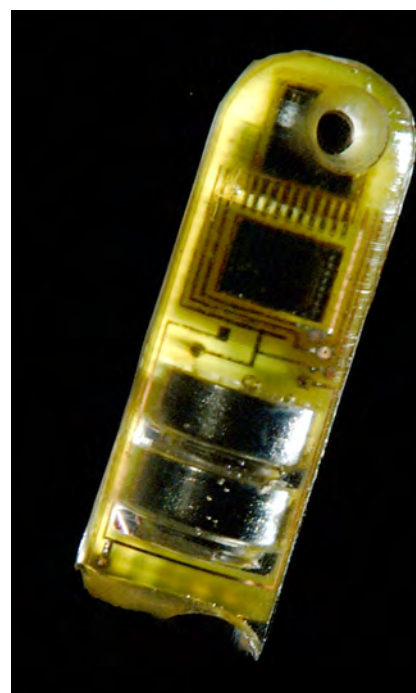
## Solar powered road signs



## Trains: Vibrations powering sensors



## Temperature control for CO<sub>2</sub> sequestration



## Battery free autonomous sensors: ECG, blood pressure, etc.





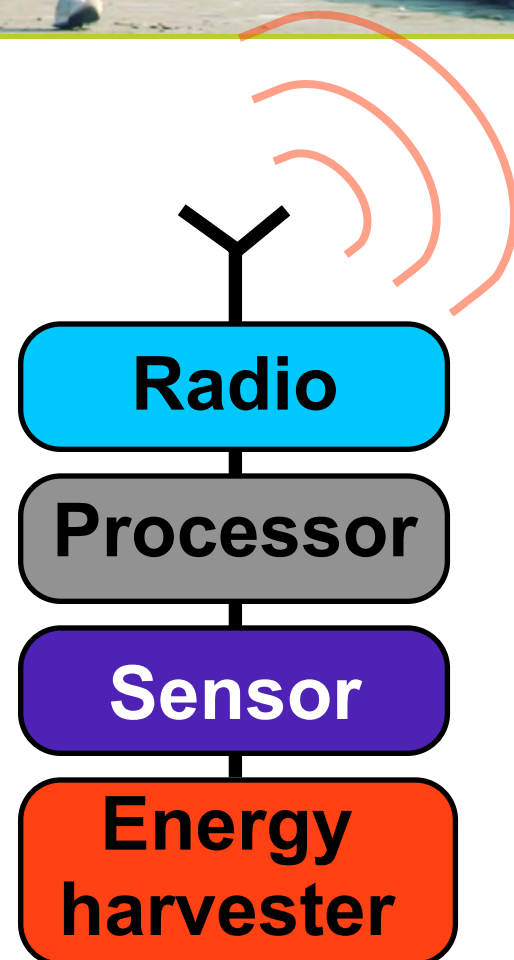
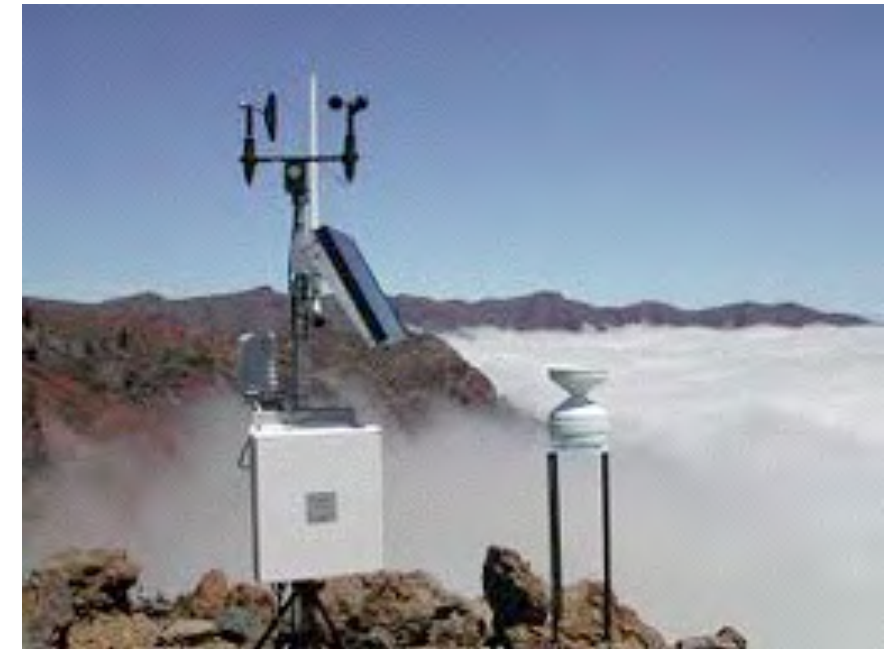
## Sports performance sensors



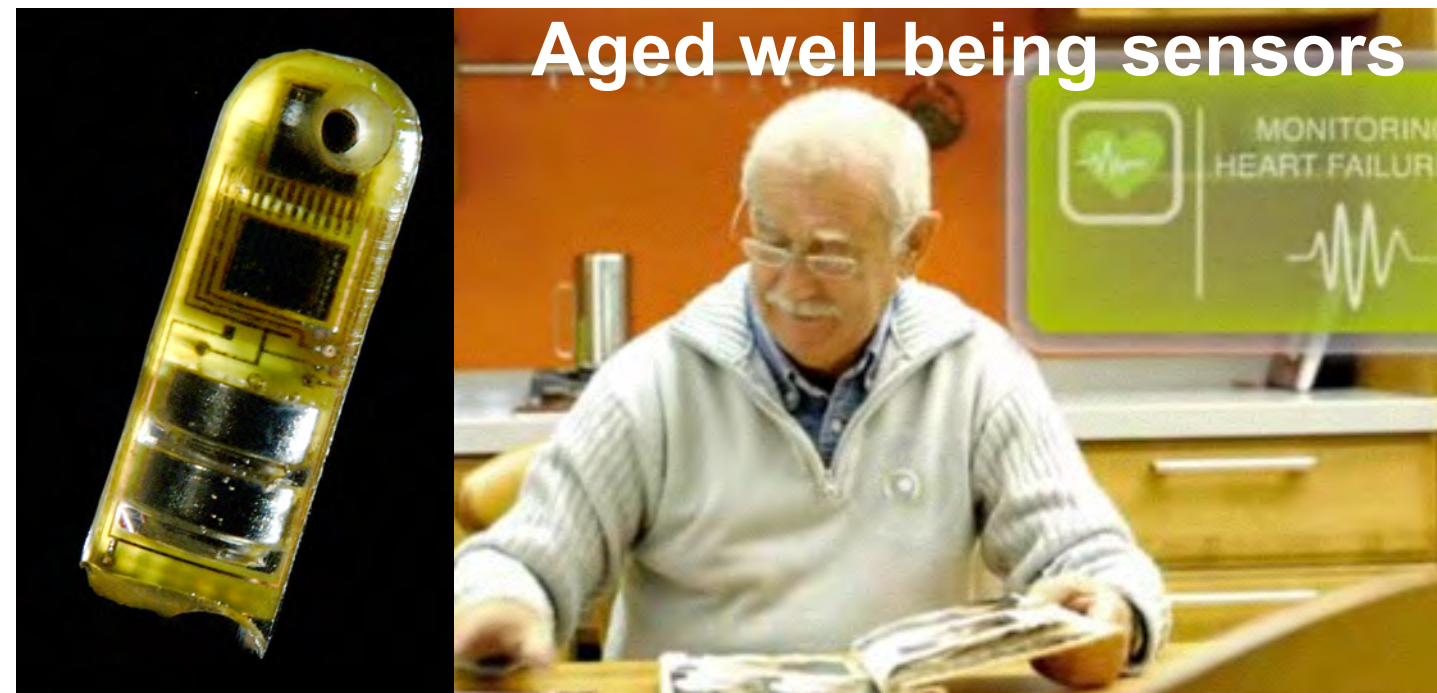
## Flood sensors



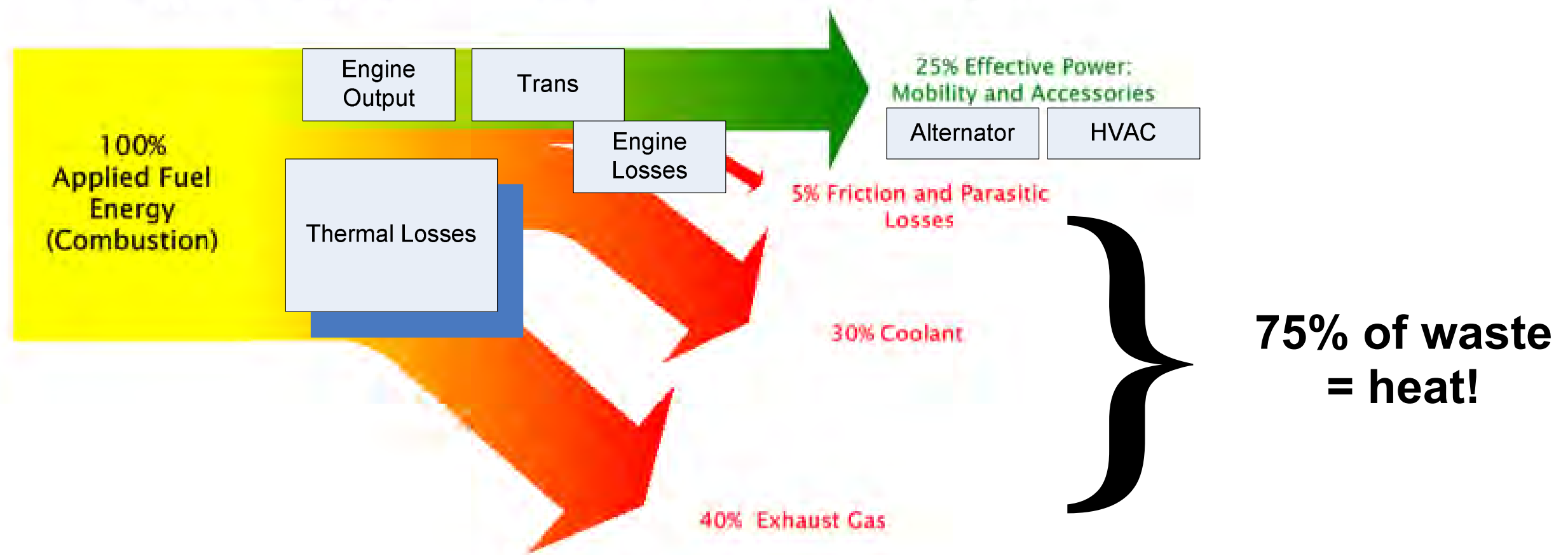
## Weather monitoring



## Aged well being sensors



**Battery free autonomous sensors: ECG, blood pressure, etc.**



**Fuel consumption  $\propto \eta_{\text{powertrain}}$  (kinetic energy + amenities energy)**

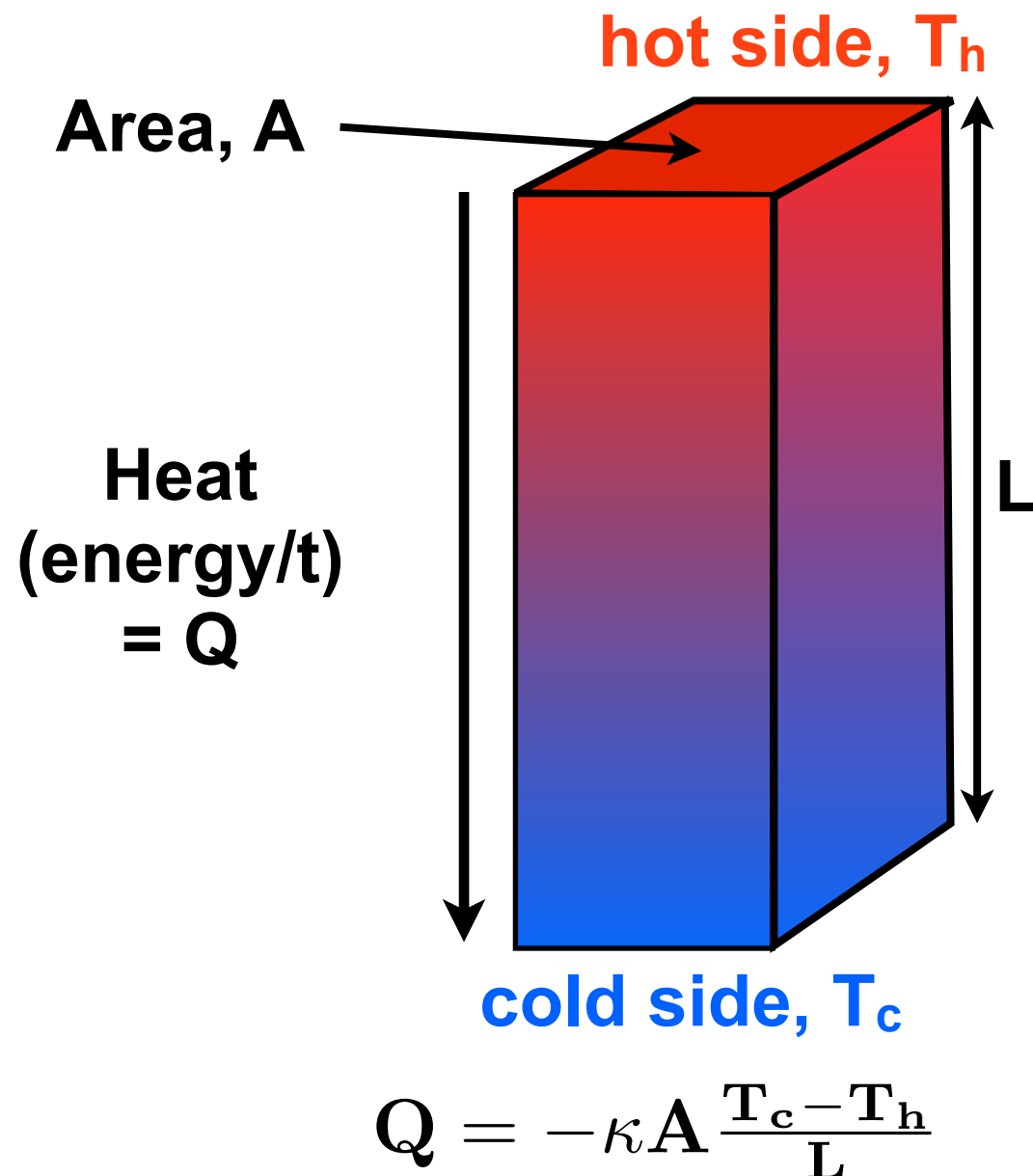
## Thermoelectrics in Cars:

- Use waste heat energy (45% of fuel!)
- Can reduce fuel consumption  $\leq 5\%$
- Provide efficient local cooling



## Fourier thermal transport

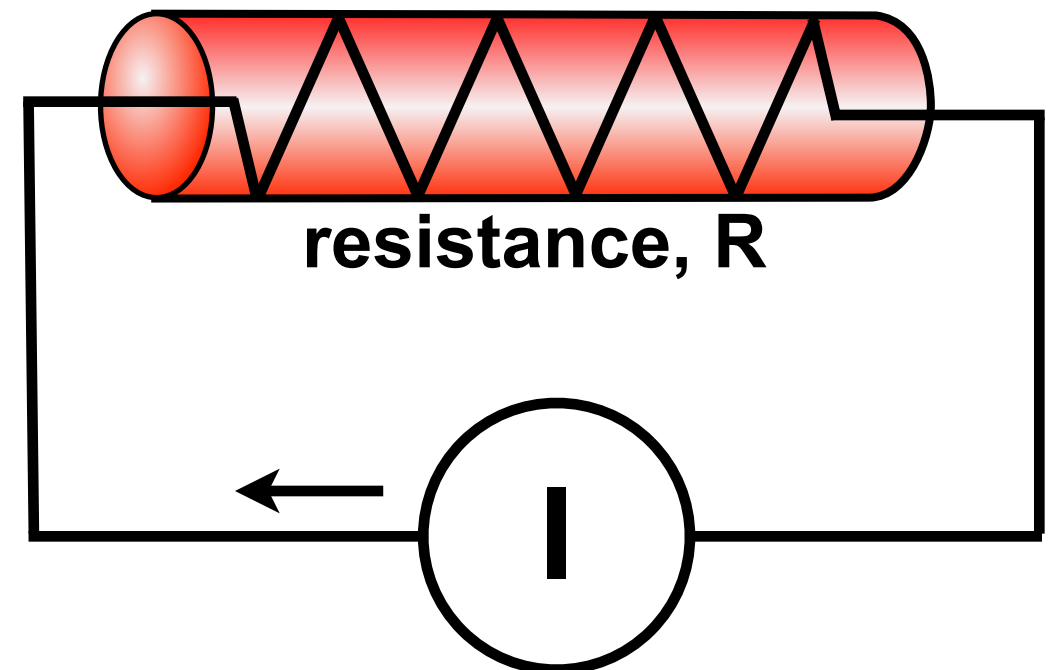
$$Q = -\kappa A \nabla T$$



## Joule heating

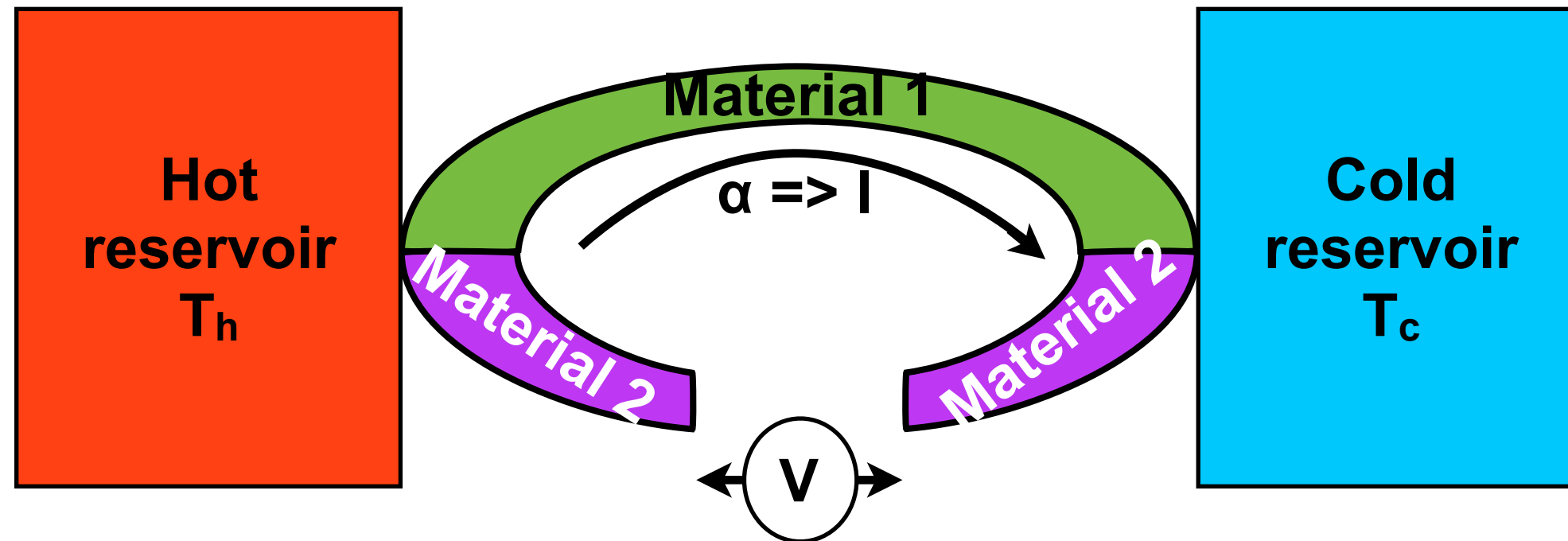
$$Q = I^2 R$$

$Q$  = heat (power i.e energy / time)





# The Seebeck Effect



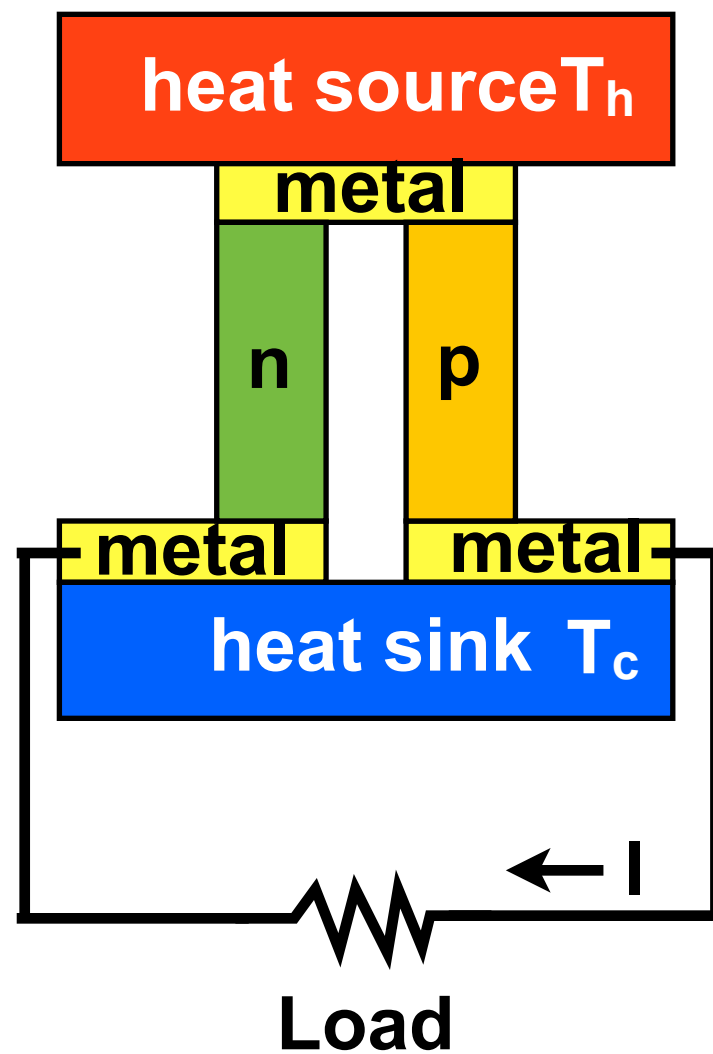
- Open circuit voltage,  $V = \alpha (T_h - T_c) = \alpha \Delta T$

Seebeck coefficient,  $\alpha = \frac{dV}{dT}$

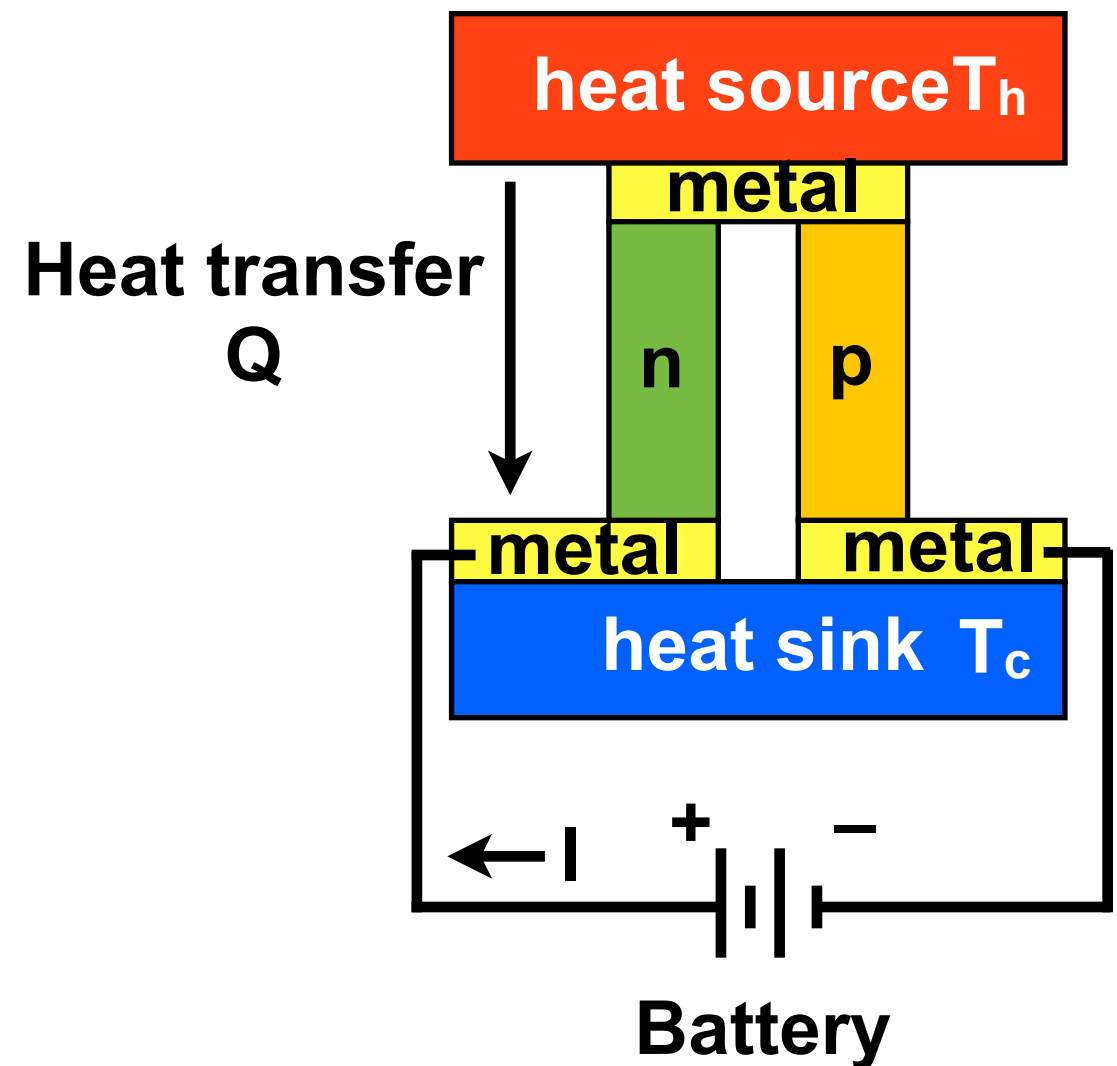
units: V/K

- Seebeck coefficient =  $\frac{1}{q}$  x entropy  $\left(\frac{Q}{T}\right)$  transported with electron

**Seebeck effect:  
electricity  
generation**



**Peltier effect:  
electrical cooling  
i.e. heat pump**





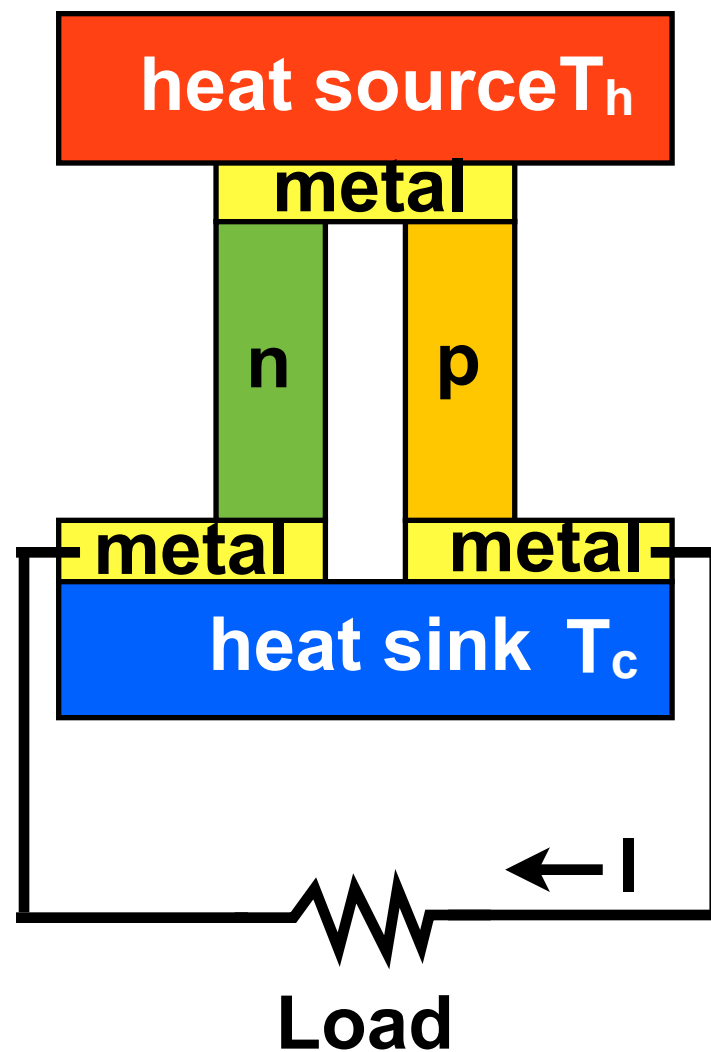
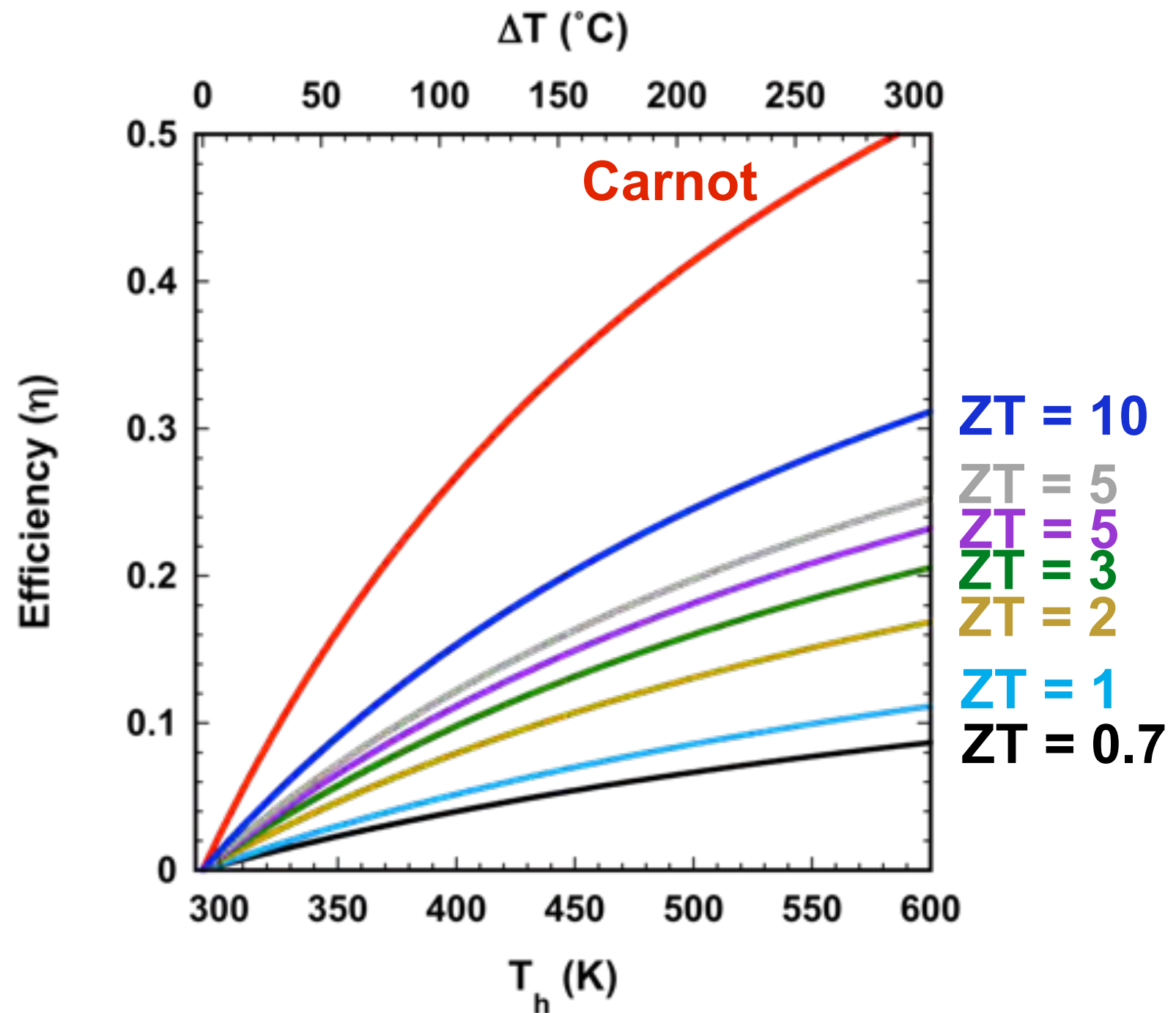


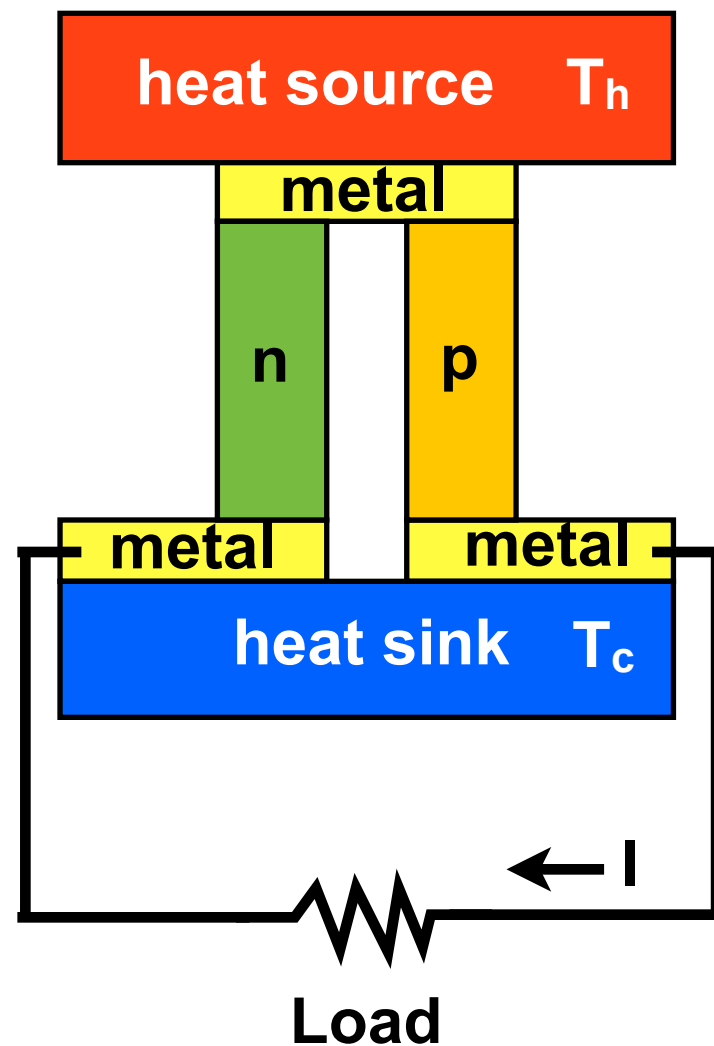
Figure of merit

$$ZT = \frac{\alpha^2 \sigma}{\kappa} T$$

$$\eta = \frac{\Delta T}{T_h} \frac{\sqrt{1+ZT}-1}{\sqrt{1+ZT}+\frac{T_c}{T_h}}$$

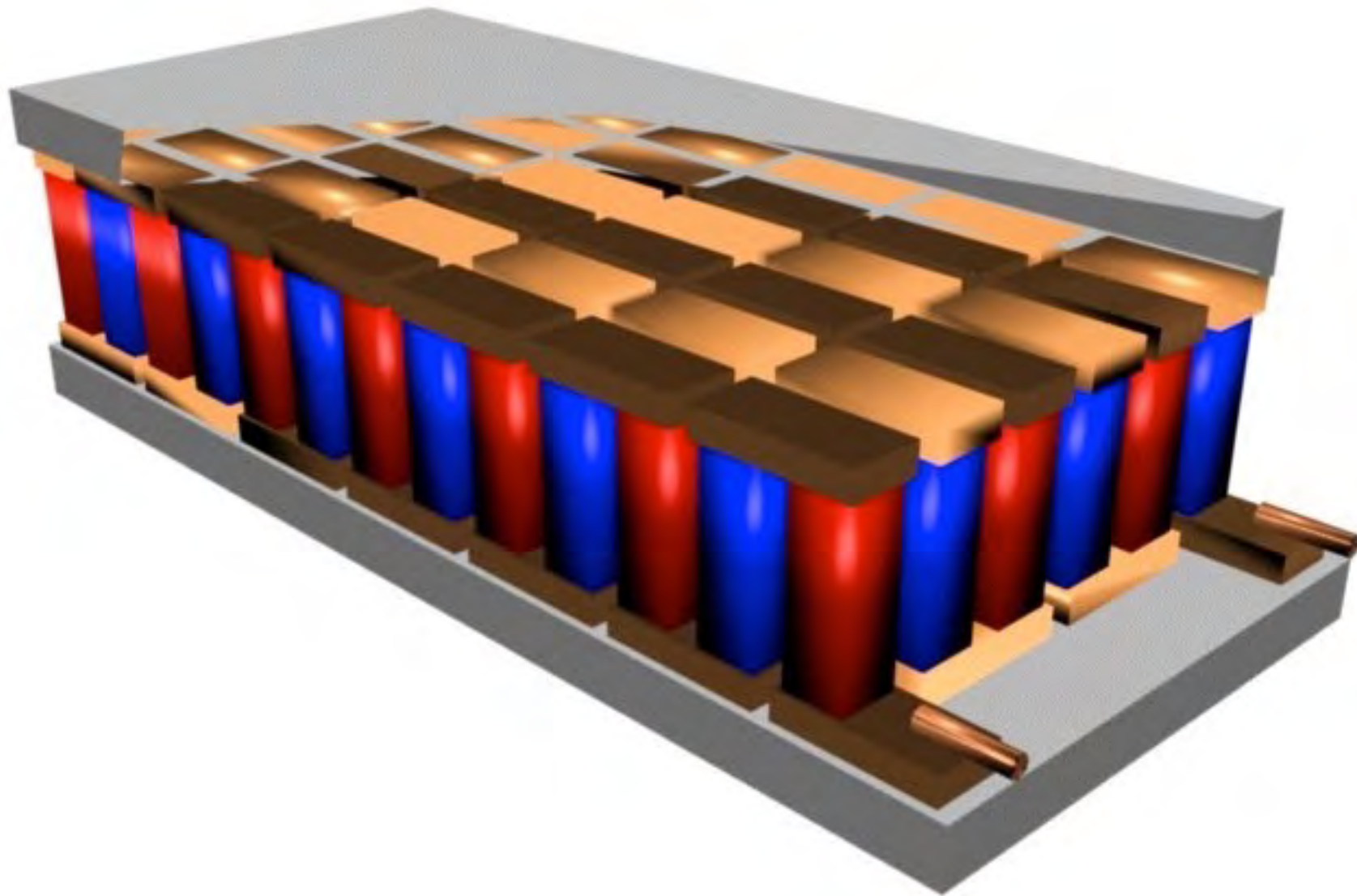


## Module

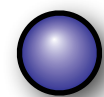


$\sim 0.2 \text{ mV}$

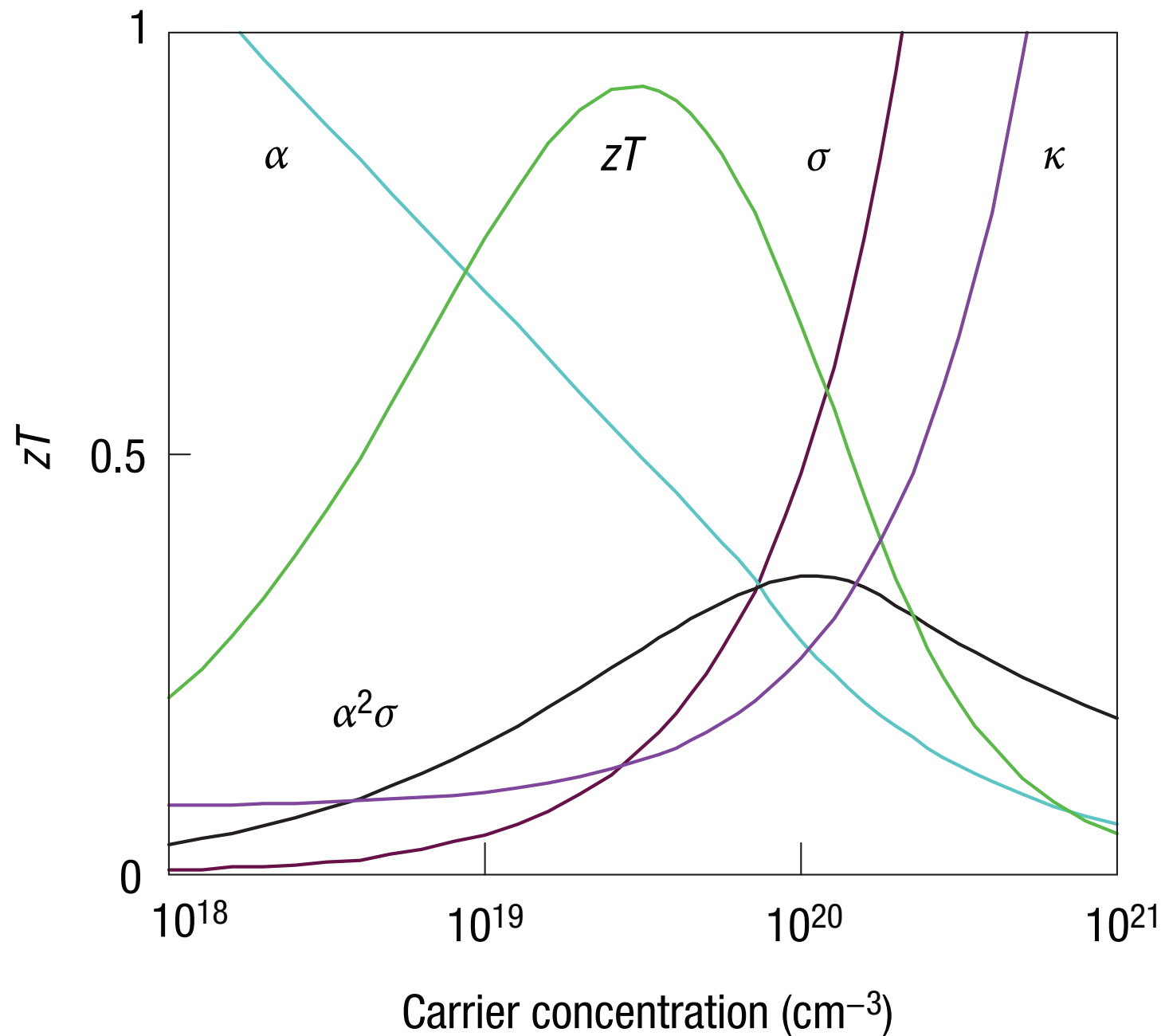
## Generator



$> 1 \text{ V}$



Modules stacked electrically in series,  
thermally in parallel to get useful  $I$  &  $V$

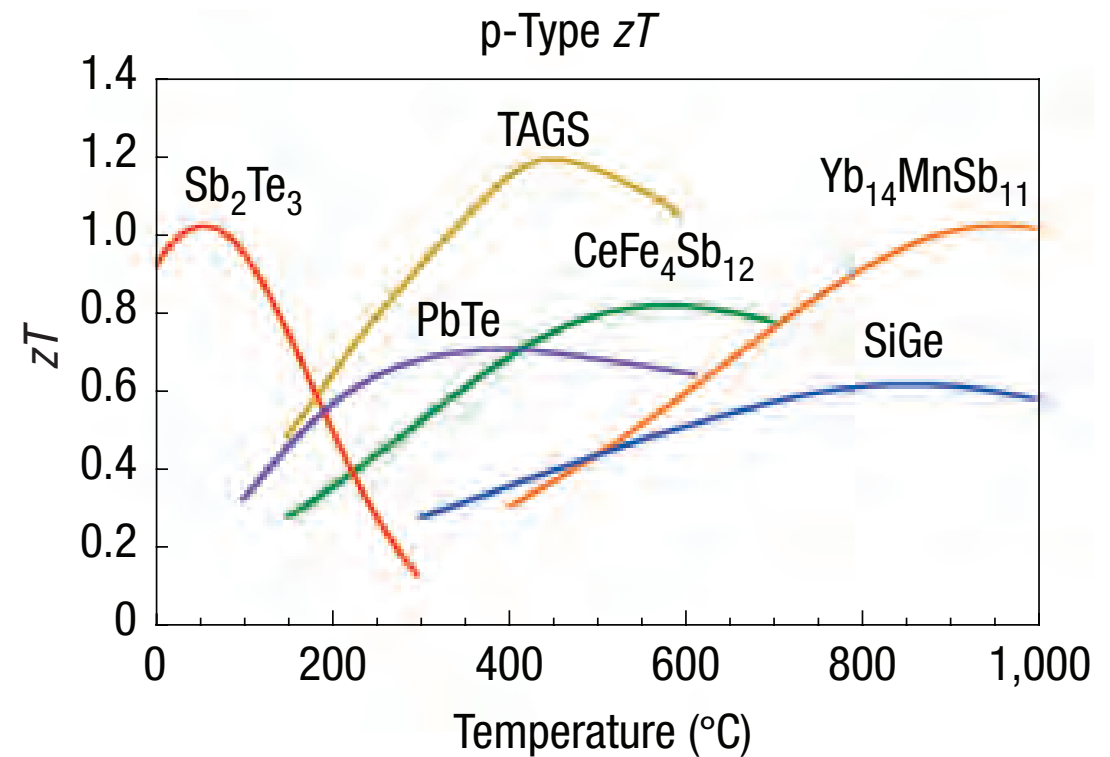
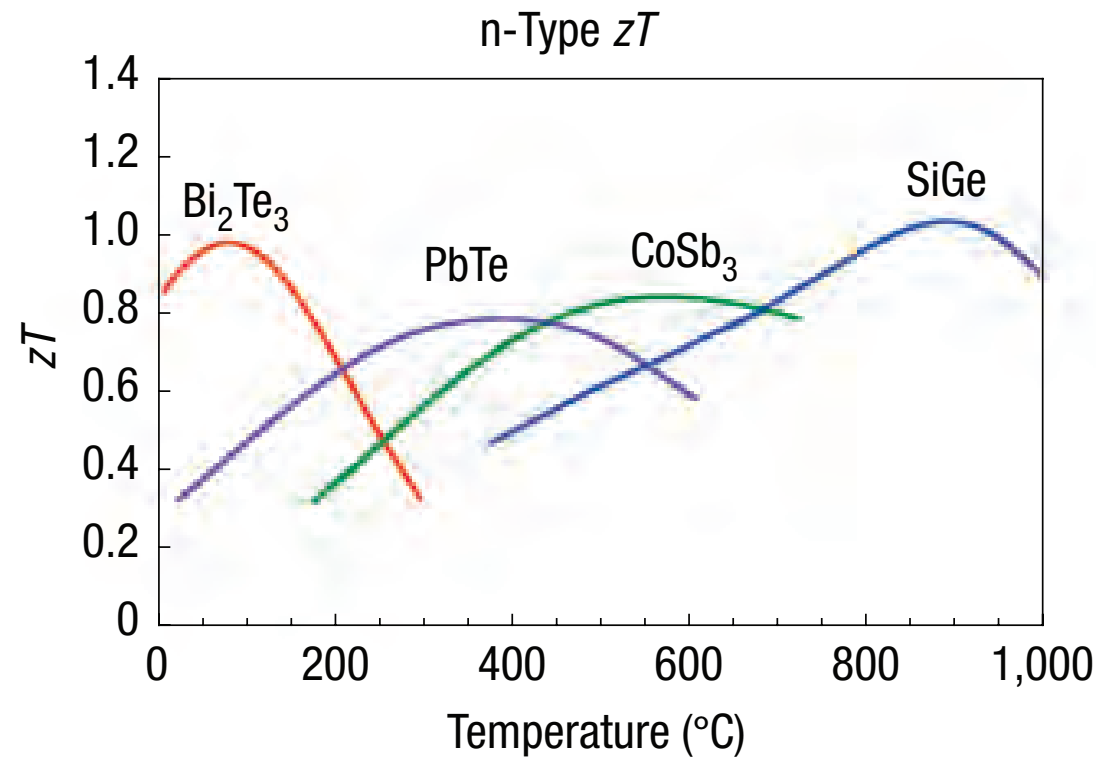


● Maximum ZT requires compromises with  $\alpha$ ,  $\sigma$  &  $\kappa$

● Limited by Wiedemann-Franz Law

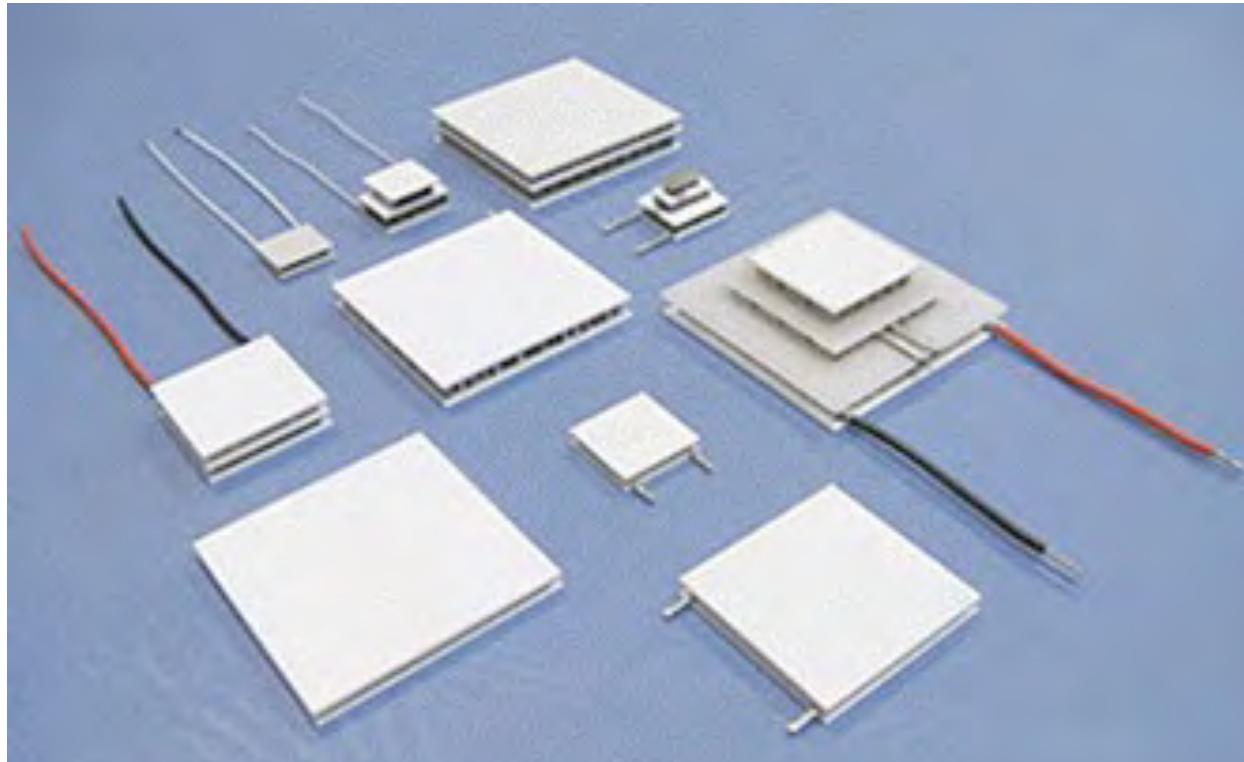
● Maximum ZT ~ 1 at ~100 °C



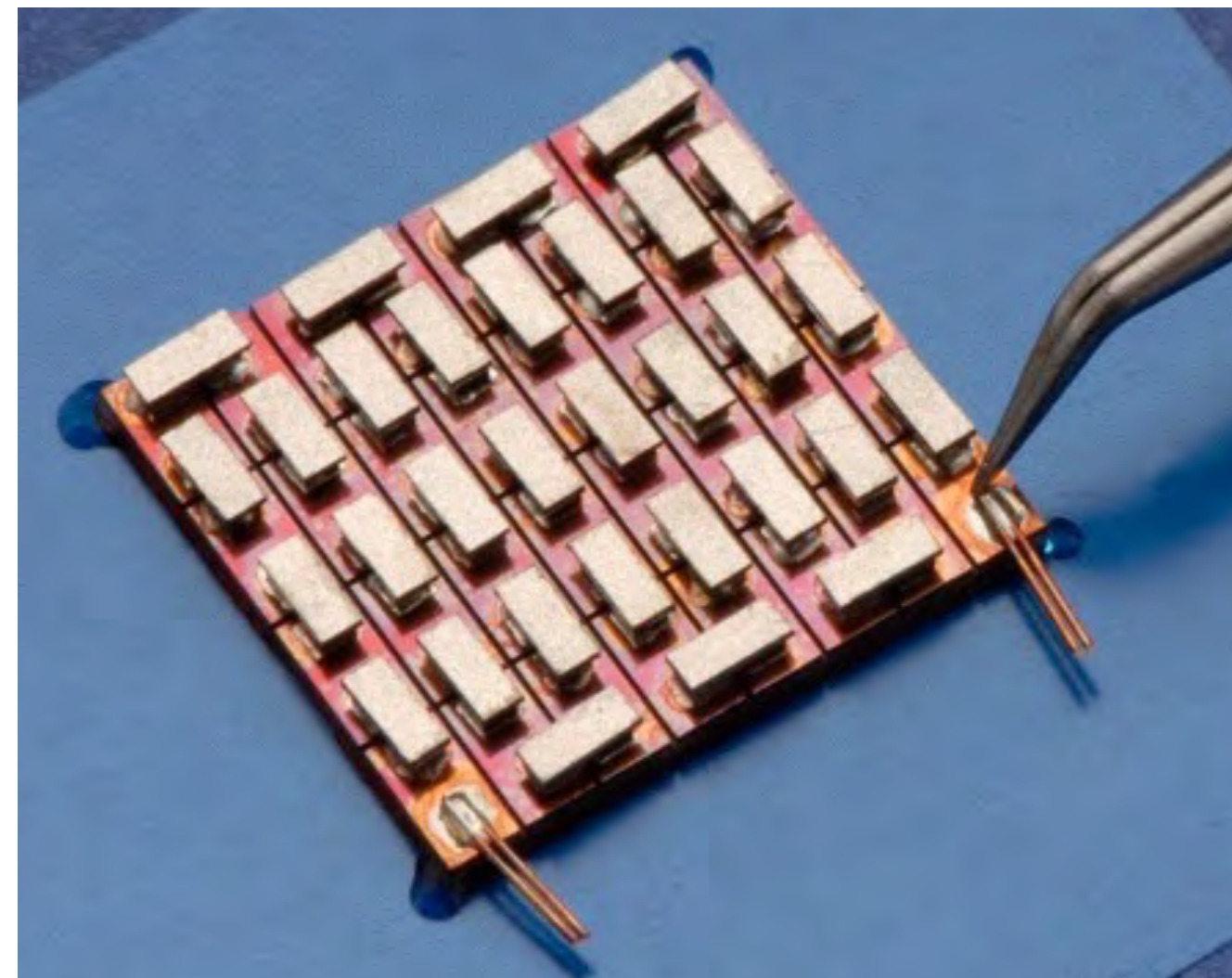
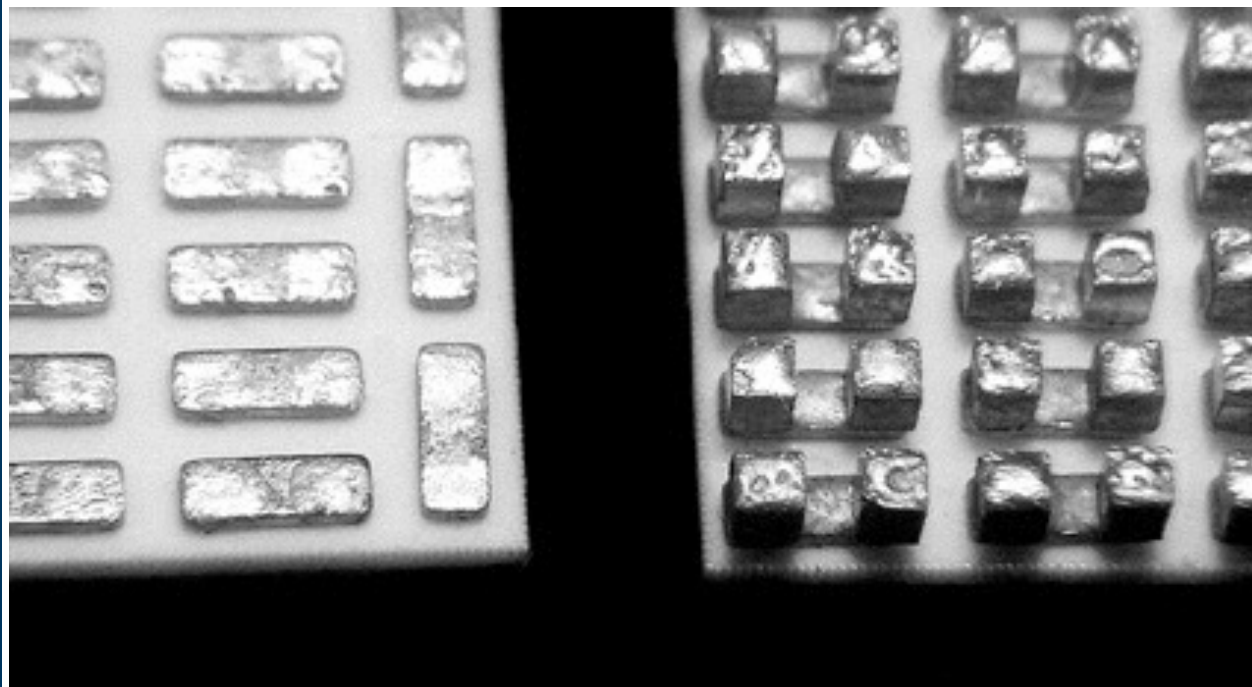


*Nature Materials 7, 105 (2008)*

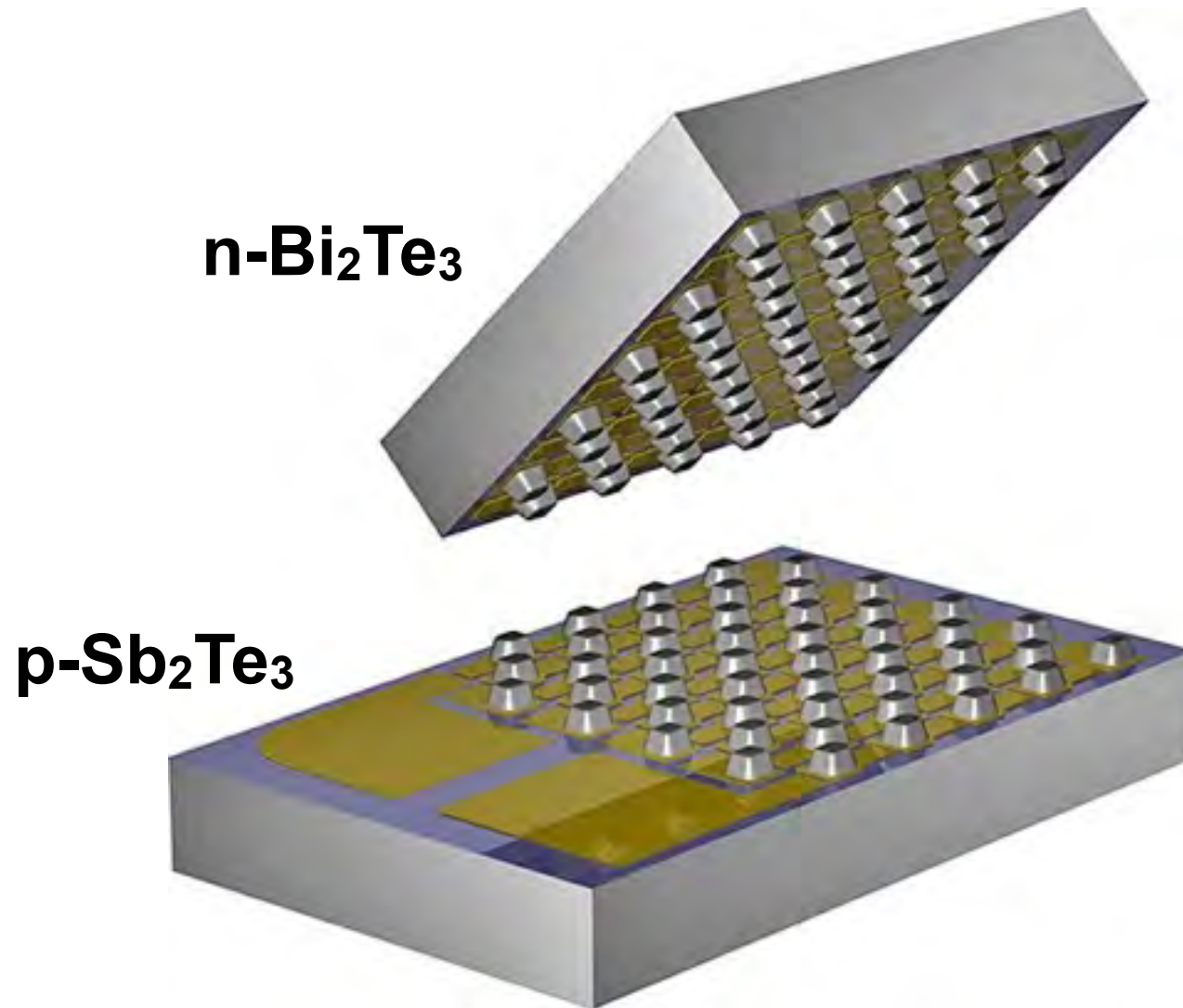
- Bulk n- $\text{Bi}_2\text{Te}_3$  and p- $\text{Sb}_2\text{Te}_3$  used in most commercial thermoelectrics & Peltier coolers
- But tellurium is 8<sup>th</sup> rarest element on earth !!!
- Bulk  $\text{Si}_{1-x}\text{Ge}_x$  ( $x \sim 0.2$  to  $0.3$ ) used for high temperature satellite applications



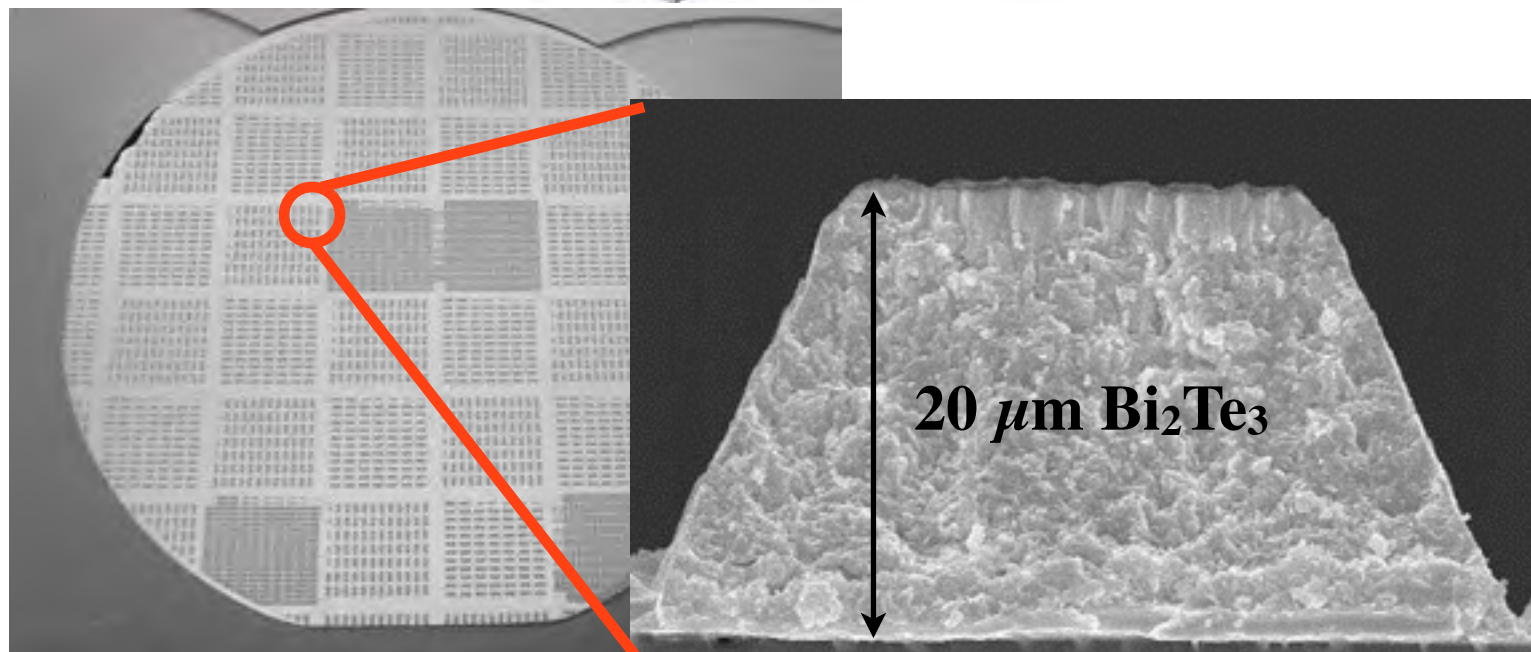
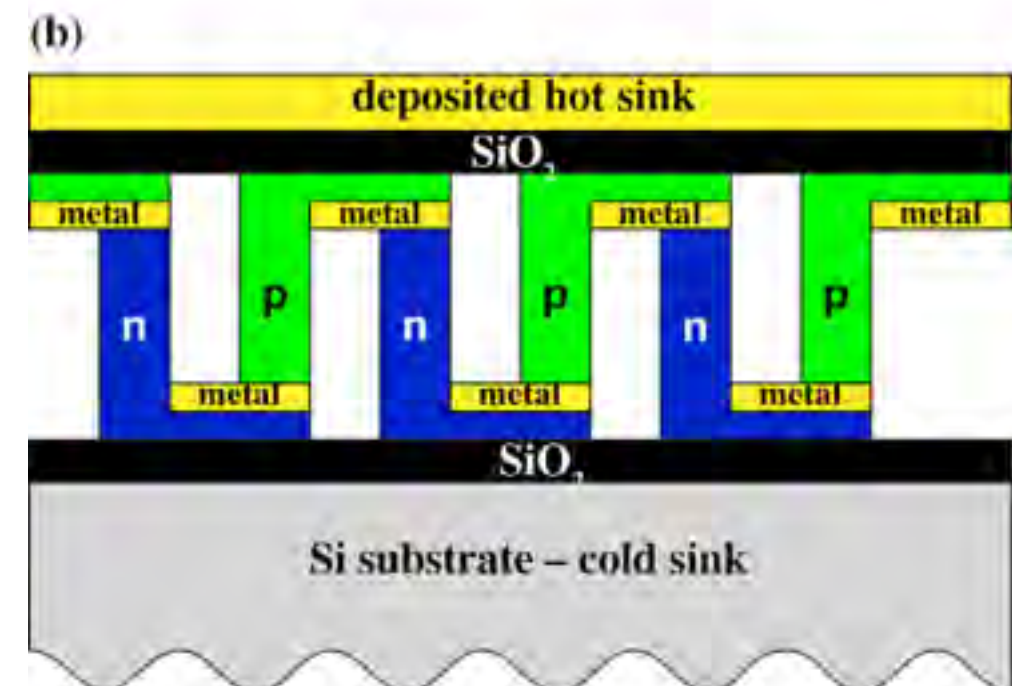
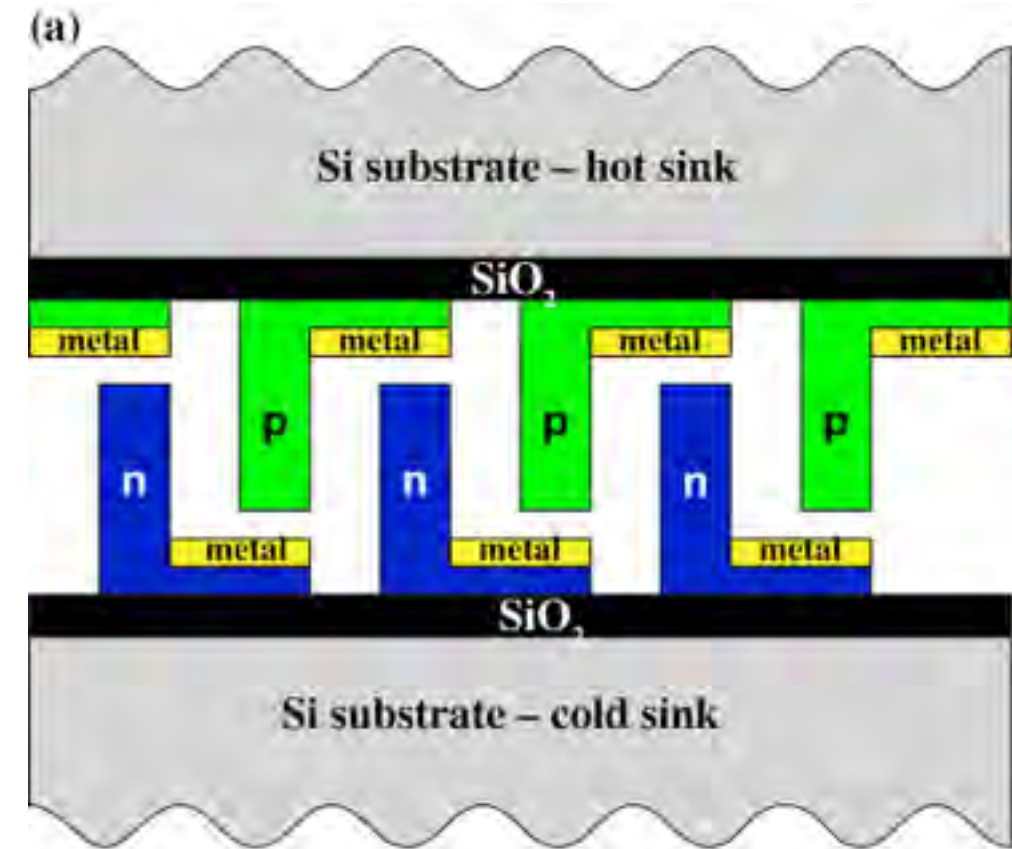
**Bulk  $n\text{-Bi}_2\text{Te}_3$  and  $p\text{-Sb}_2\text{Te}_3$  devices**



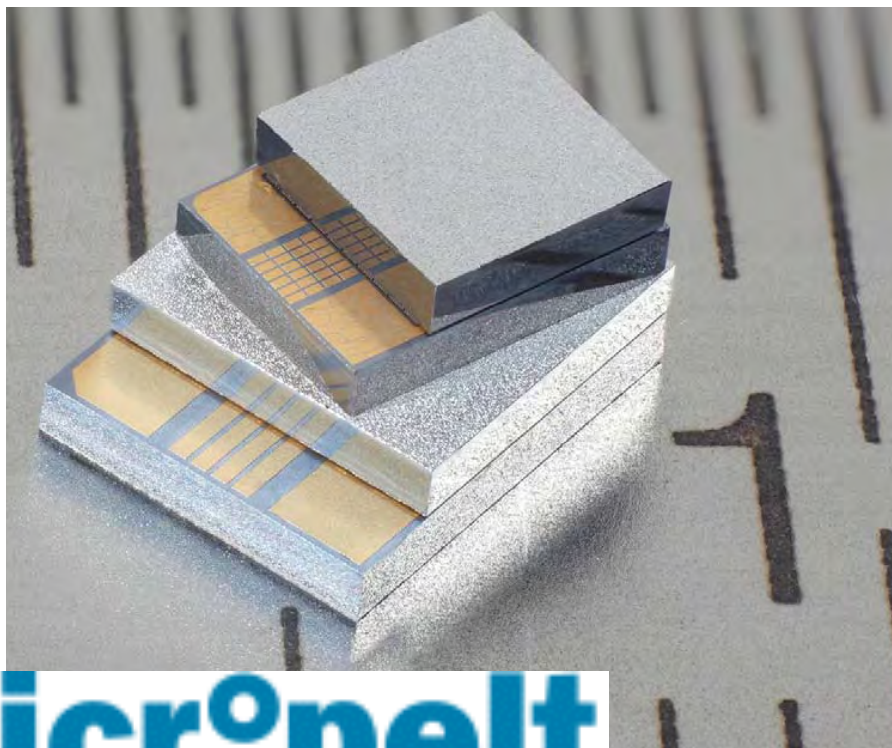
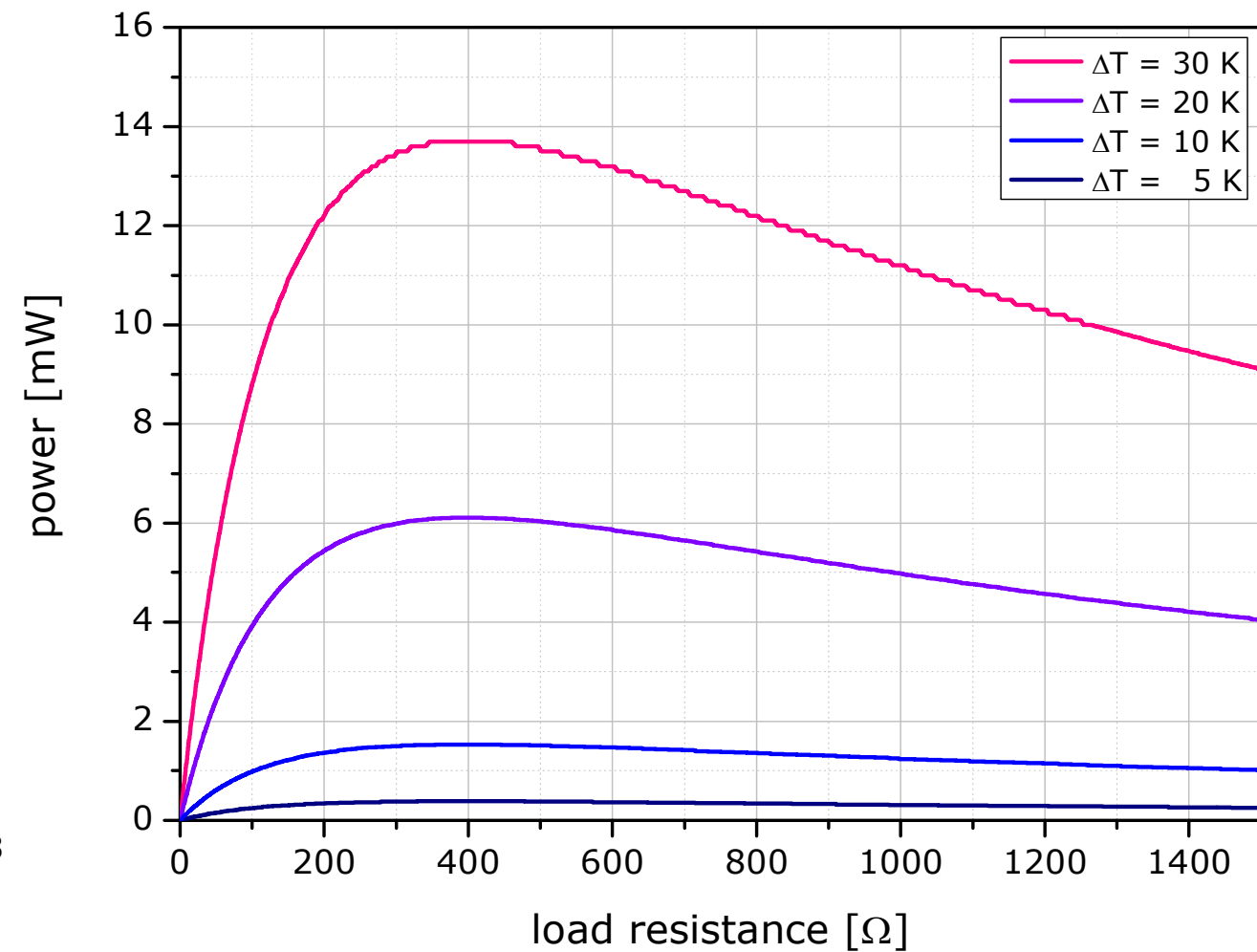
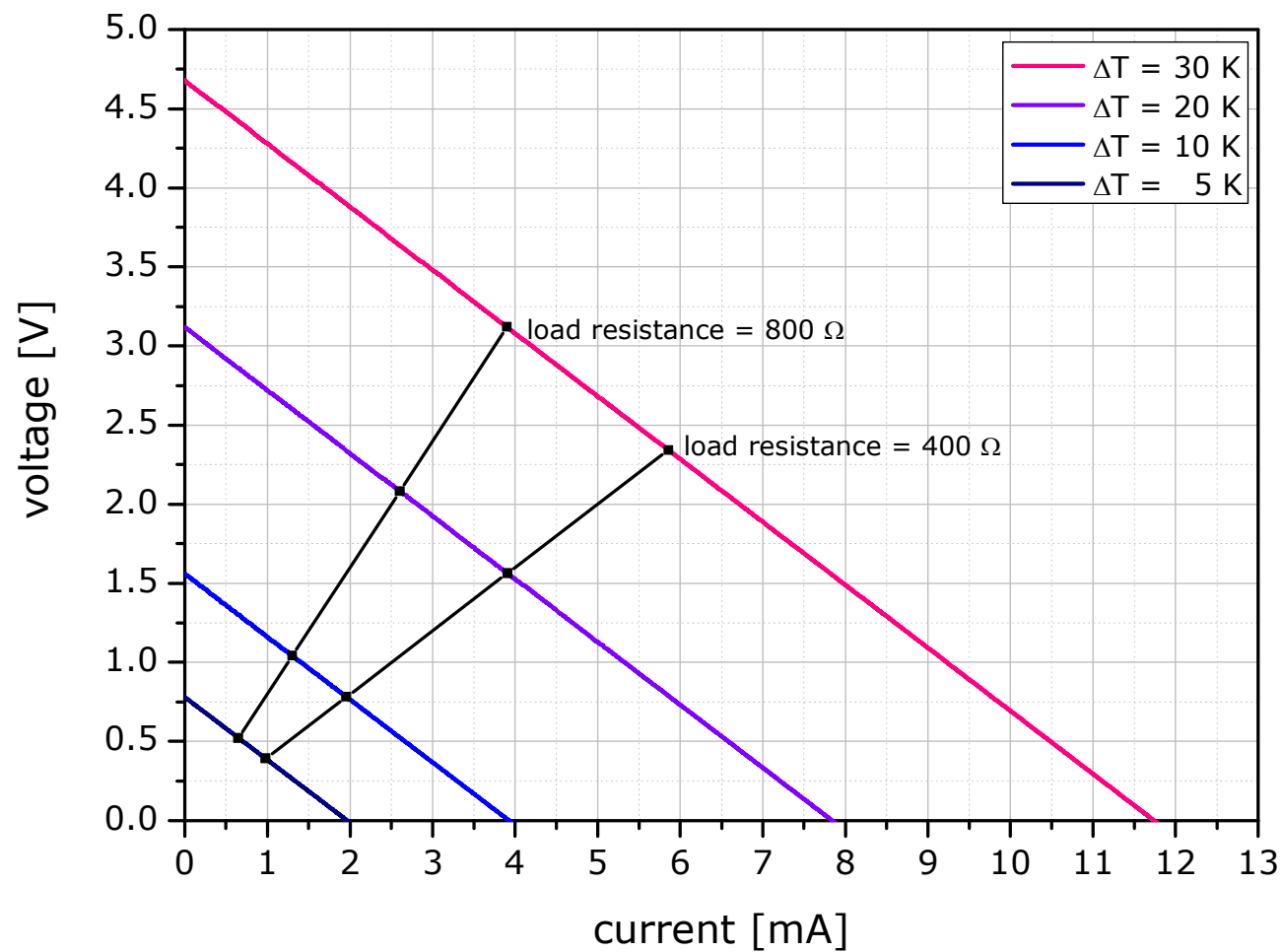




## Vertical Generator

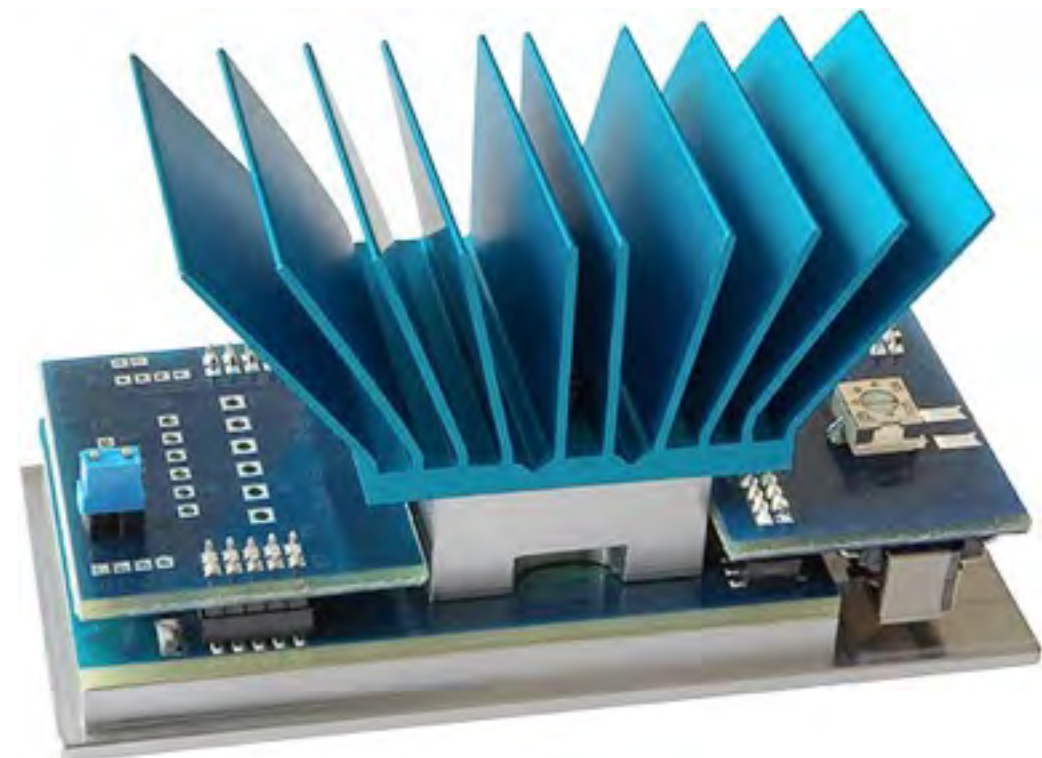






**micropelt**

**3.4 x 3.4 mm**



- The sun is an abundant source of “clean” energy
- Photovoltaic cells absorb photons and convert them into dc electricity through the creation of electron-hole pairs



## Questions:

- How much solar energy is available to use?
- What is the optimum absorption wavelength?
- How can we maximise the electricity generation efficiency?
- Can we make photovoltaic cells which are economically competitive with other energy sources?

- A black body emits photons with a distribution of energies  $= h\nu$  determined by the objects characteristic temperature  $T$

$h$  = Planck's constant,  $\nu$  = frequency,  $\lambda$  = wavelength

$$E = h\nu \qquad \lambda = \frac{c}{\nu} \qquad E = \frac{hc}{\lambda}$$

- Equilibrium photon energy density (i.e. per unit volume)

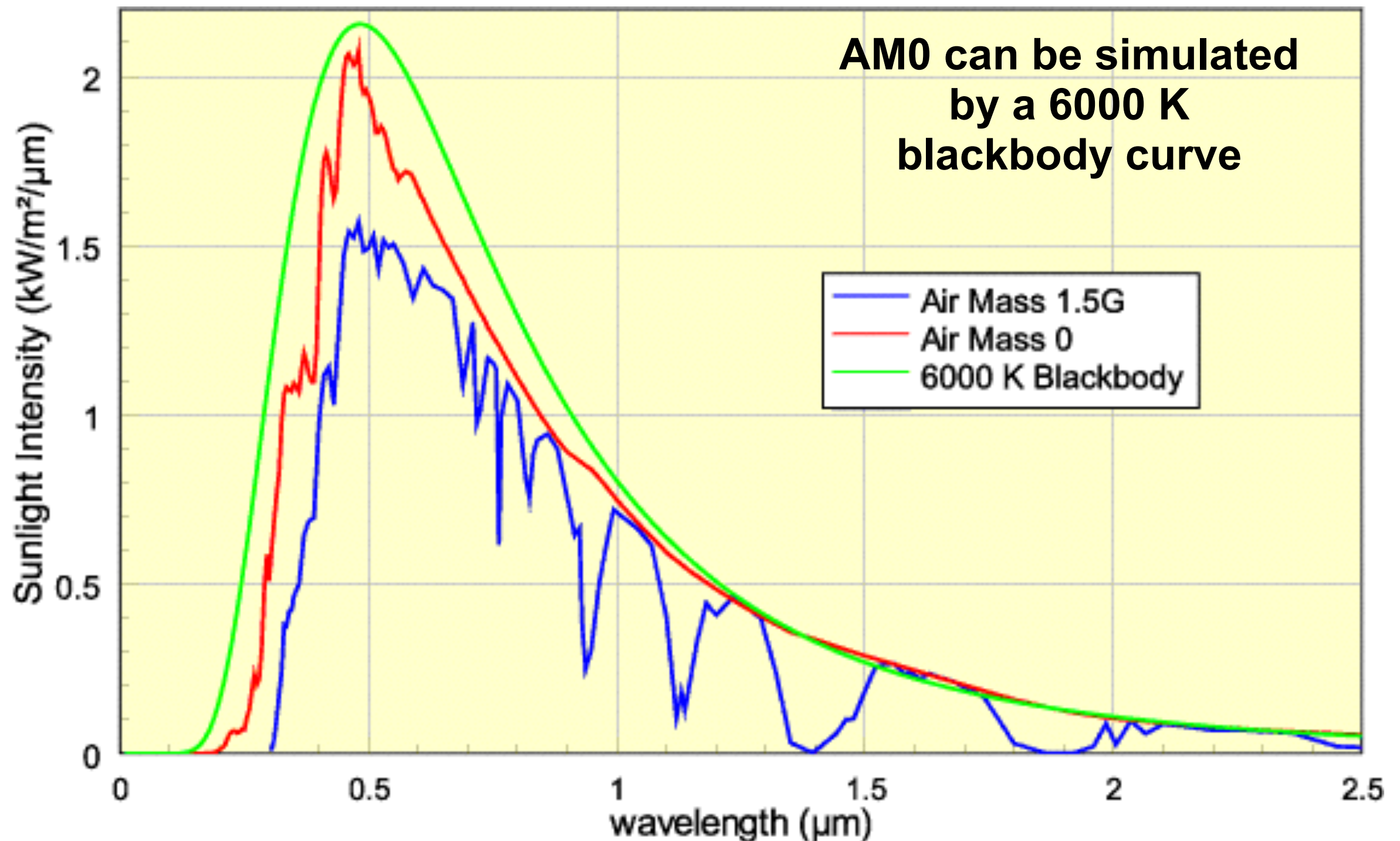
$$\rho(h\nu) = \frac{8\pi h\nu^3}{c^3 [\exp(\frac{h\nu}{k_B T}) - 1]}$$

- The particle or energy flux emitted by a blackbody per unit surface area of a hemisphere over energy range  $E_1$  to  $E_2$  is

$$N(E) = \frac{2\pi}{h^3 c} \int_{E_1}^{E_2} \frac{E^2}{[\exp(\frac{E}{k_B T}) - 1]} dE$$

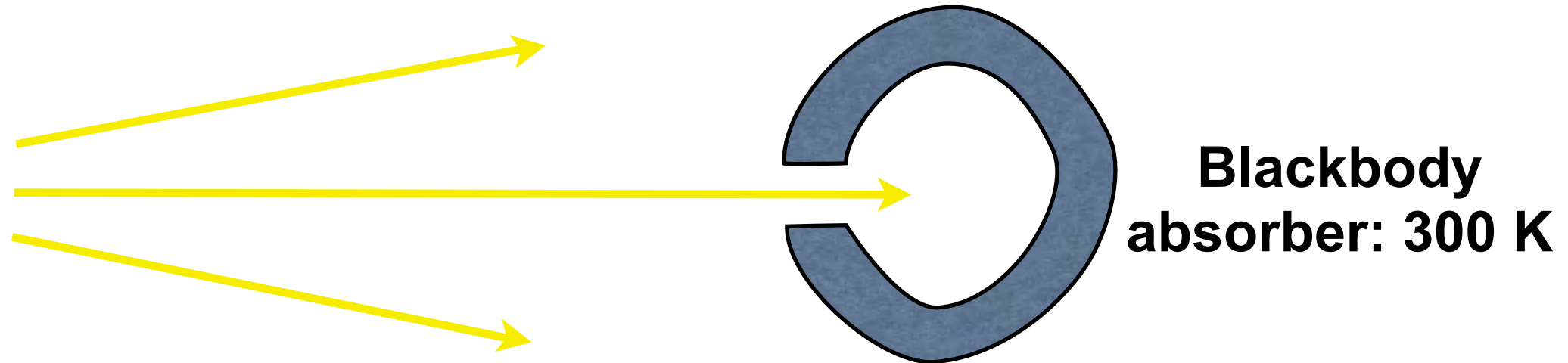


- “Air Mass Zero” (AM0) is the solar spectrum at the equator before it enters the atmosphere

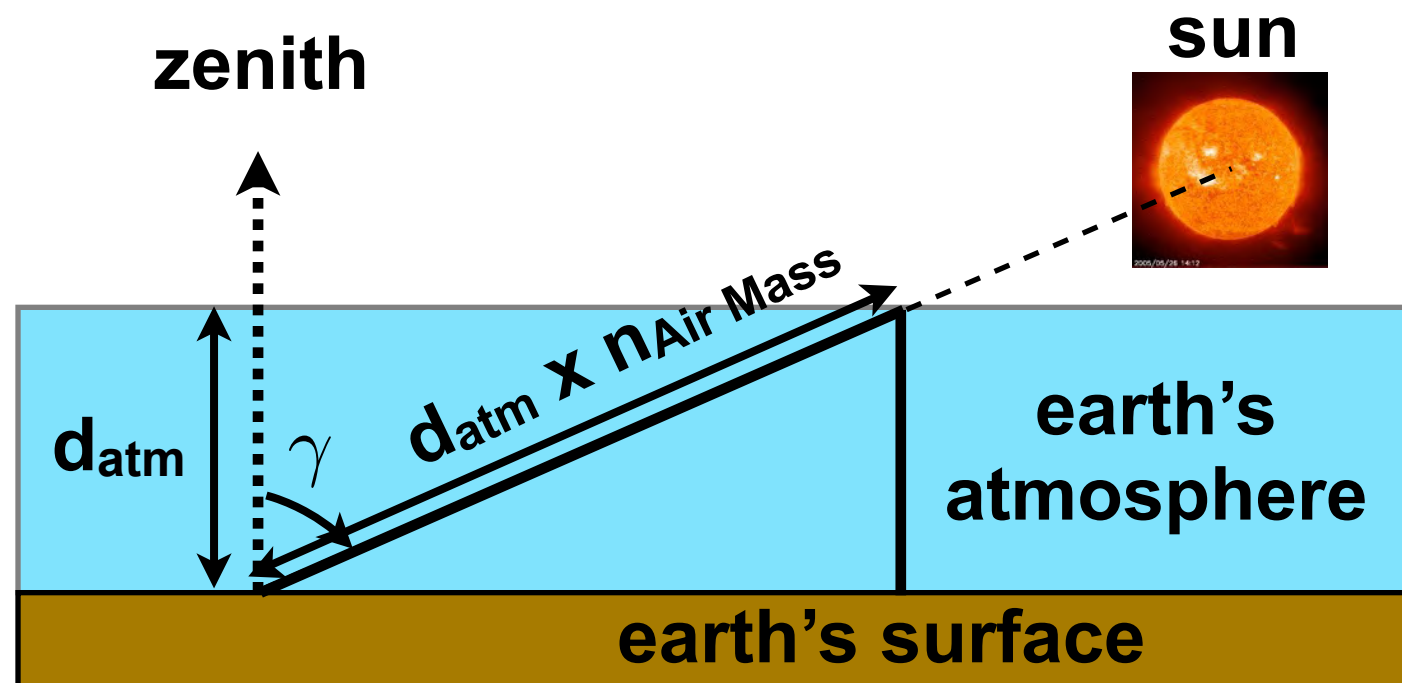


- Thermal limit i.e. heating for the sun as a 6000 K black body emitter with a 300 K solar cell black body absorber

Sun: 6000 K



- Maximum Carnot efficiency is 85% for absorber at 2470 K:  
all photons absorbed  
maximum heat from every photon  
zero thermal dissipation from absorber
- Actual efficiencies for a room temperature absorber are  $< 85\%$



$$\cos \gamma = \frac{d_{atm}}{d_{atm} \times n_{\text{Air Mass}}}$$

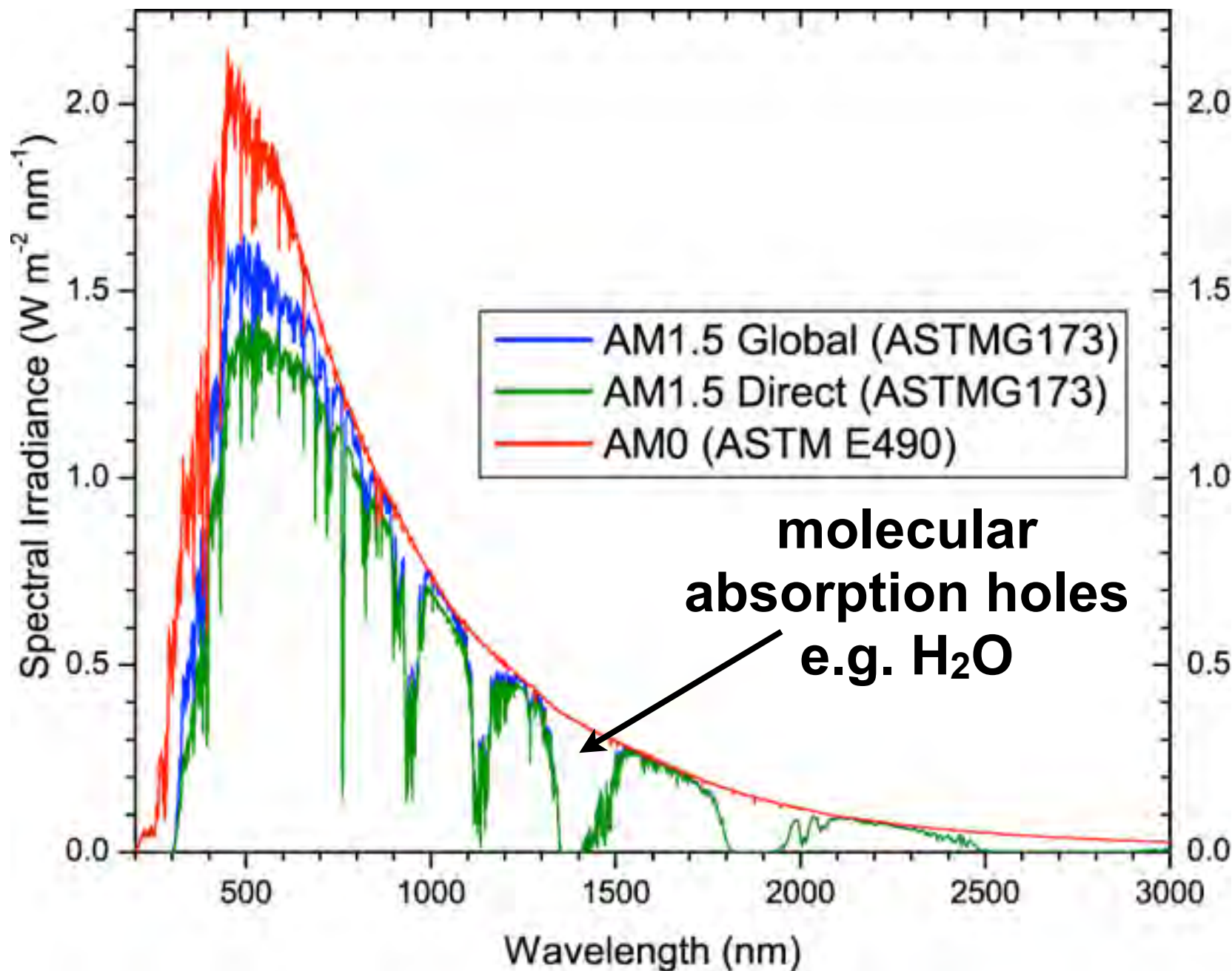
$$\begin{aligned} n_{\text{Air Mass}} &= \frac{\text{optical path length to sun}}{\text{optical path length if sun directly overhead}} \\ &= \frac{1}{\cos \gamma} \end{aligned}$$



To allow comparison between solar cell technology all cells compared at AM1.5



- **“Air Mass Zero” (AM0) is the solar spectrum at the equator before it enters the atmosphere**

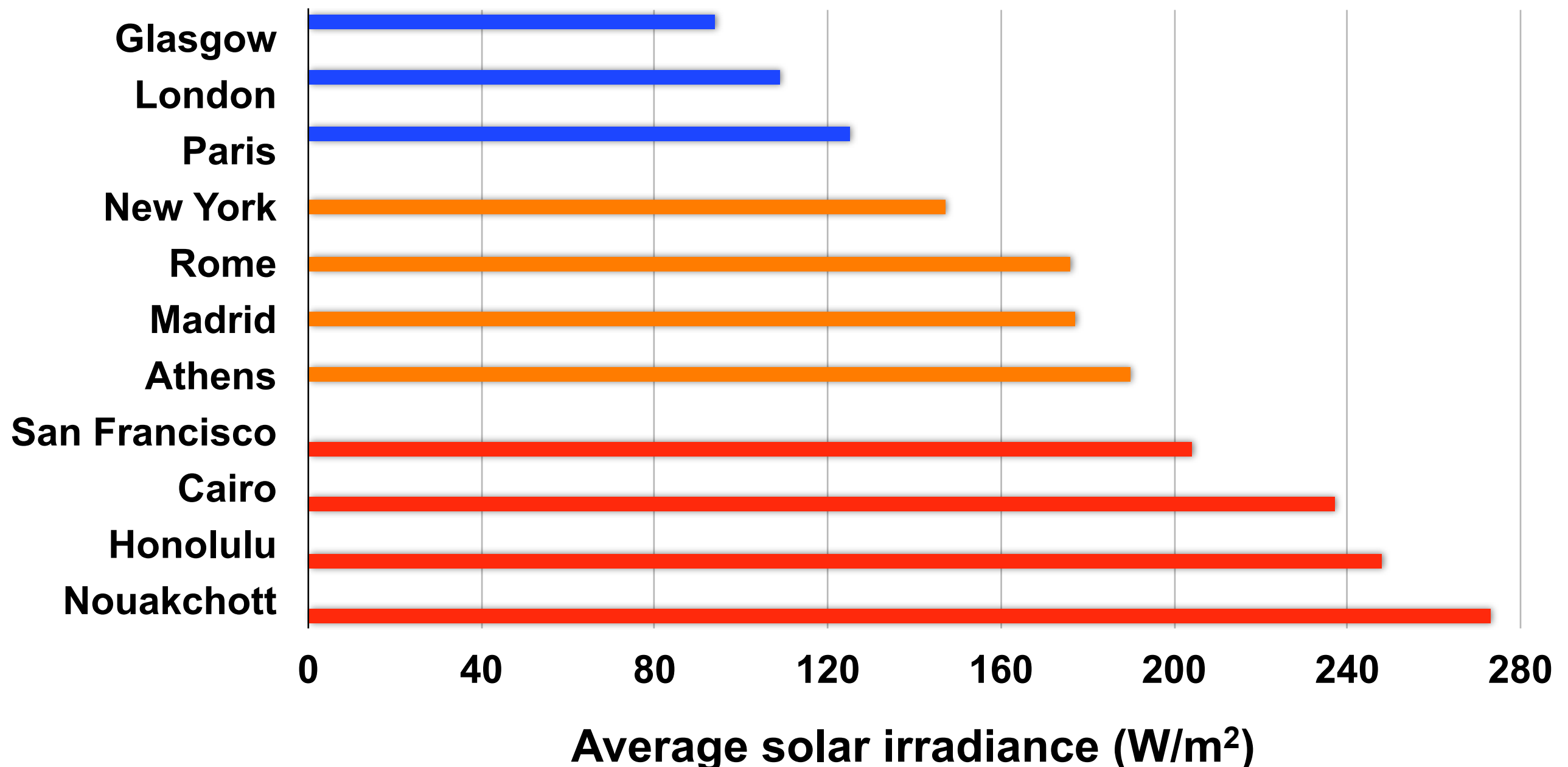


- **Maximum AM0 power is  $\sim 1353 \text{ W/m}^2$  over all wavelengths**

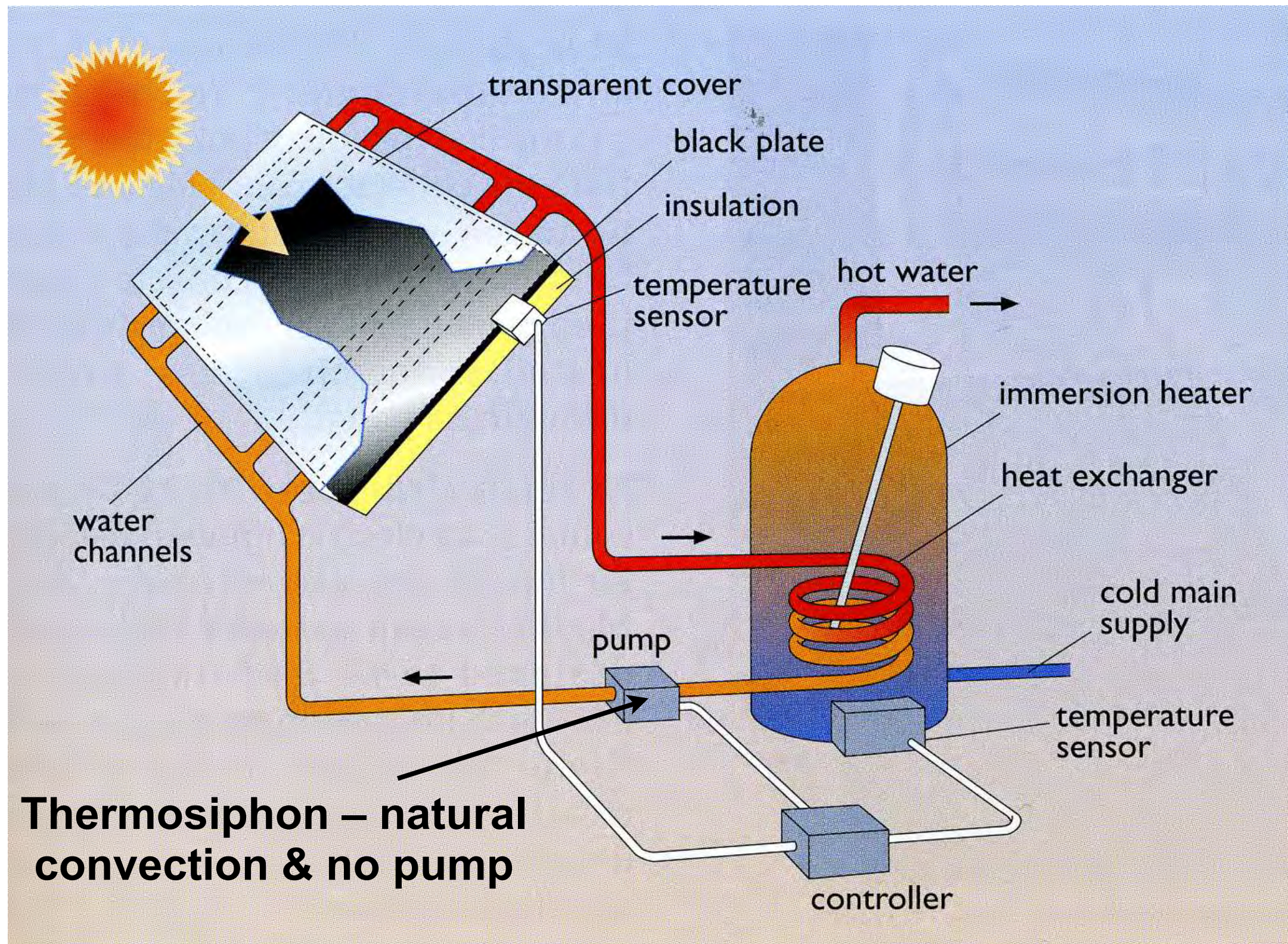
- **Molecular absorption produces “holes”**

- **AM1.5 power is  $\sim 1000 \text{ W/m}^2$  over all wavelengths**

- Due to clouds, day/night & seasons, average energy << peak energy
- Available energy needs to be averaged over 365 days and 24 hours







- Typically efficiencies up to 70% for generating hot water in homes

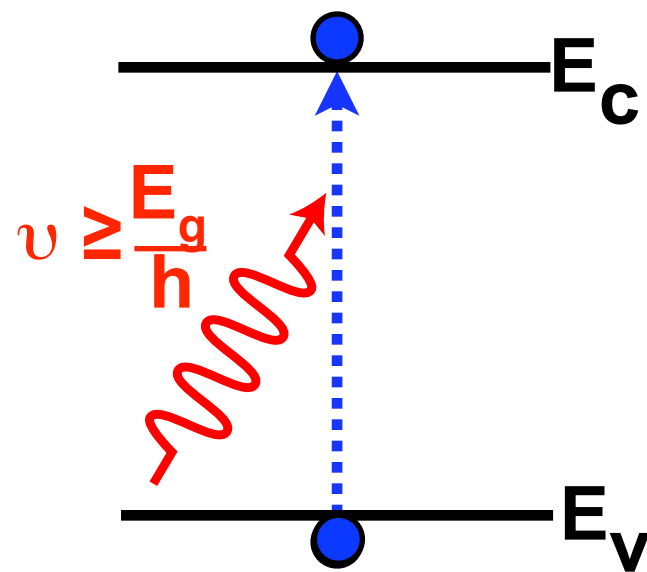




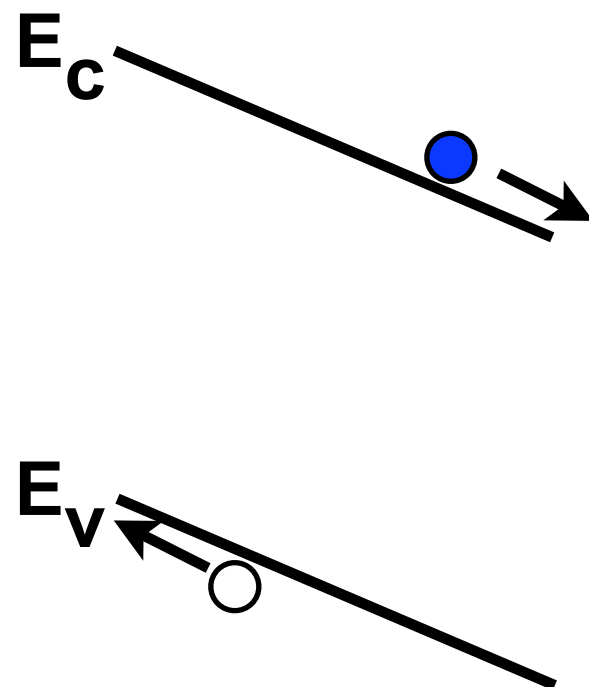
**Serpa, Portugal 11 MW from 52,000 photovoltaic modules**



**photon  
absorption**

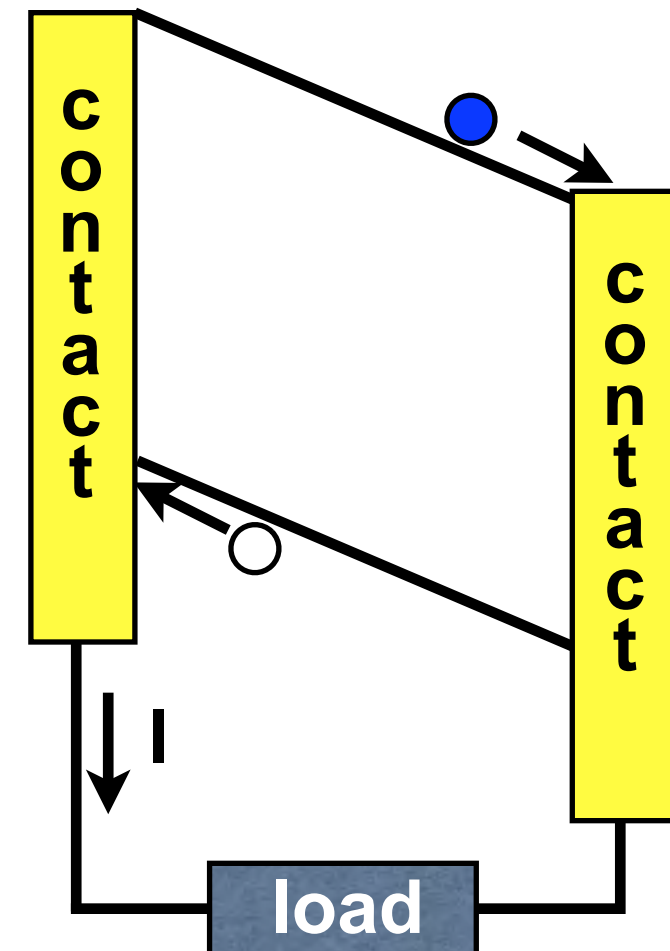


**separate  
electron-hole  
pairs**

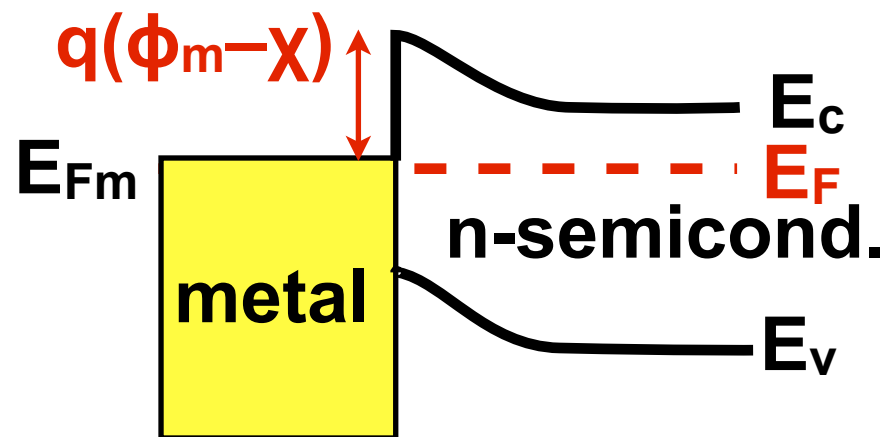


**an electric field  
is required**

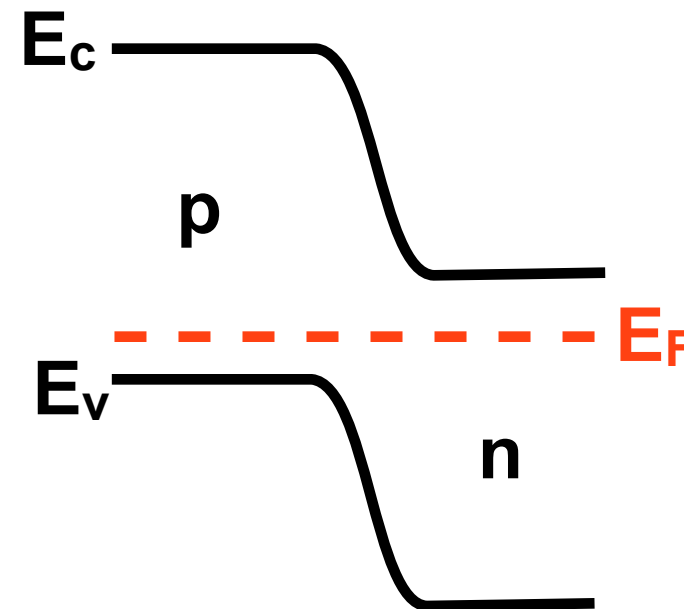
**collect  
current**



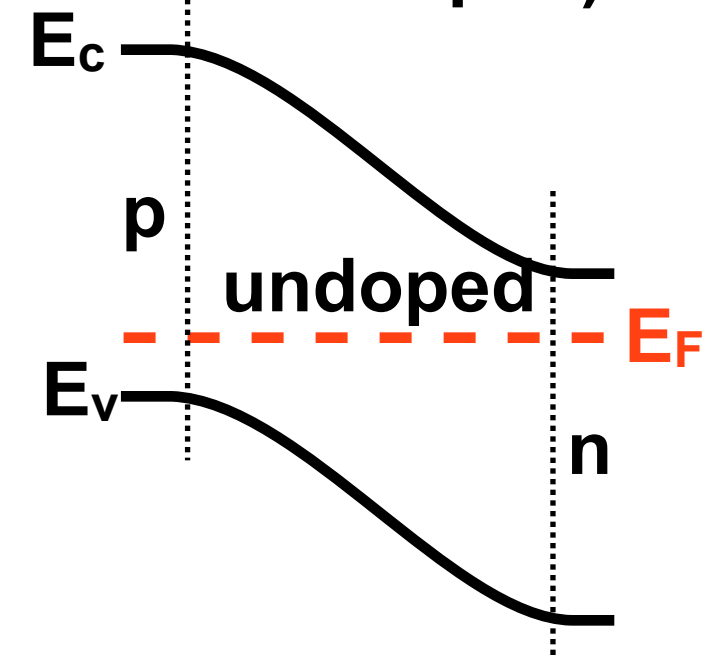
## Schottky diode



## p-n junction



## p-i-n junction (i = insulating = undoped)



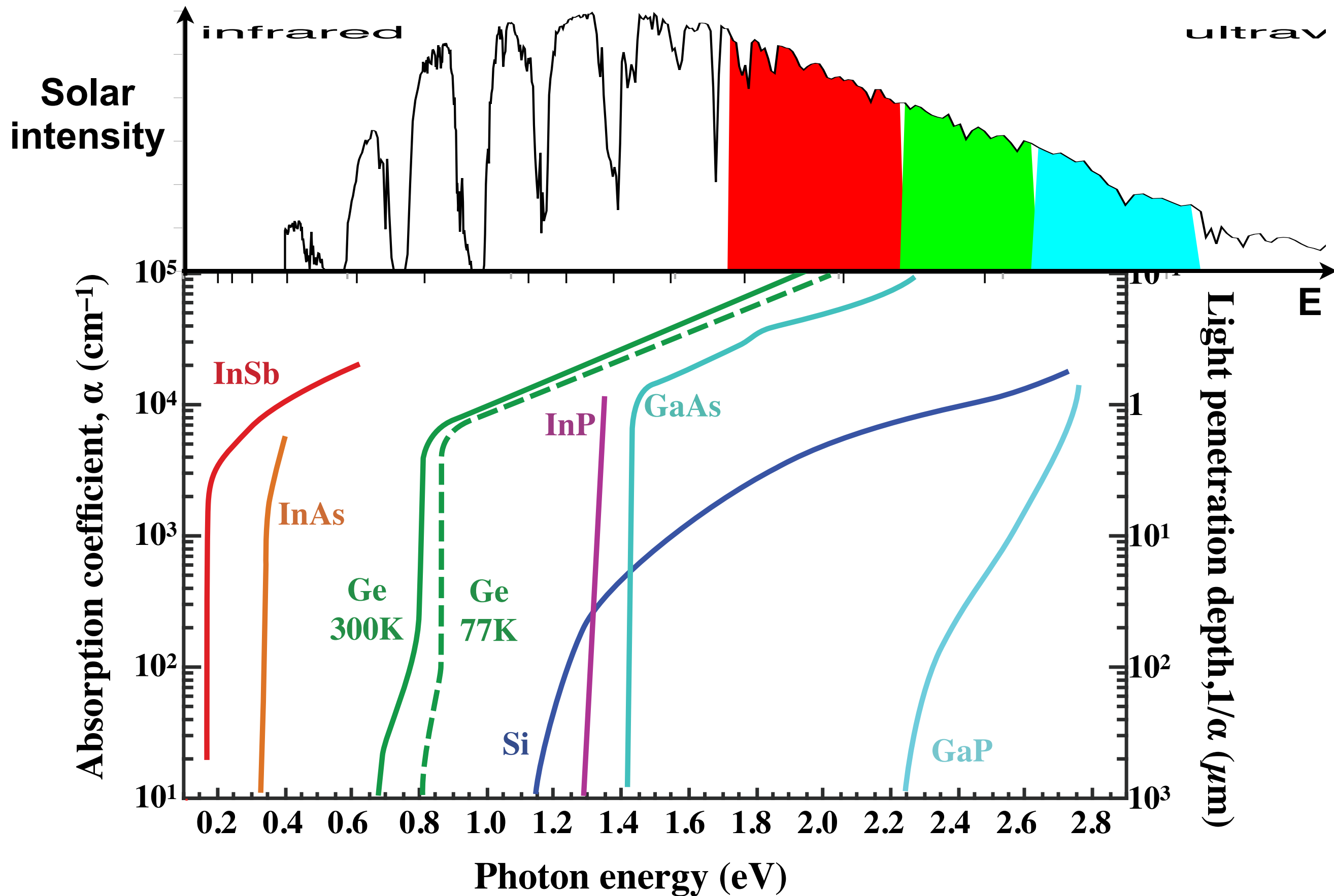
- N.B. only a few metals are transparent at visible wavelengths

- Schottky diodes not used for PV

- Expands region over which absorption + separation occurs

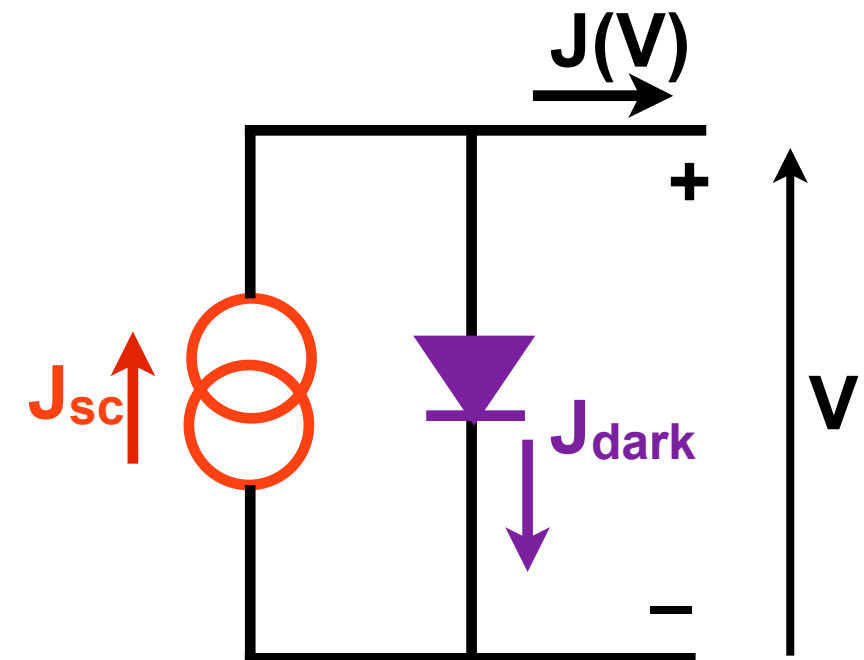
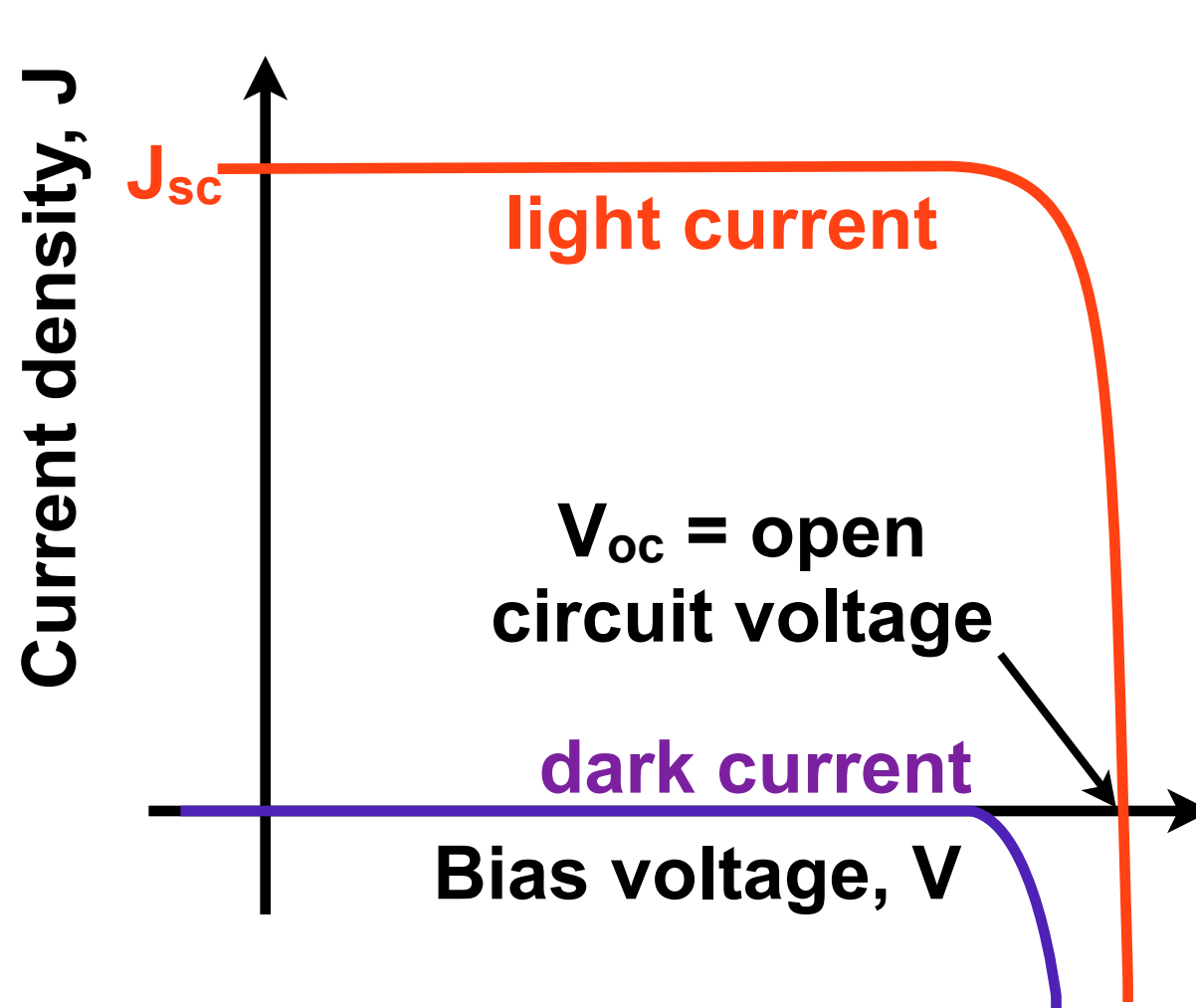
- Same IV equations as p-n junction



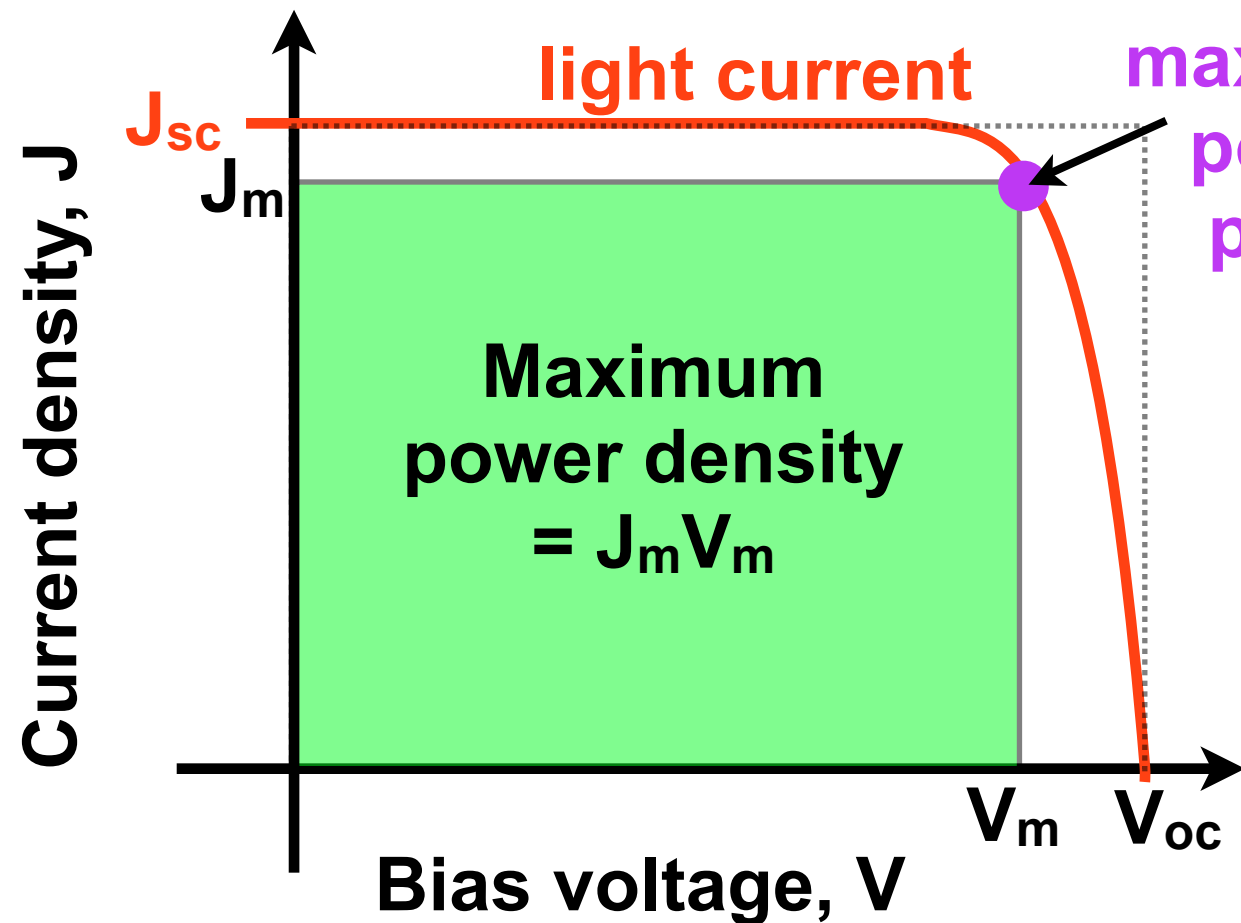


# The Superposition Approximation

- For solar cell, current-voltage can be approximated by the sum of short circuit photocurrent + dark current
- Current convention: photocurrent is positive (this is the opposite to normal current !)



$$J(V) = J_{sc} - J_{dark}(V)$$



● power density =  $P = JV$

$$\text{efficiency} = \frac{\text{electrical power out}}{\text{optical power in}}$$

$$\eta = \frac{P_{\max}}{P_{\text{opt}}} = \frac{J_m V_m}{P_{\text{opt}}}$$

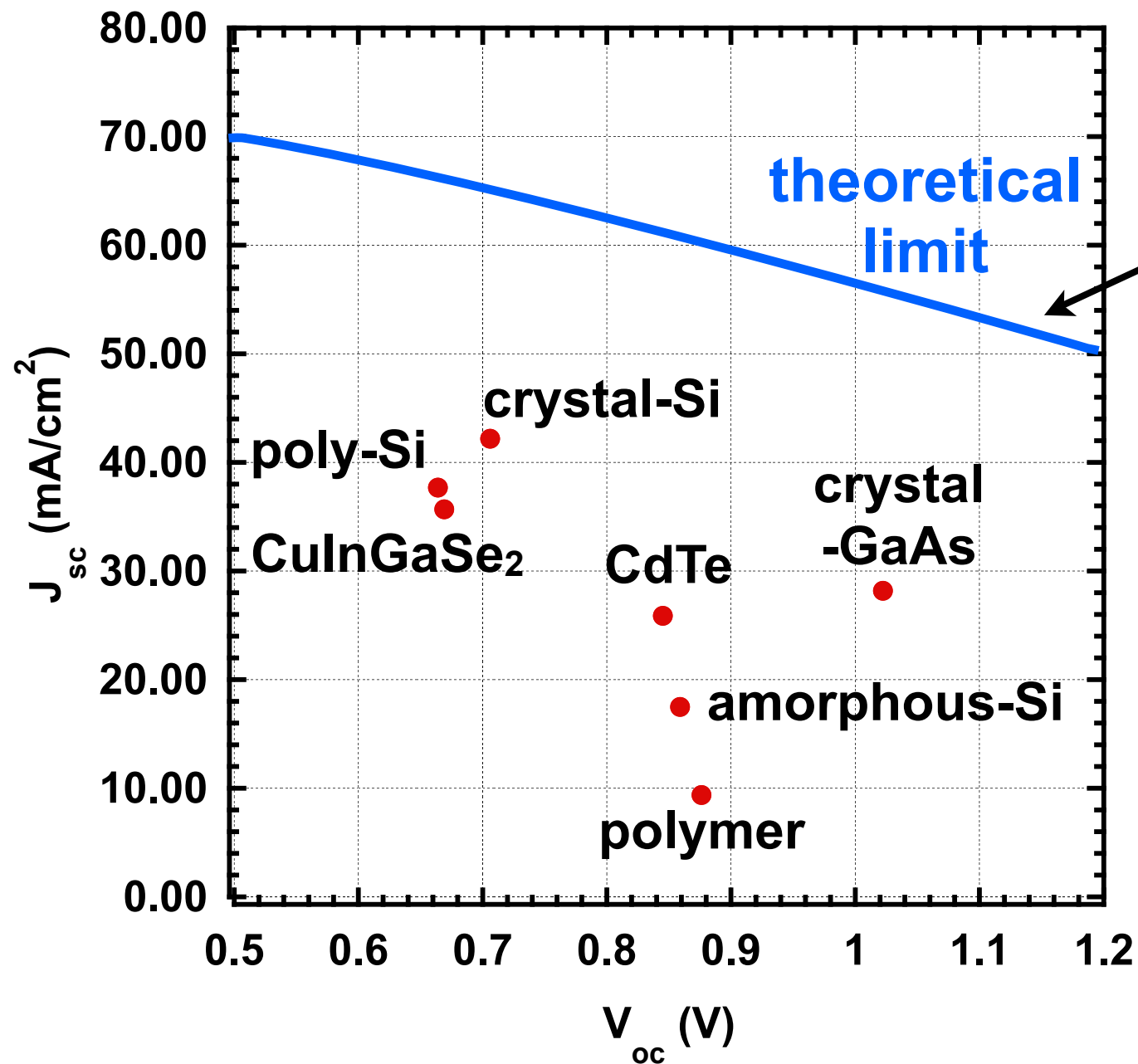
● The efficiency is related to  $J_{sc}$  and  $V_{oc}$  using the fill factor, FF

$$\eta = \frac{J_{sc} V_{oc} FF}{P_{\text{opt}}}$$

or

$$FF = \frac{J_m V_m}{J_{sc} V_{oc}}$$





Maximum theoretical  
output power

●  $J_{sc}V_{oc} \propto \text{constant} = f(E_g)$

● i.e. high  $J_{sc} \rightarrow$  low  $V_{oc}$   
and vice-versa

● N.B. All voltages too low for most appliances and  
applications: requires stacking

- Best results quoted from the literature – not commercial devices

Type	$\eta$ (%)	$V_{oc}$ (V)	$J_{sc}$ (mA/cm <sup>2</sup> )	FF (%)
crystalline silicon	$25.0 \pm 0.5$	0.706	42.7	82.8
crystalline GaAs	$28.3 \pm 0.8$	1.107	29.5	86.7
polycrystalline silicon	$20.4 \pm 0.5$	0.664	38	80.9
amorphous Si	$10.1 \pm 0.3$	0.886	16.8	67
CdTe	$16.5 \pm 0.5$	0.845	25.9	75.5
organic polymer	$10.0 \pm 0.3$	0.889	16.8	66.1

*Prog. Photovoltaics: Res. Appl. 20, 12 (2012)*

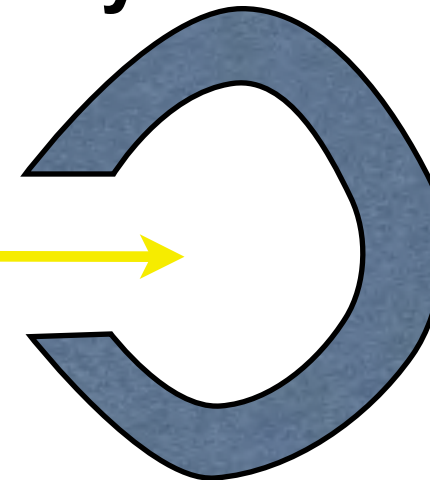
- Standard test conditions: 1000 W/m<sup>2</sup> illumination (i.e. 1 sun - no concentration) with AM1.5 spectra at 25 °C
- $\eta$  decay over time due to x-ray absorption from sun / space

- Thermal limit i.e. heating for the sun as a 6000 K black body emitter with a 300 K solar cell black body absorber

Sun: 6000 K

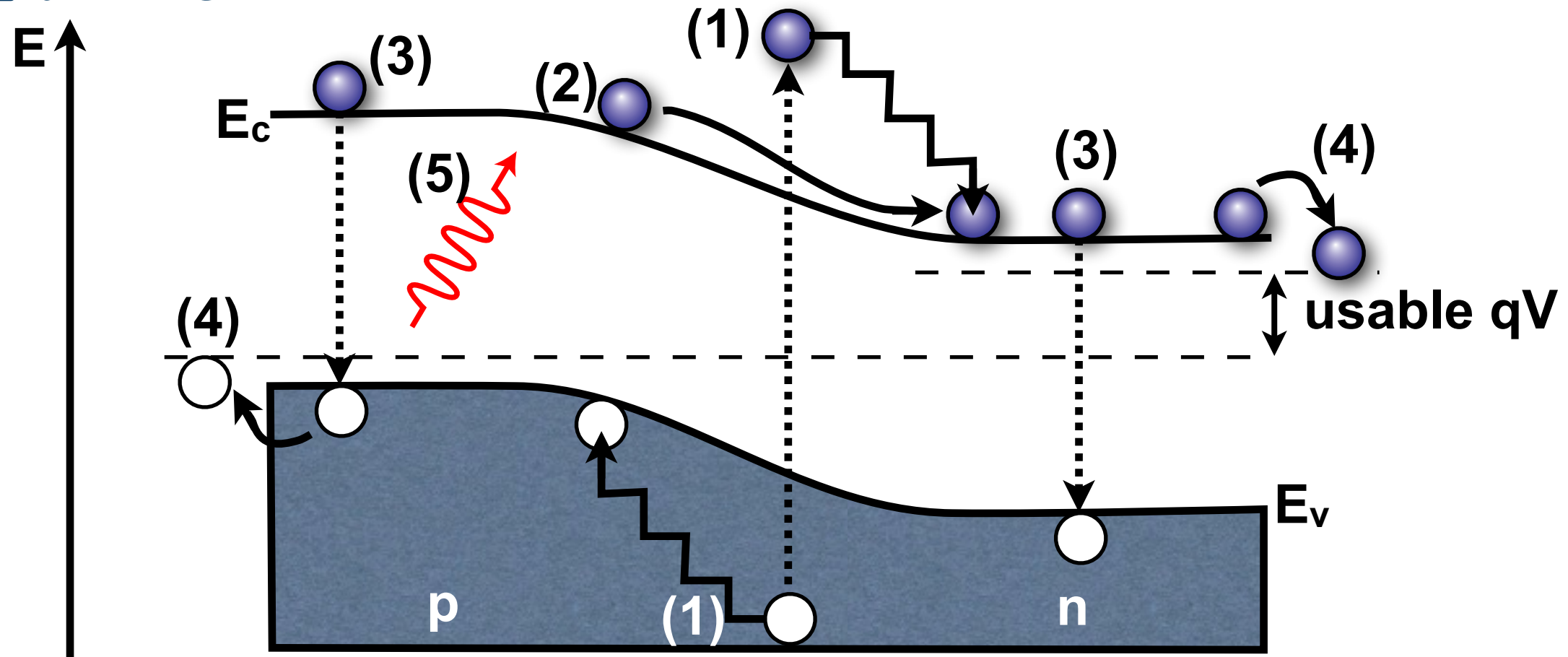


Blackbody absorber: 300 K



- Maximum Carnot efficiency is 85% for absorber at 2470 K:  
all photons absorbed  
maximum heat from every photon  
zero thermal dissipation from absorber
- Why are real PV cells significantly smaller than is efficiency?





Energy conversion loss processes in single-junction solar cell:

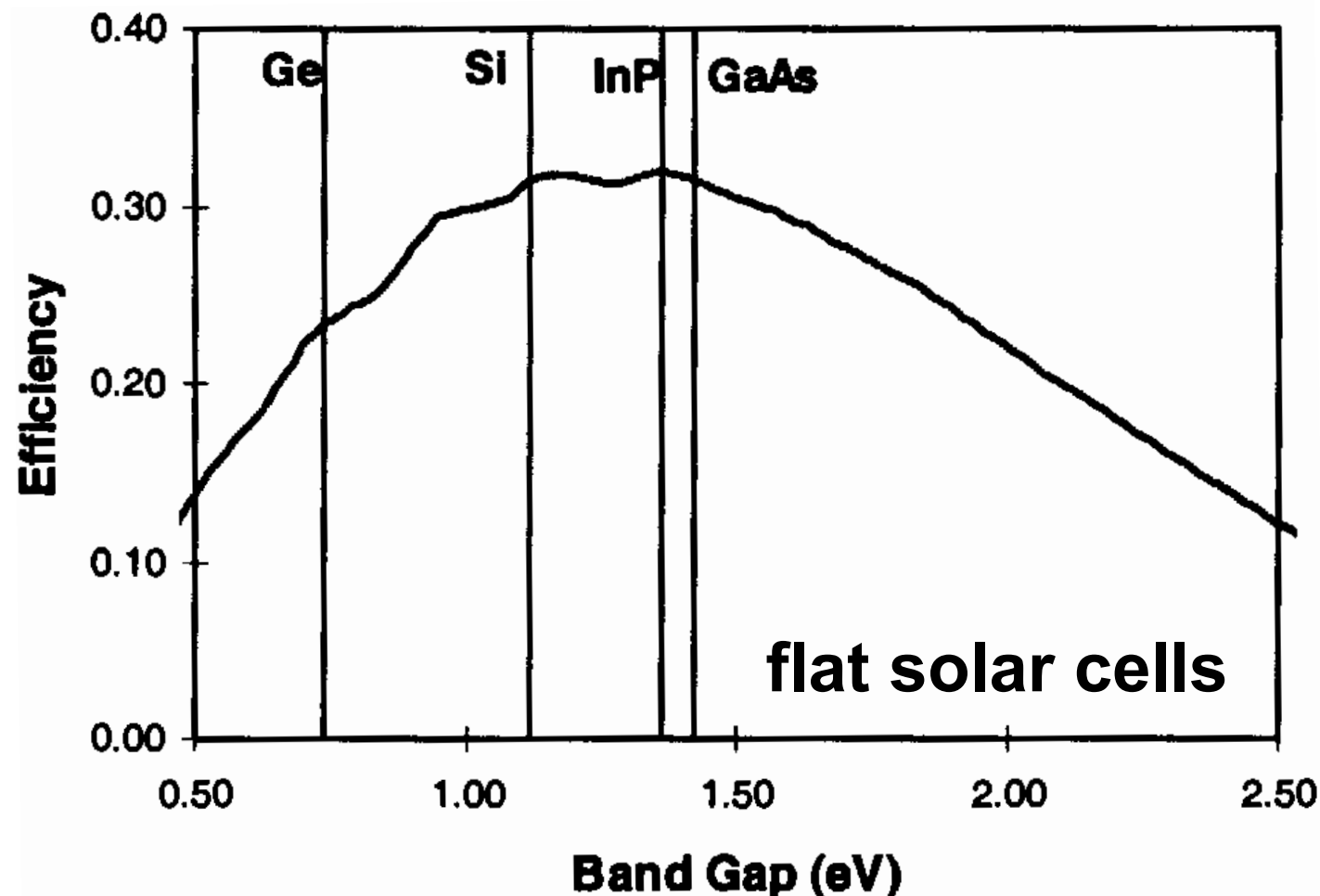
- (1) Lattice thermalisation loss
- (2) Junction loss
- (3) recombination loss
- (4) contact loss
- (5) no absorption from photons with energy  $< E_g$

For **Si** cells:  $T_s = 6000 \text{ K}$ ,  $T_c = 300 \text{ K}$ ,  $E_g = 1.1 \text{ eV}$

● **Maximum  $\eta = 30\%$**

For **GaAs** cells:  $T_s = 6000 \text{ K}$ ,  $T_c = 300 \text{ K}$ ,  $E_g = 1.46 \text{ eV}$

● **Maximum  $\eta = 31\%$**



● Quite low efficiencies for single junction cells

● Variation with  $E_g$  related to black-body curve

● What can be done to improve efficiency?

Reflected light  
= losses !

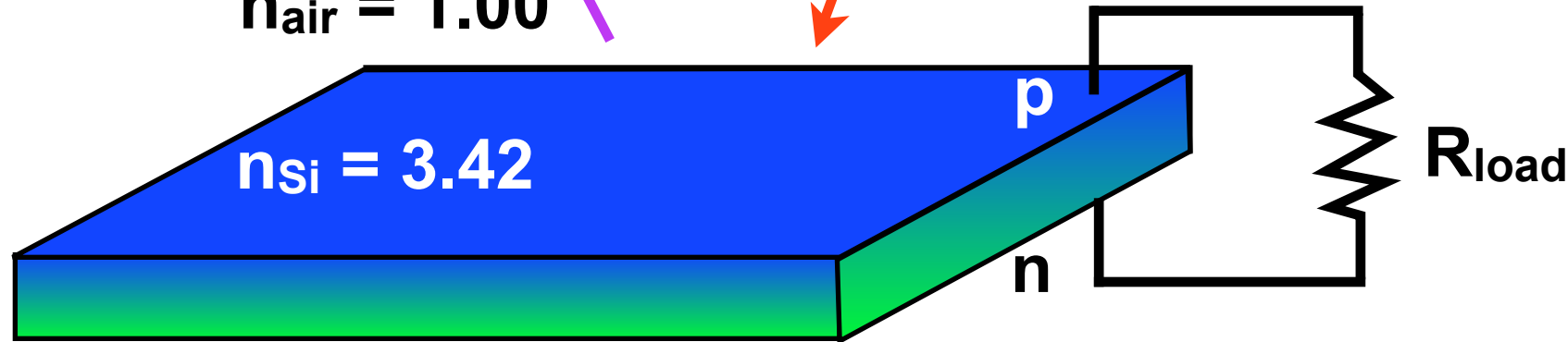
sun light

Reflected light =

$$R = \left( \frac{n_{\text{Si}} - n_{\text{air}}}{n_{\text{Si}} + n_{\text{air}}} \right)^2 = 30\%$$

$n_{\text{air}} = 1.00$

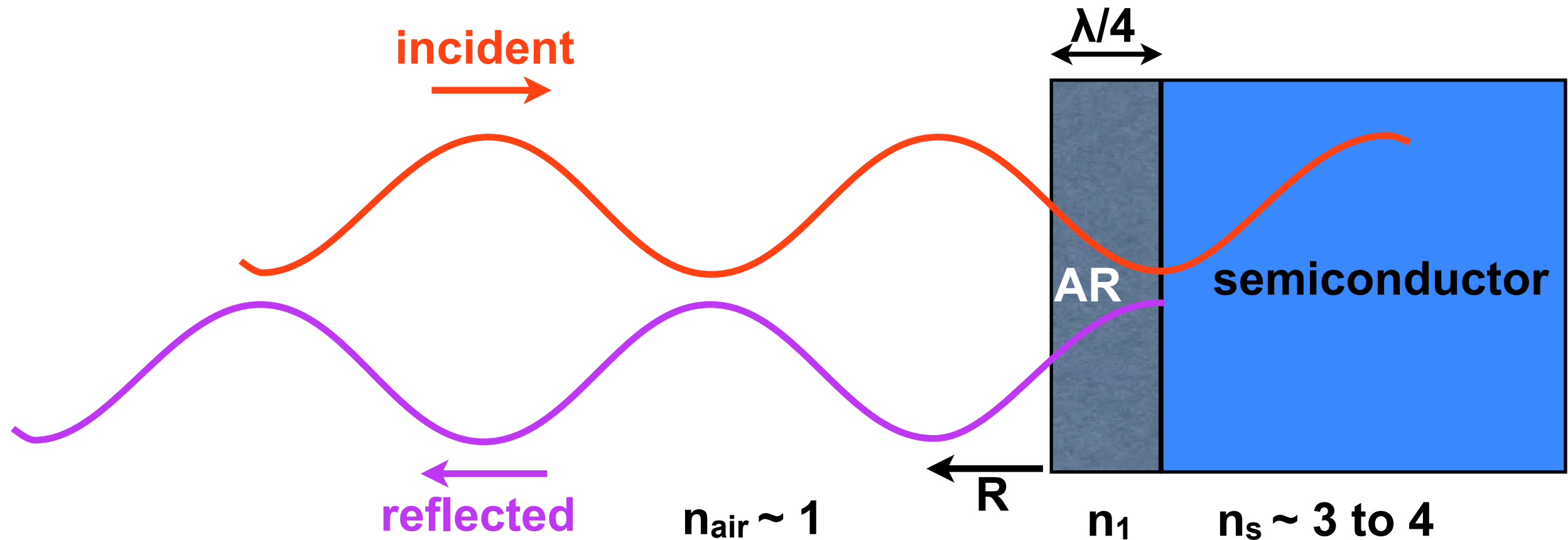
$n_{\text{Si}} = 3.42$



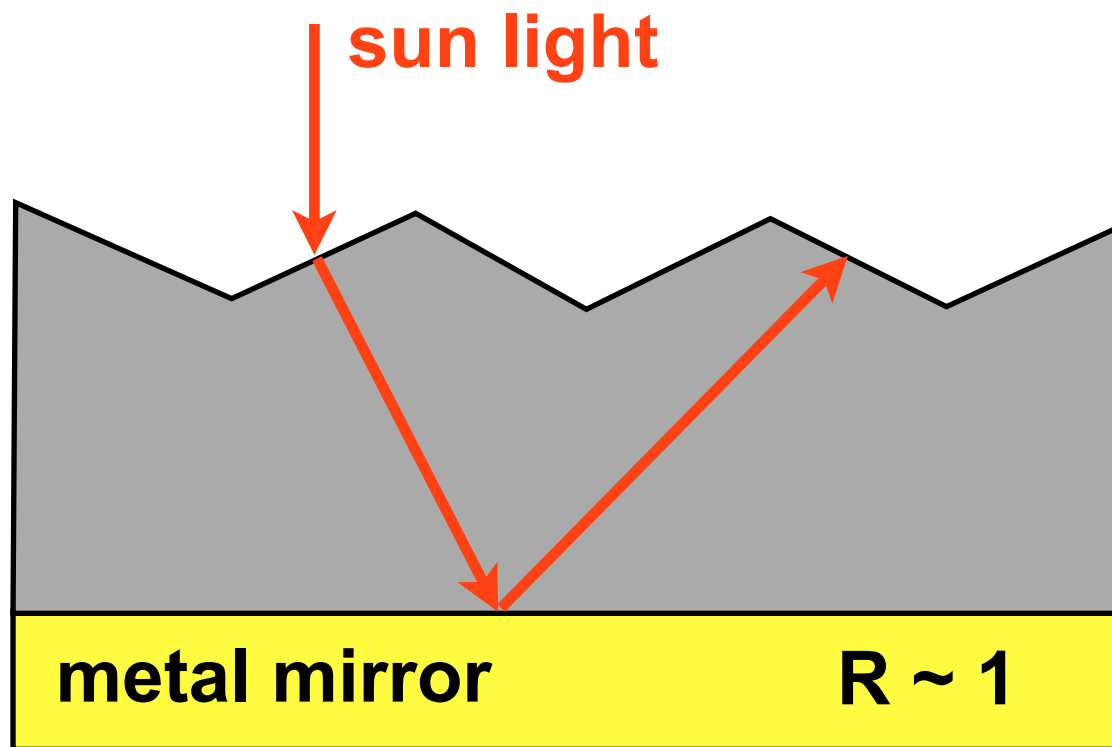
- Efficiency for standard flat Si wafer = 13% since many photons are not absorbed
- Need to reduce all surface reflections
- Also need longer path length for absorption: can we trap the light?



# Anti-reflection (AR) Coatings



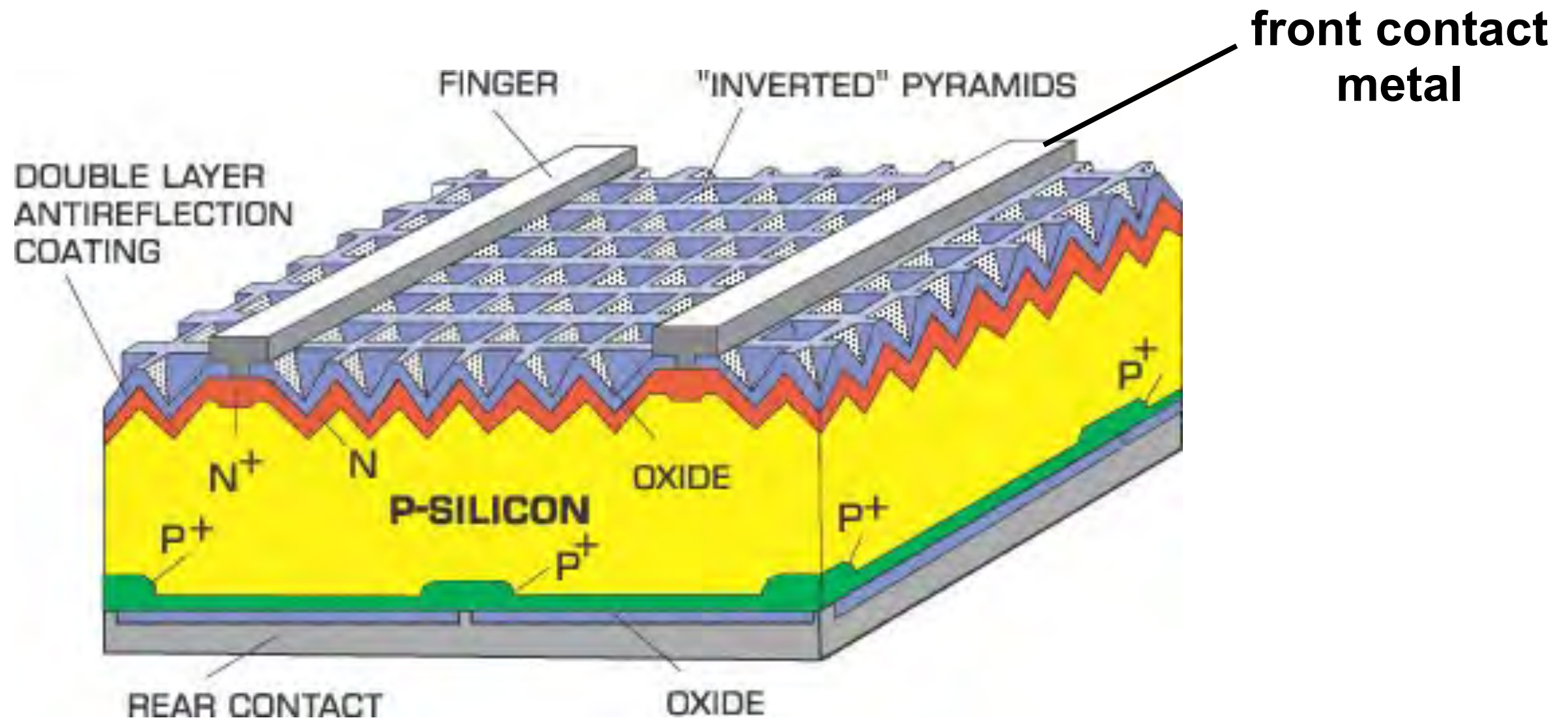
- $R$  vanishes for  $n_1 = \sqrt{n_{\text{air}} n_s} \sim \sqrt{n_s}$  with a thickness of  $\lambda/4$
- For this condition, incident and reflect waves are out of phase & interfere destructively so  $R \rightarrow 0$
- $\therefore \eta$  increases since more light is trapped and can be absorbed



Also electrical contact metal

- Path length of light doubled
- Higher probability of absorption

- Asymmetrical patterning can produce x4 or greater path length
- Texturing can be combined with anti-reflection coating



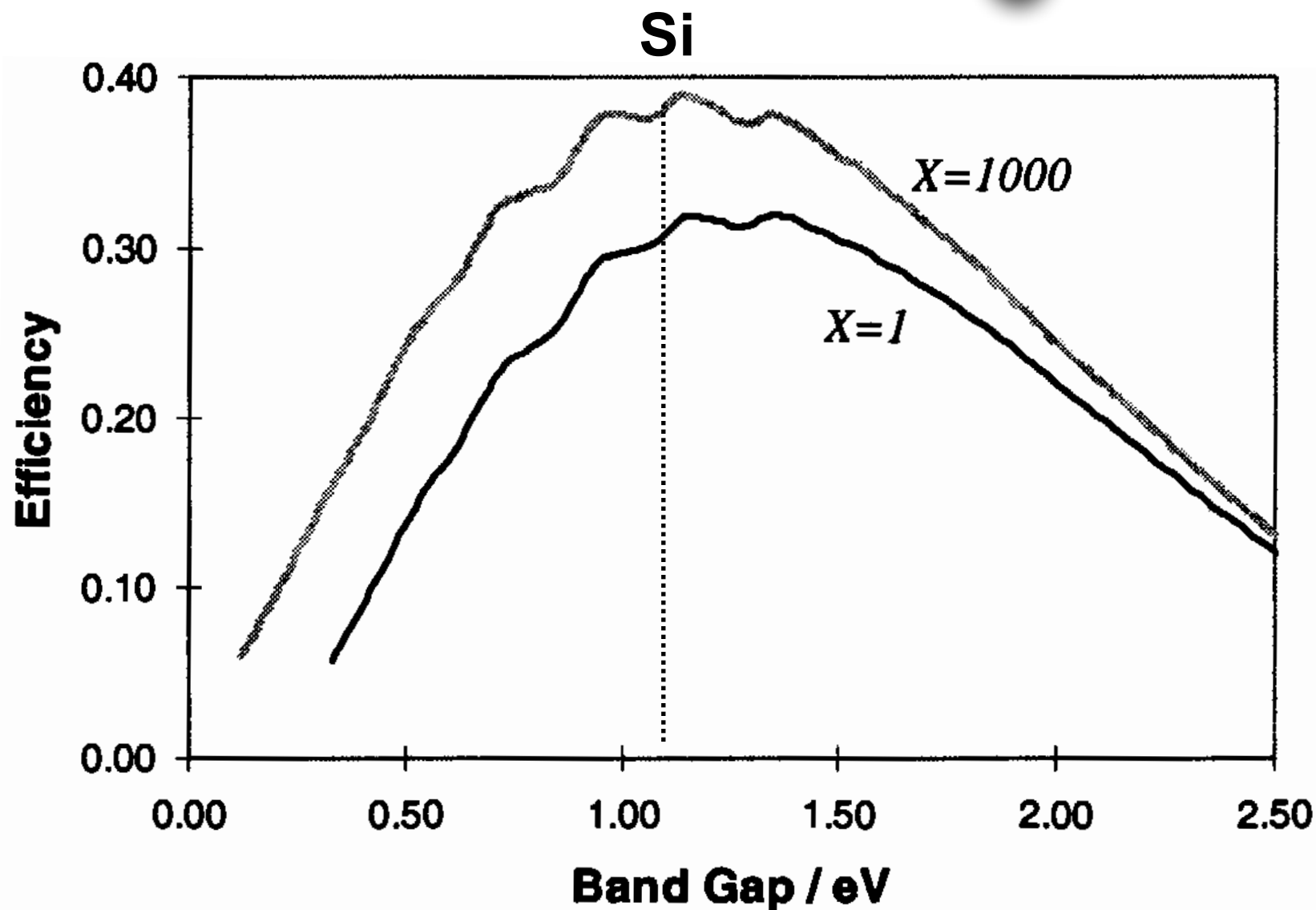
● Highest performance silicon solar cell: 25.0% efficiency

● Anti-reflective coatings, textured surface, bottom mirror

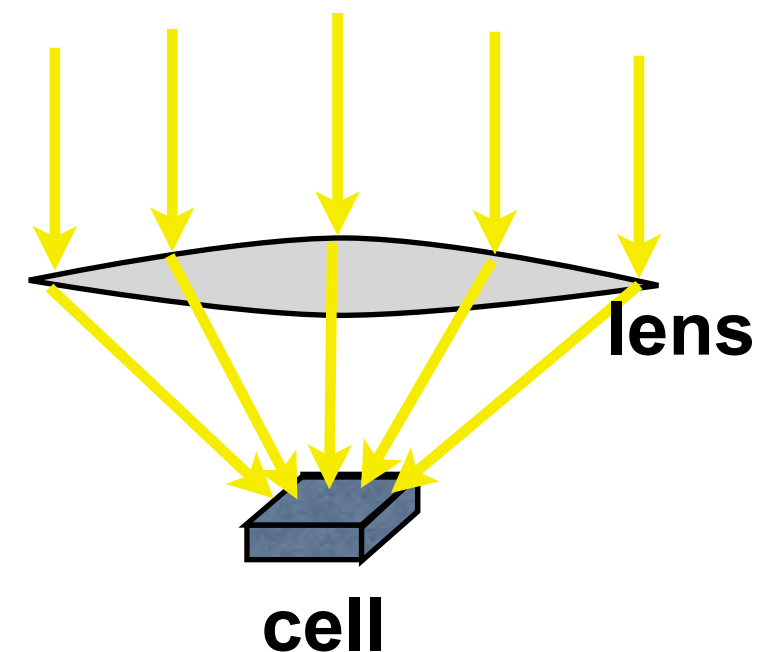
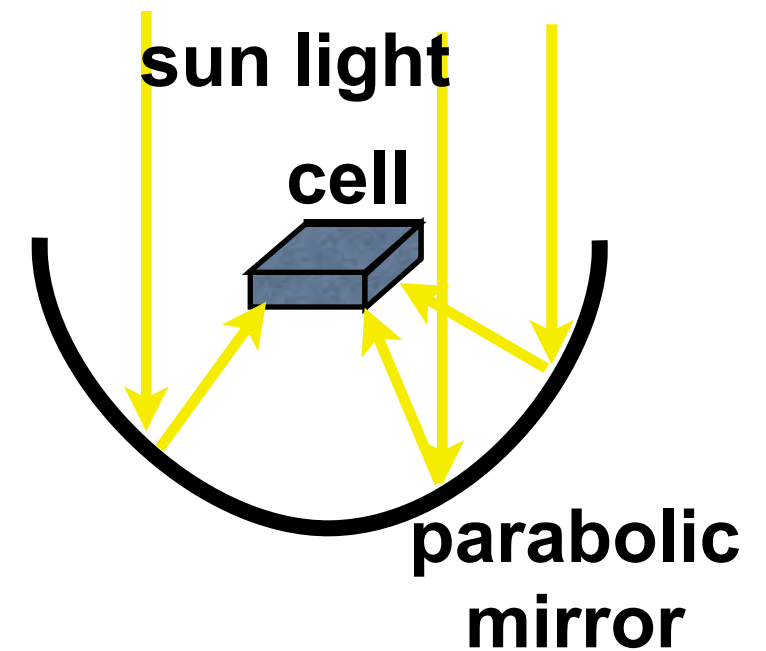


- Increase  $f_s$  = solar intercept fraction by concentrating light into cell

● Examples:

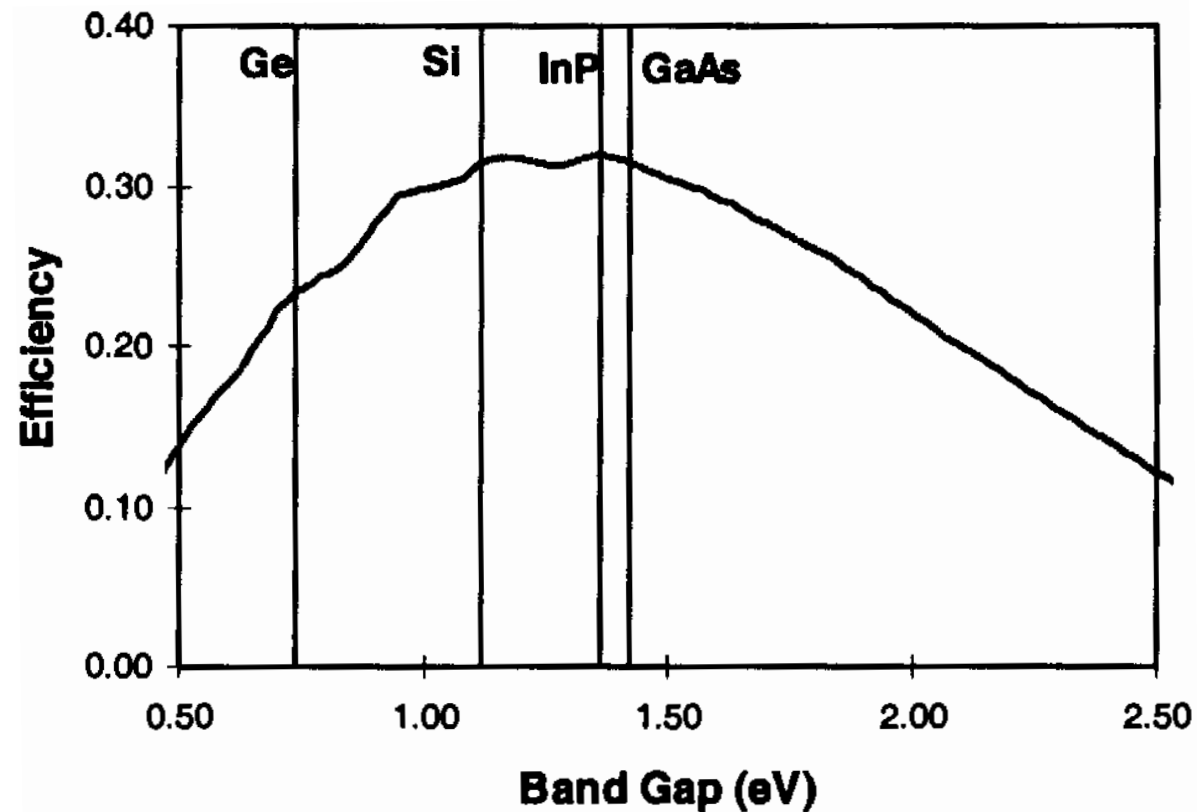


More light captured → Shockley-Queisser limit increases

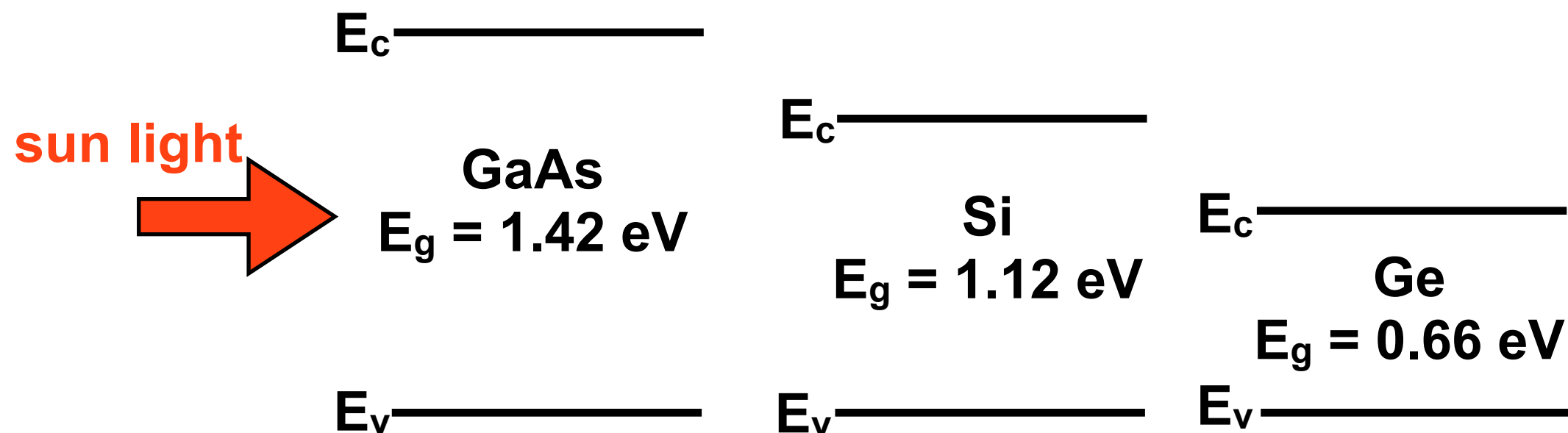


- **The sun moves from the east to the west through a day**
- **A tracking system can be used so that the solar cell is always pointing at the sun**
- **Tracking systems give 40% more energy compared to stationary systems – but at higher system cost**
- **For many concentration designs, tracking systems are essential**

# Multiple Bandgap Cells

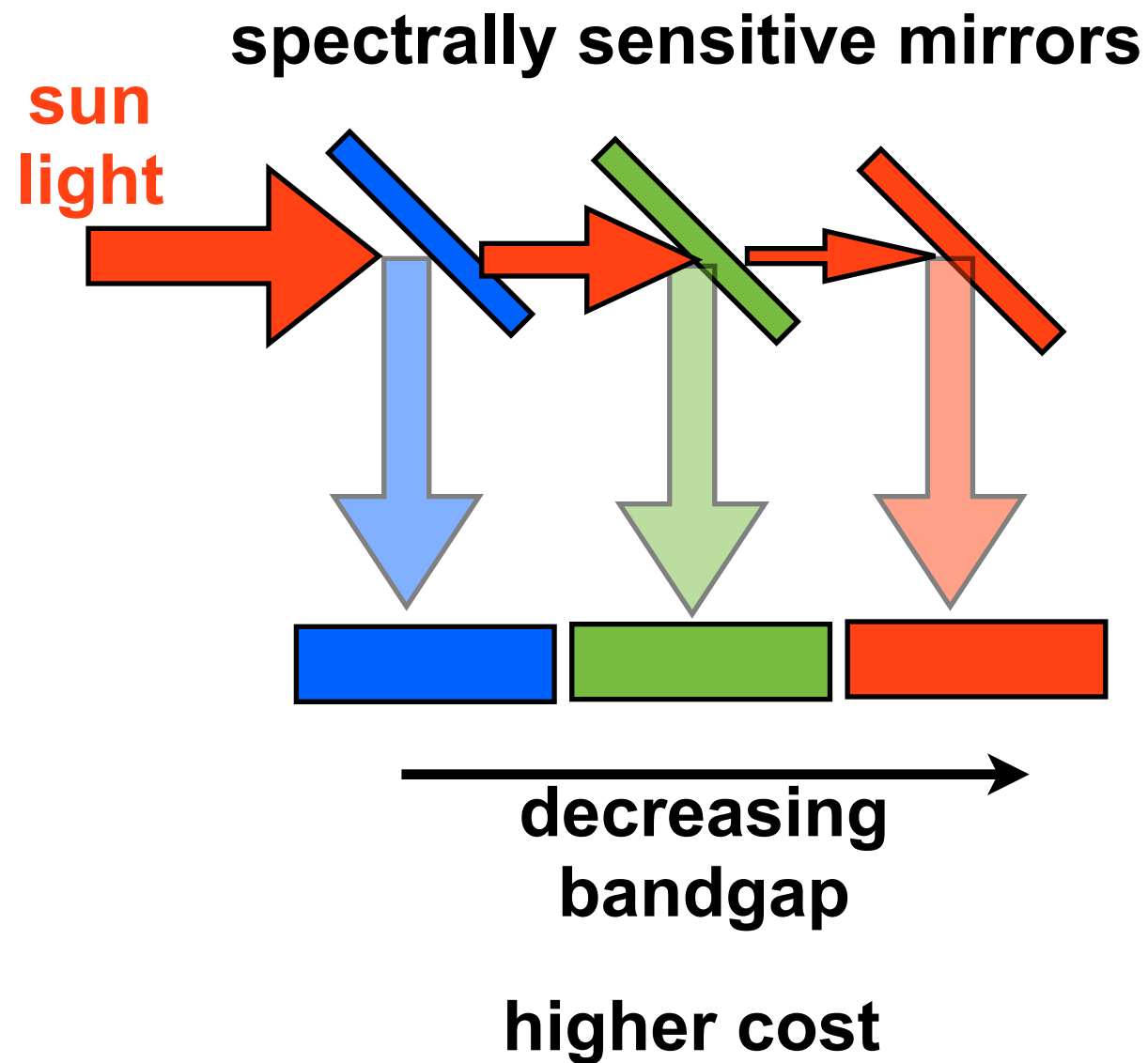


- Choose 2 or 3 materials with different bandgaps
- Need to have largest bandgap as front cell due to absorption
- Example: GaAs, Si and Ge cells



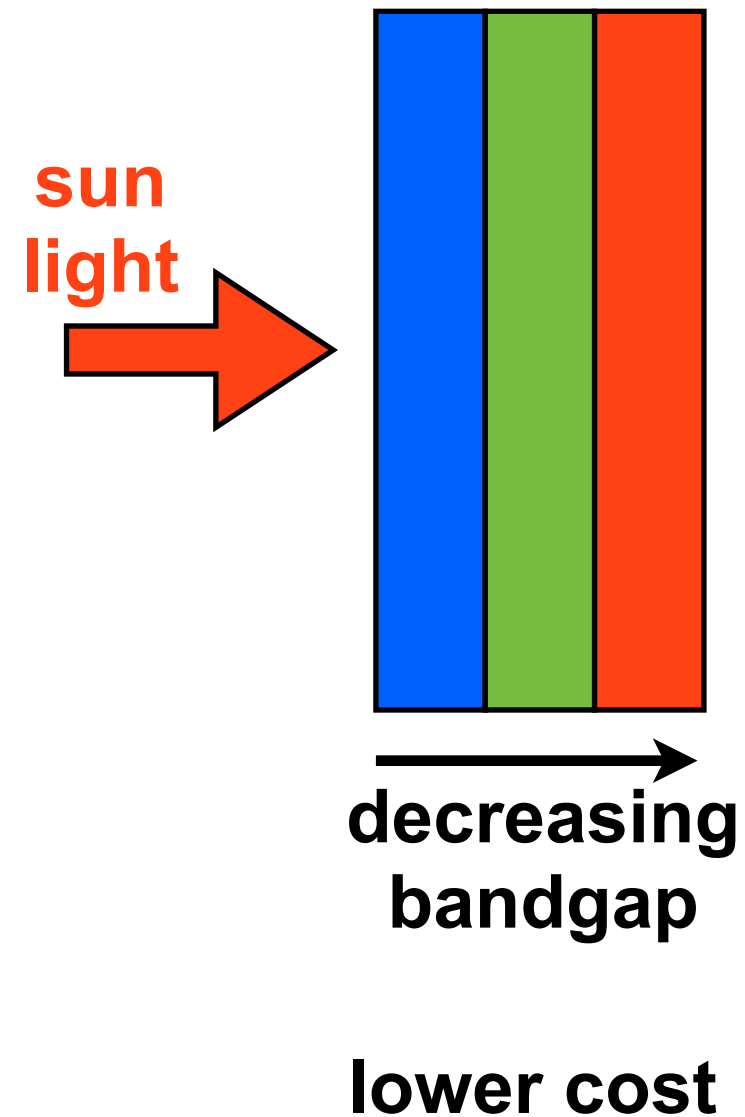


## ● Spectrum splitting



## ● Cell stacking

series connected p-i-n



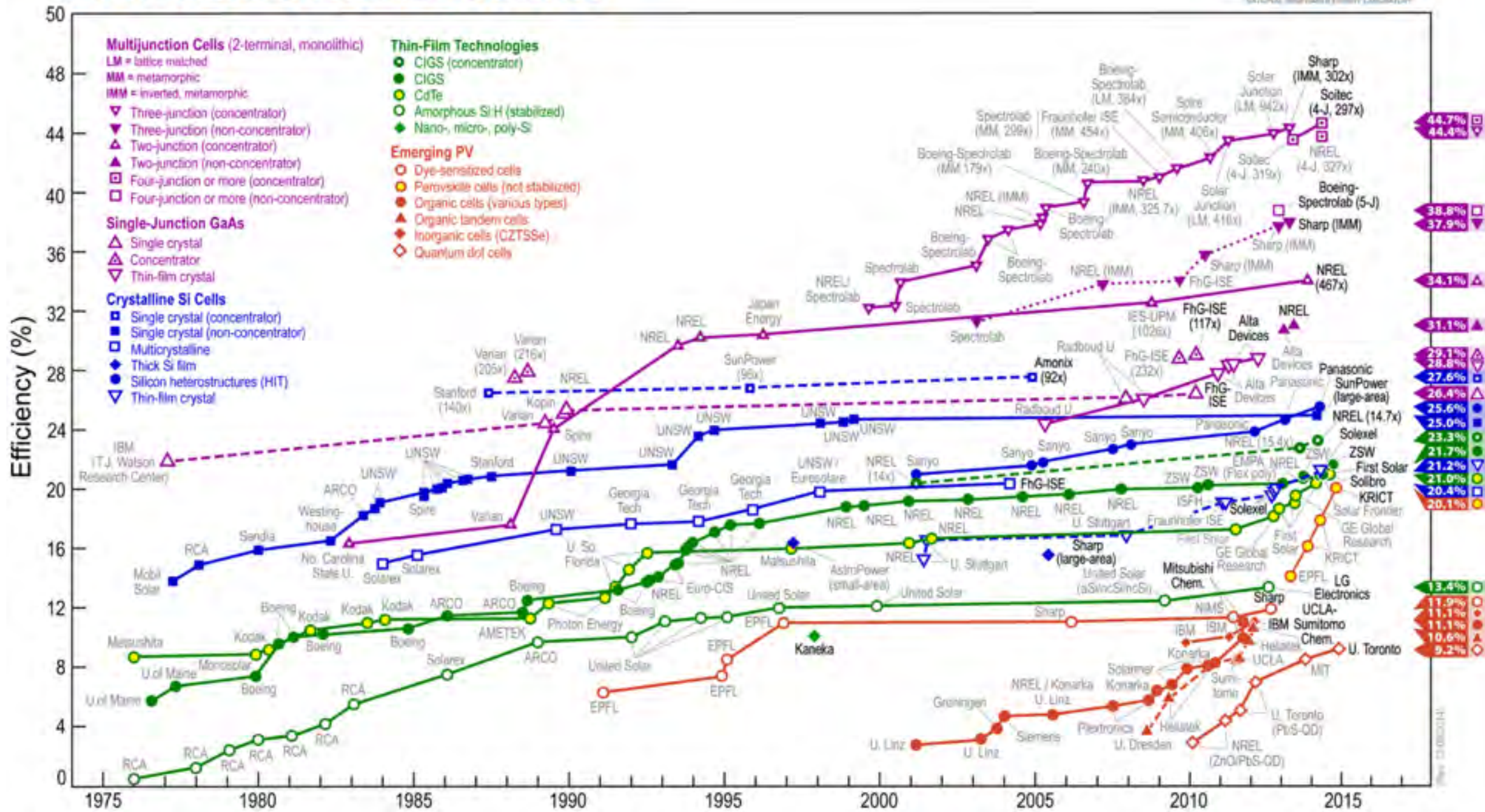
● All values at 1 sun AM1.5 **without concentration**

No. of cells	Description	Optimal bandgaps (eV)						Max. $\eta$ (%)
		E <sub>1</sub>	E <sub>2</sub>	E <sub>3</sub>	E <sub>4</sub>	E <sub>5</sub>	E <sub>6</sub>	
1	diffuse series	1.31						31
2	diffuse series	0.97	1.7					42.5
3	diffuse series	0.82	1.3	1.95				48.6
4	diffuse series	0.72	1.1	1.53	2.14			52.5
5	diffuse series	0.66	0.97	1.3	1.7	2.29		55.1
6	diffuse series	0.61	0.89	1.16	1.46	1.84	2.41	57
$\infty$	diffuse series							68.2

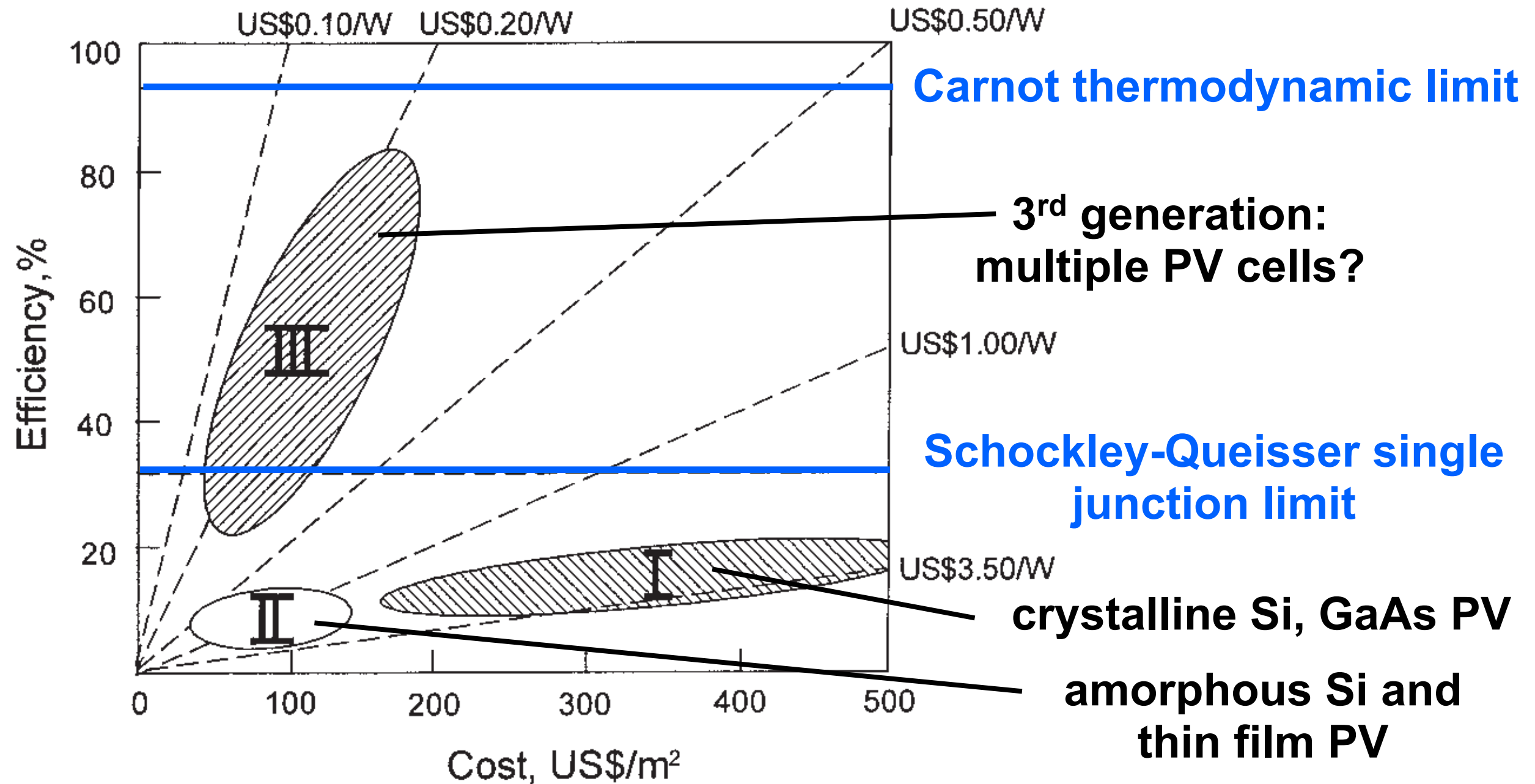
*M.A. Green "Third Generation Photovoltaics" Springer (2003)*

● Best demonstrated 3 bandgap cell has  $\eta = 37.9\%$  for 1 sun !

## Best Research-Cell Efficiencies







- **The market is driven by cost per Watt generated**
- **Smaller area is cheaper so higher efficiency is a stronger driver**

Highest Quality
Electromagnetic
Mechanical (kinetic)
Photon (light)
Chemical
Heat (thermal)
Lowest Quality

- First proposed as **availability** by Kelvin in 1851  
refined by Ohta

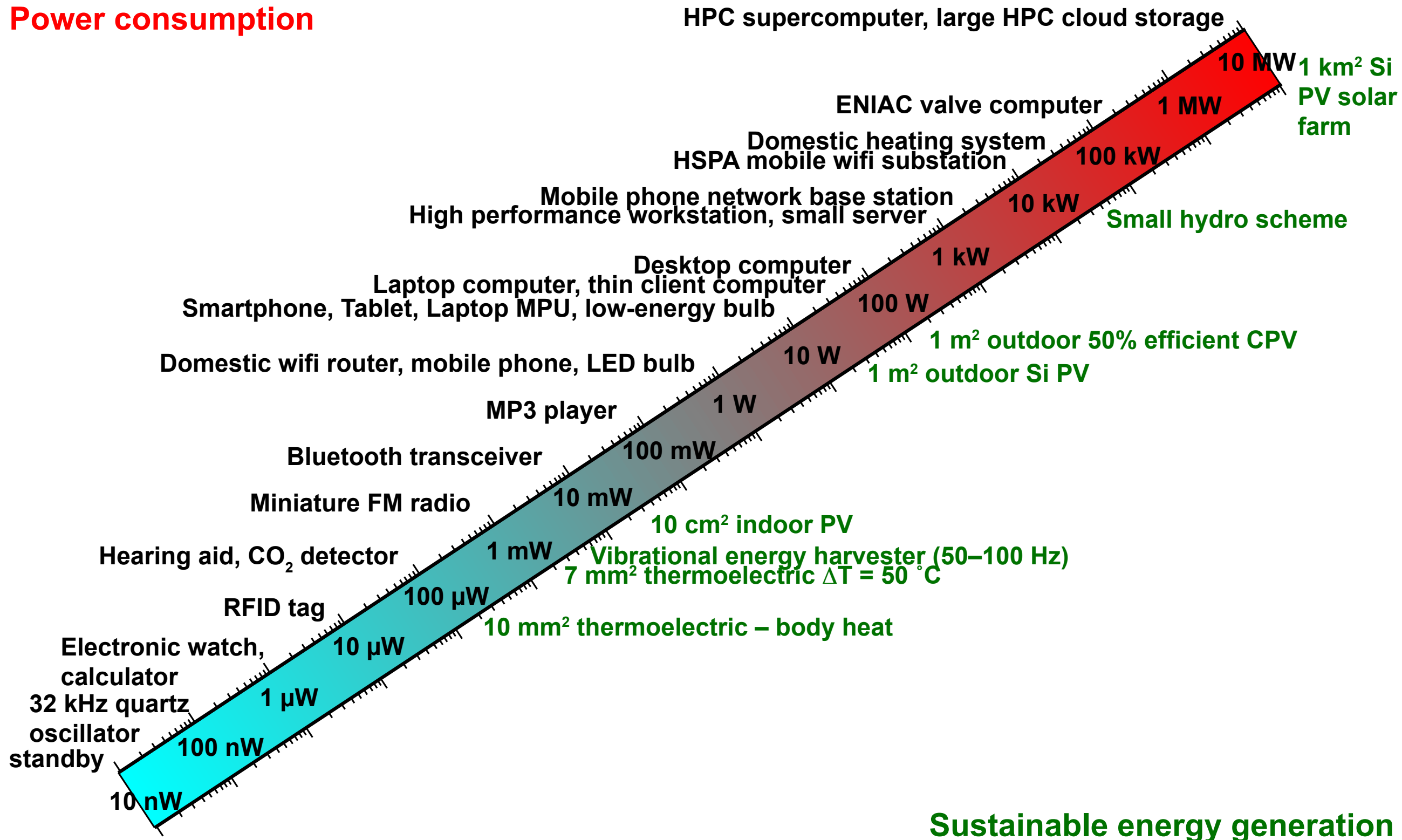
- Energy quality describes the ease (i.e.  $\eta$ )  
with which energy can be transformed

- A transition down the table will be more  
efficient than moving up the table

- Therefore solar heating is more efficient  
than photovoltaic electrical generation

- Expanded version from chemistry developed by Odum

## Power consumption



Sustainable energy generation



- **The available spectrum of solar energy varies around the globe**
- **Carnot efficiency limit 85% for solar energy**
- **Thermal heating most efficient use of solar energy  $\eta < 75\%$**
- **PV Shockley-Queisser maximum  $\eta \sim 31\%$  for single cell**
- **Trapping light important. Multi-junction & concentration offer higher  $\eta$  potential up to  $\sim 70\%$**
- **Low cost per Watt essential for large market penetration**